

# Study of $\Lambda$ N interaction via the $A=4$ mirror $\Lambda$ hypernuclei: ${}^4_{\Lambda}\text{H}$ and ${}^4_{\Lambda}\text{He}$

Department of Physics  
Tohoku University

Takeshi Koike

# TORIJIN-EFES- FJNSP LIA\* Joint Workshop on:

## “Next Generation Detector System for Nuclear Physics with RI beams”

GANIL, February 14-15, 2008

### February, 15

#### **Gamma-ray arrays**

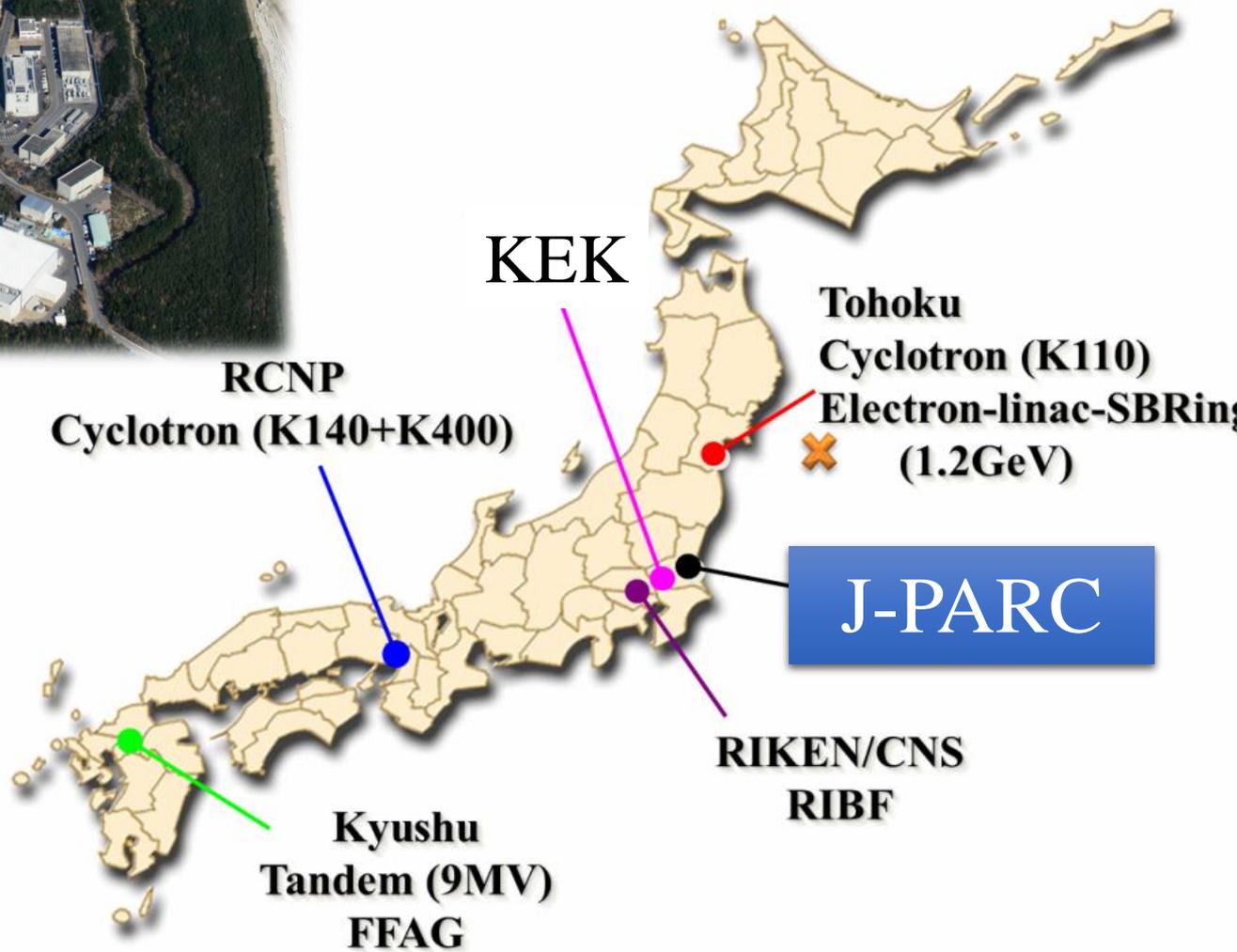
- 9:00 EXOGAM2, the upgrade of EXOGAM: E Clement+M Tripon (GANIL)
- 9:30 Digital Signal Processing for Germanium Detector: H Fukuchi (RIKEN)
- 10:00 AGATA: C Theisen (SPhN)
- 10:30 Hyper Ball: T Koike (Tohoku)
- 11:30 New crystals: C. Dathy (Saint Gobain)
- 12:00 GASPARD: D Beaumel (IPNO)
- 12:30 PARIS : J.P. Wieleczo (GANIL)

#### **Organizers:**

- Gilles de France (GANIL)
- Patricia Roussel-Chomaz (GANIL)
- Susumu Shimoura (CNS, University of Tokyo)
- Tohru Motobayashi (RIKEN)



**J-PARC**



# Our story and data: *J. Radiol. Prot.* 34 (2014) 675

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Journal of Radiological Protection

J. Radiol. Prot. 34 (2014) 675–698

doi:10.1088/0952-4746/34/3/675

Selected as highlights of 2014

## Comprehensive data on ionising radiation from Fukushima Daiichi nuclear power plant in the town of Miharu, Fukushima prefecture: The Mishi Project

T Koike<sup>1</sup>, Y Suzuki<sup>2</sup>, S Genyu<sup>3</sup>, I Kobayashi<sup>4</sup>, H Komori<sup>4</sup>,  
H Otsu<sup>5</sup>, H Sakuma<sup>6</sup>, K Sakuma<sup>6</sup>, E M Sarausad<sup>7,8</sup>,  
K Shimada<sup>9</sup>, T Shinozuka<sup>9</sup>, H Tamura<sup>1</sup>, K Tsukada<sup>1</sup>, M Ukai<sup>1</sup>,  
T O Yamamoto<sup>1</sup> and for The Mishi Project<sup>2</sup>



Mishi Project -Miharu-

Monitoring information of environmental radioactivity level

monitoring post -Miharu-

2016. 3. 7 AM 5:00

0.181 $\mu$ Sv/h

Japanese

English

<http://fukushima-misho.com/miharu>

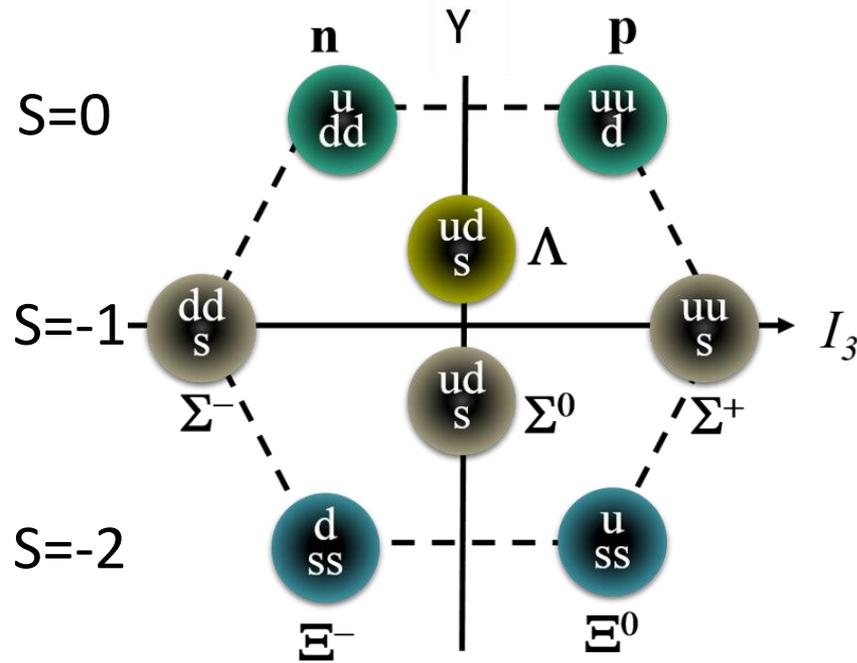


# Contents

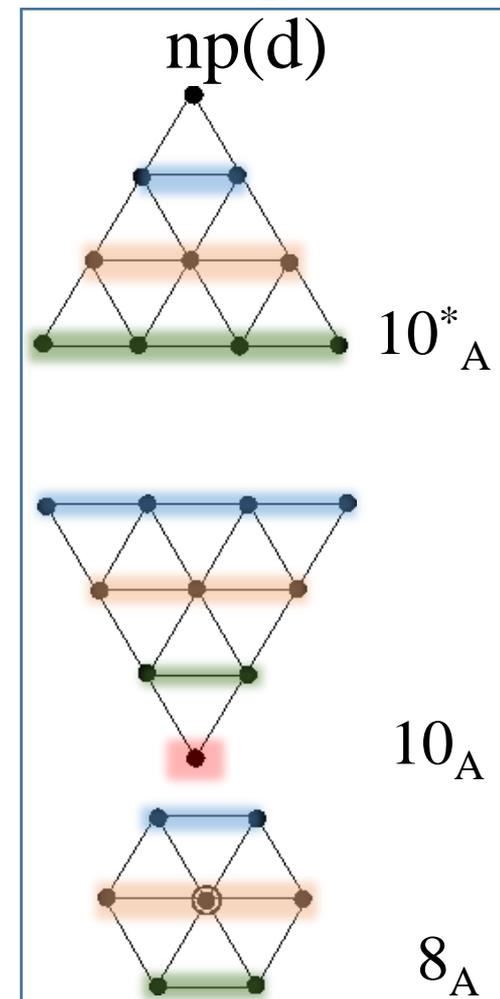
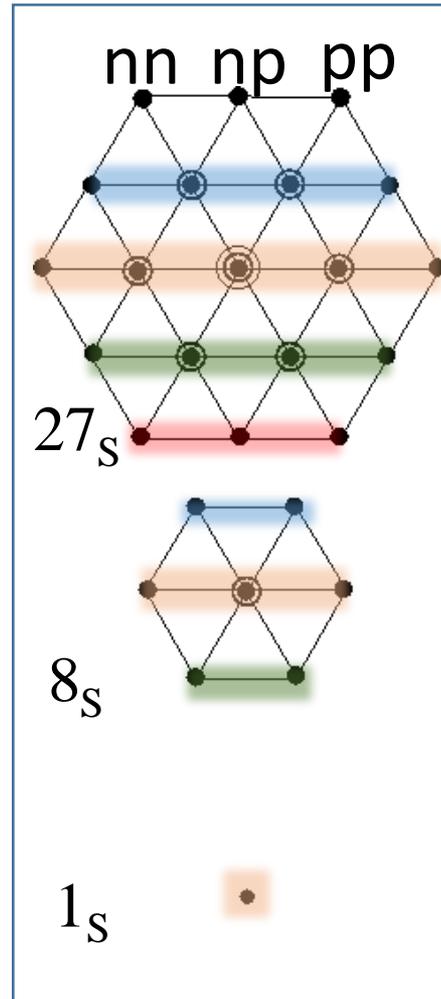
- Introduction
  - what we know about  $\Lambda N$  interaction
- Experimental confirmation of charge symmetry breaking in  $\Lambda N$  interaction
  - $A=4$  mirror  $\Lambda$  hypernuclei
- Theoretical studies
- Summary

# Baryon-Baryon interaction

Baryon octet:  $J^\pi=1/2^+$



$$8 \otimes 8 = \underbrace{27_S \oplus 8_S \oplus 1_S}_{^1S_0} \oplus \underbrace{10_A^* \oplus 10_A \oplus 8_A}_{^3S_1}$$



In  $SU(3)_f$  limit, no mixing among different multiplets.

# Difficulties of YN scattering experiments

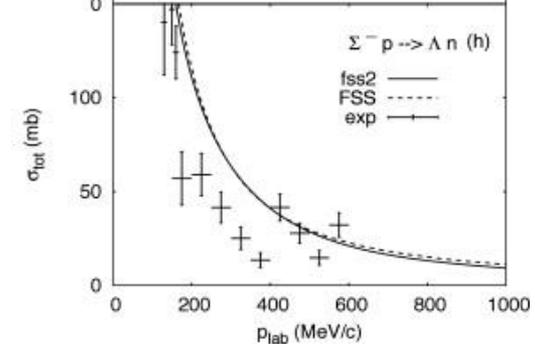
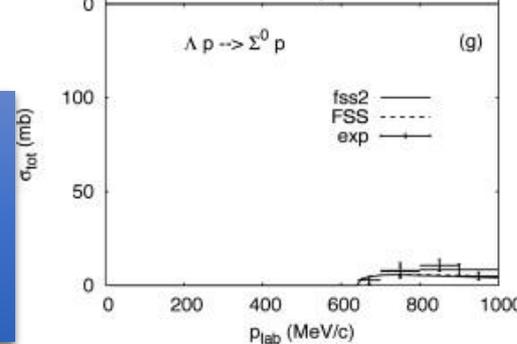
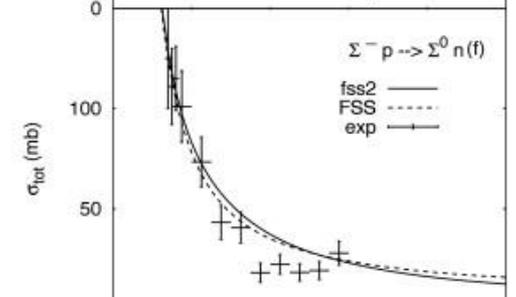
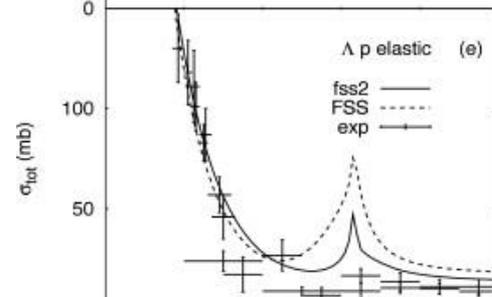
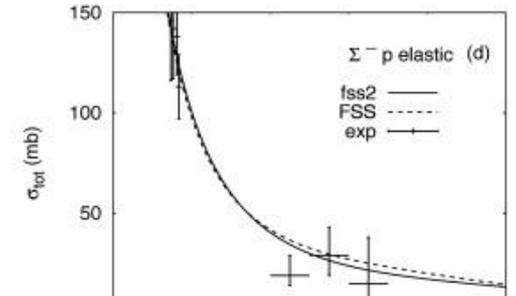
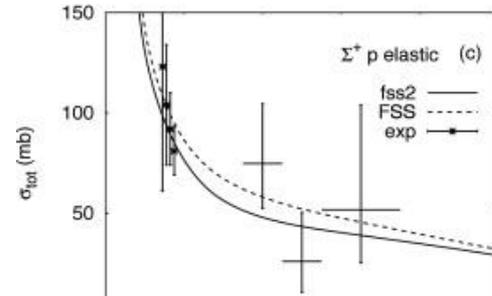
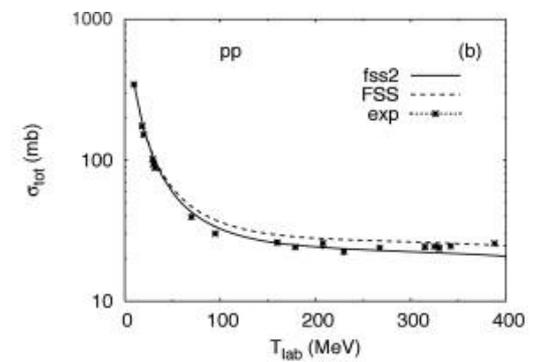
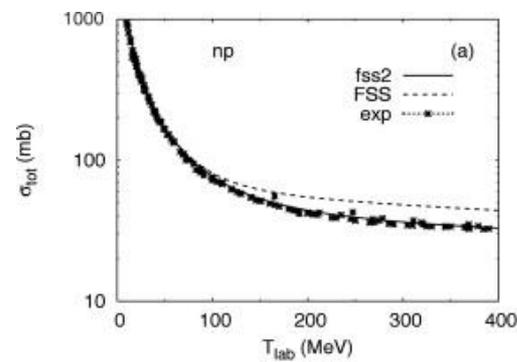
NN data  $\sim 4000$

YN data  $\sim 40$

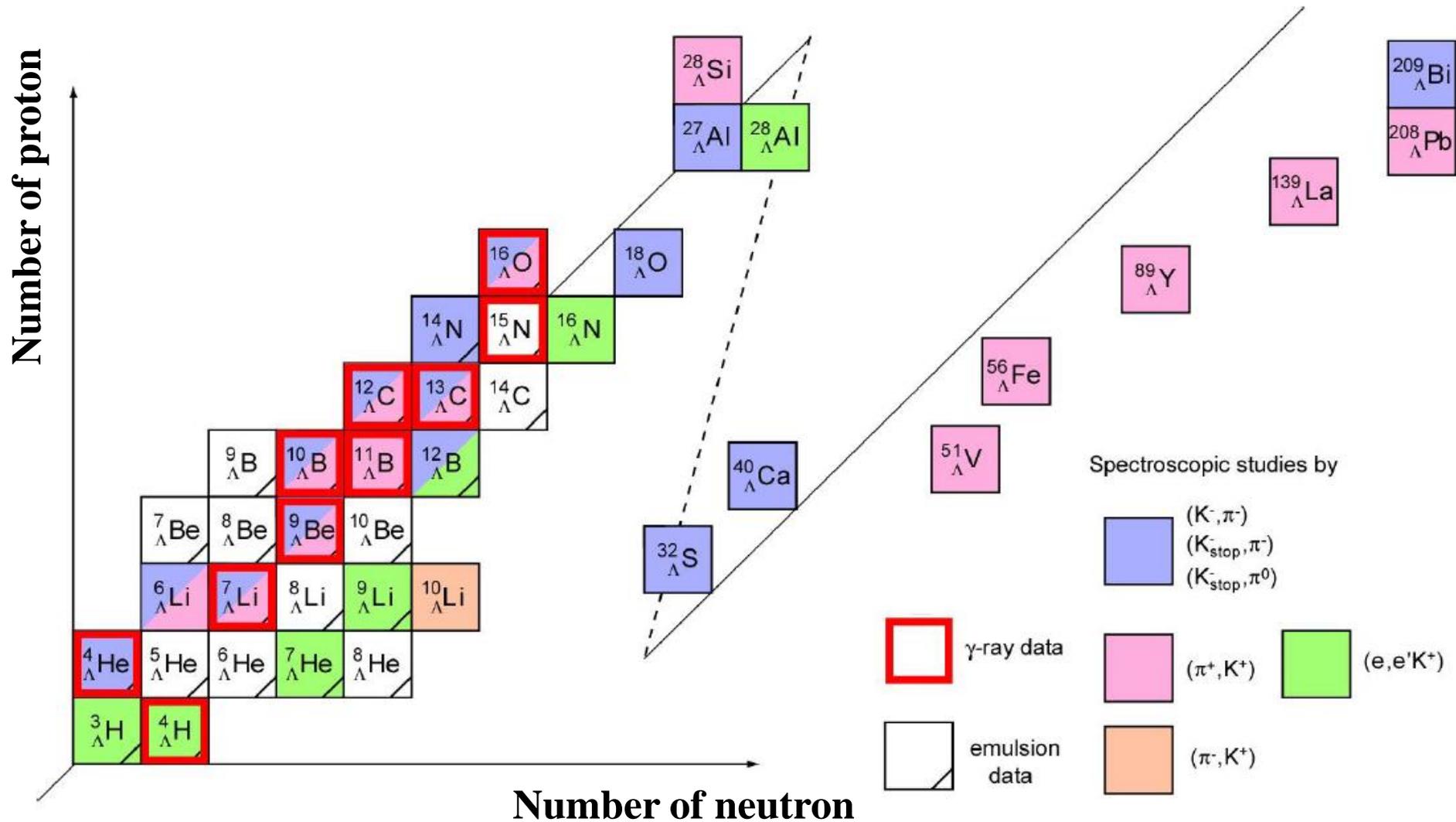
- $\tau_{\Lambda} : 263$  ps
- $\tau_{\Sigma^-} : 148$  ps
- $\tau_{\Xi^-} : 164$  ps



Extraction of YN interaction information from structures of hypernuclei

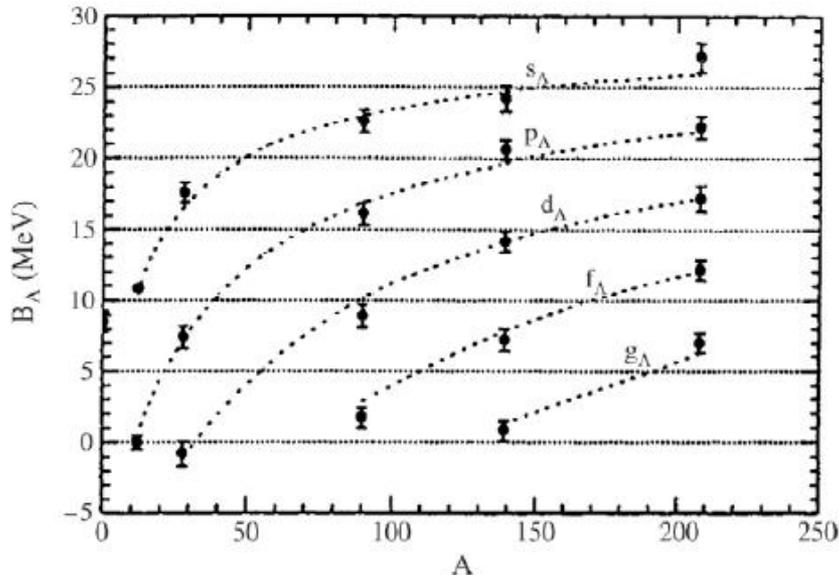
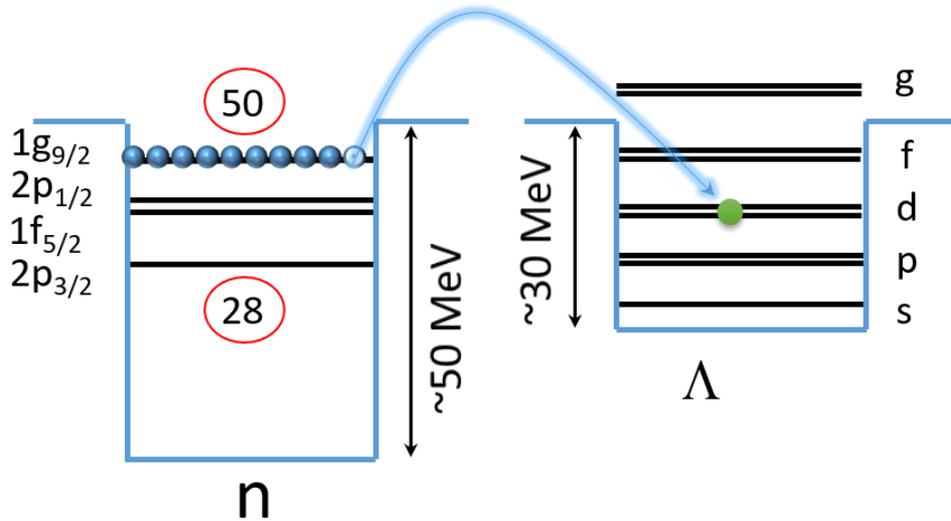


# $\Lambda$ Hypernuclear chart

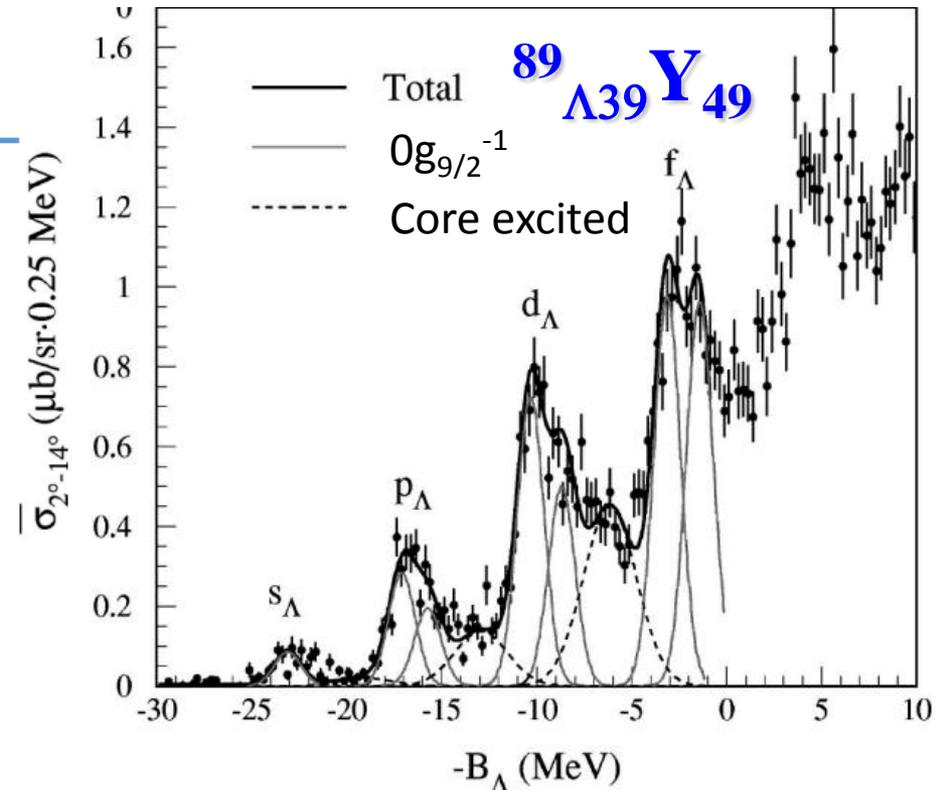


*Courtesy of H. Tamura*

# Missing mass spectroscopy



*Prog. Part. Nucl. Phys.* **57** (2006) 564



$^{89}\text{Y}(\pi^+, K^+)^{89}_\Lambda\text{Y}$  [KEK E369]

Counter experiment:

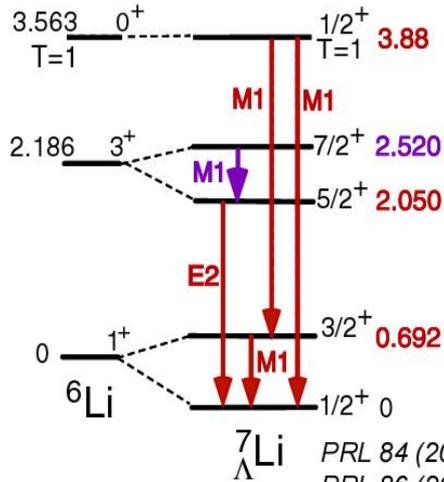
SKS magnet

FWHM = 1.6 MeV

*Phys. Rev. C.* **64** 044302 (2001)

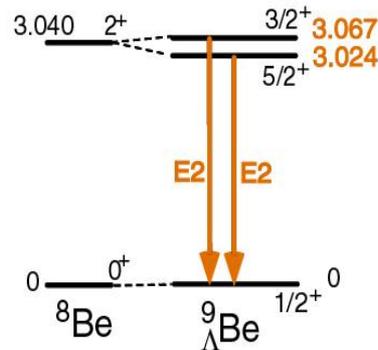
# $\gamma$ -ray transitions in $p$ -shell hypernuclei

${}^7\text{Li} (\pi^+, K^+\gamma)$  KEK E419



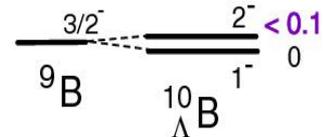
${}^7\text{Li}$  PRL 84 (2000) 5963  
 PRL 86 (2001) 1982  
 PLB 579 (2004) 258  
 PRC 73 (2006) 012501

${}^9\text{Be} (K^-, \pi^-\gamma)$  BNL E930('98)



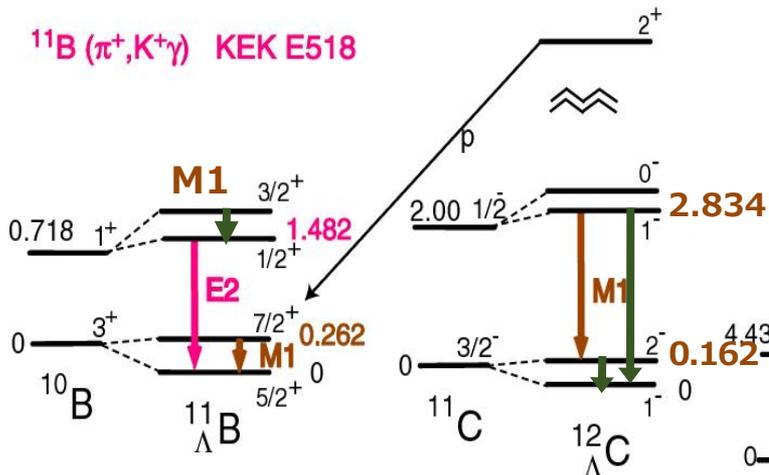
PRL 88 (2002) 082501  
 NPA 754 (2005) 58c

${}^{10}\text{B} (K^-, \pi^-\gamma)$  BNL E930('01)



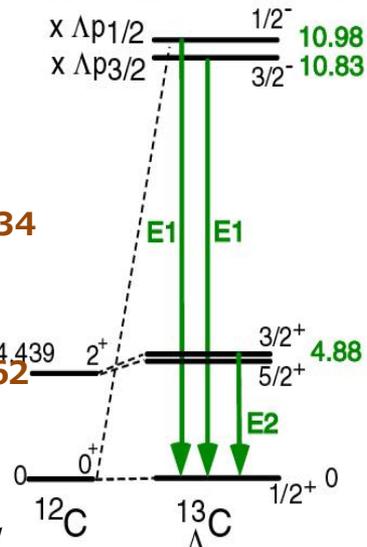
NPA 754 (2005) 58c

${}^{12}\text{C} (\pi^+, K^+\gamma)$  KEK E566



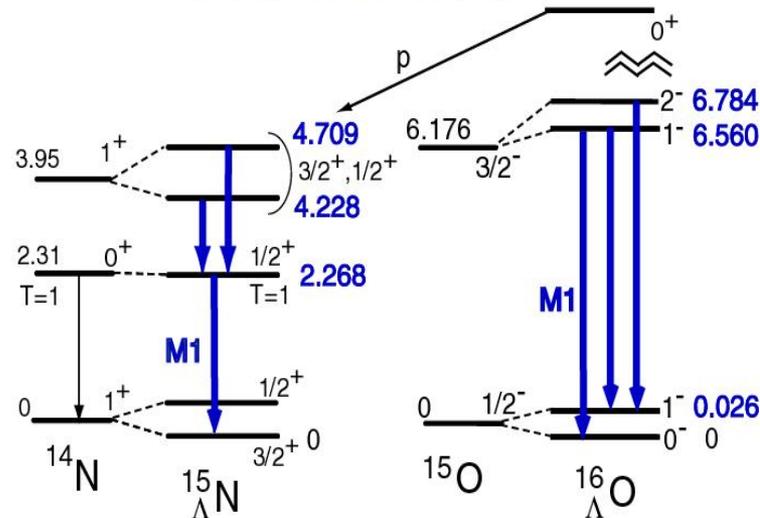
PTEP (2015) 081D01

${}^{13}\text{C} (K^-, \pi^-\gamma)$  BNL E929 (NaI)



PRL 86 (2001) 4255  
 PRC 65 (2002) 034607

${}^{16}\text{O} (K^-, \pi^-\gamma)$  BNL E930('01)



PRL 93 (2004) 232501

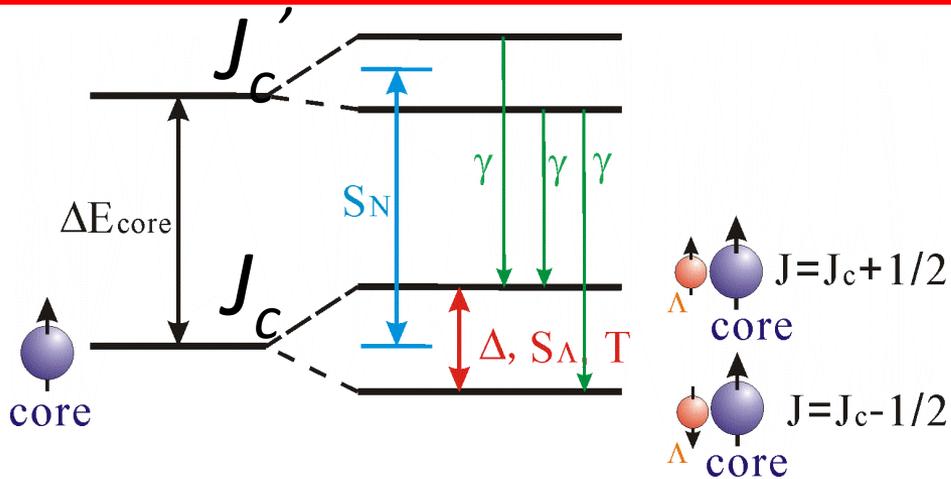
NPA 754 (2005) 58c

Y. Ma, Ph.D Thesis (2009),

# Effective two-body $\Lambda N$ interaction

$$V_{\Lambda N}^{\text{eff}} = V_0(r) + \underbrace{V_\sigma(r)}_{\Delta} \vec{s}_\Lambda \vec{s}_N + \underbrace{V_\Lambda(r)}_{S_\Lambda} \vec{l}_{\Lambda N} \vec{s}_\Lambda + \underbrace{V_N(r)}_{S_N} \vec{l}_{\Lambda N} \vec{s}_N + \underbrace{V_T(r)}_T S_{12}$$

*p*-shell : 4 radial integrals for  $p_N s_\Lambda$  w.f.

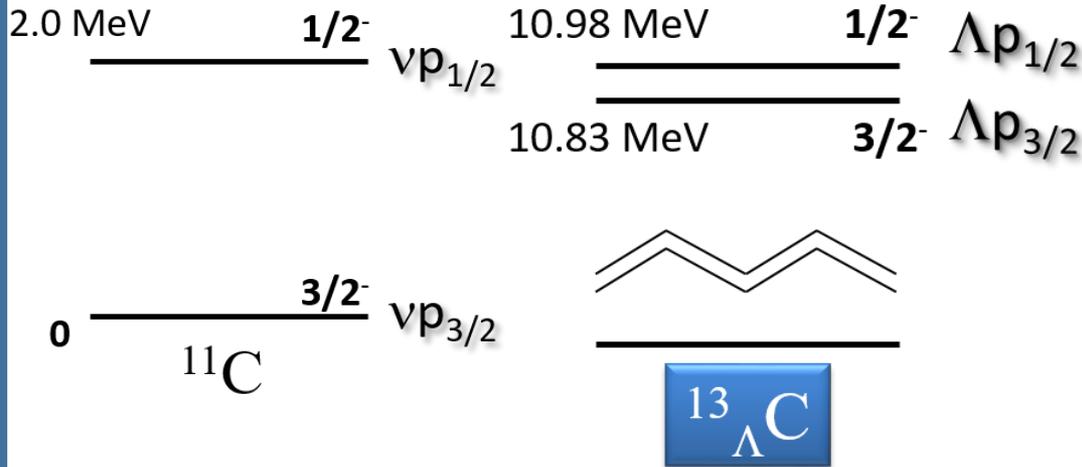


spin-spin  $\Delta=0.43$  or  $0.33$  MeV  
 $\Lambda$  spin-orbit:  $S_\Lambda=-0.02$  MeV  
 $N$  spin-orbit  $S_N=-0.4$   
 Tensor  $T=0.03$

*D. J. Millener, NPA 881 (2012) 298.*

	$J_u^\pi$	$J_l^\pi$	$\Lambda\Sigma$	$\Delta$	$S_\Lambda$	$S_N$	$T$	$\Delta E^{th}$	$\Delta E^{exp}$
${}^7_\Lambda\text{Li}$	$3/2^+$	$1/2^+$	72	628	-1	-4	-9	693	692
${}^7_\Lambda\text{Li}$	$7/2^+$	$5/2^+$	74	557	-32	-8	-71	494	471
${}^9_\Lambda\text{Be}$	$3/2^+$	$5/2^+$	-8	-14	37	0	28	44	43
${}^{11}_\Lambda\text{B}$	$7/2^+$	$5/2^+$	56	339	-37	-10	-80	267	264
${}^{11}_\Lambda\text{B}$	$3/2^+$	$1/2^+$	61	424	-3	-44	-10	475	505
${}^{12}_\Lambda\text{C}$	$2^-$	$1^-$	61	175	-12	-13	-42	153	161
${}^{15}_\Lambda\text{N}$	$3/2_2^+$	$1/2_2^+$	65	451	-2	-16	-10	507	481
${}^{16}_\Lambda\text{O}$	$1^-$	$0^-$	-33	-123	-20	1	188	23	26
${}^{16}_\Lambda\text{O}$	$2^-$	$1_2^-$	92	207	-21	1	-41	248	224

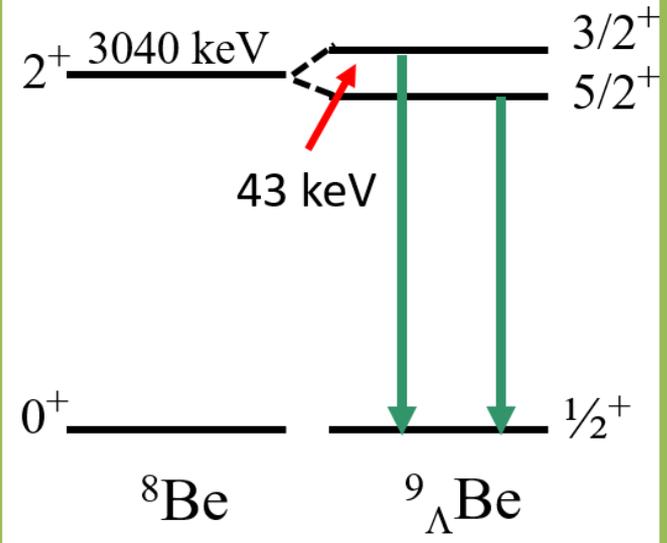
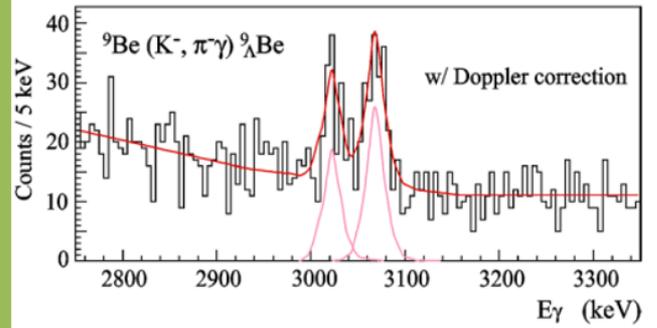
# Small $\Lambda N$ spin-orbit force



$^{13}\text{C}(\text{K}^-, \pi^-)^{13}_{\Lambda}\text{C}$   
 BNL E929  
 $\gamma$ -ray spectroscopy  
 NaI(Tl) array

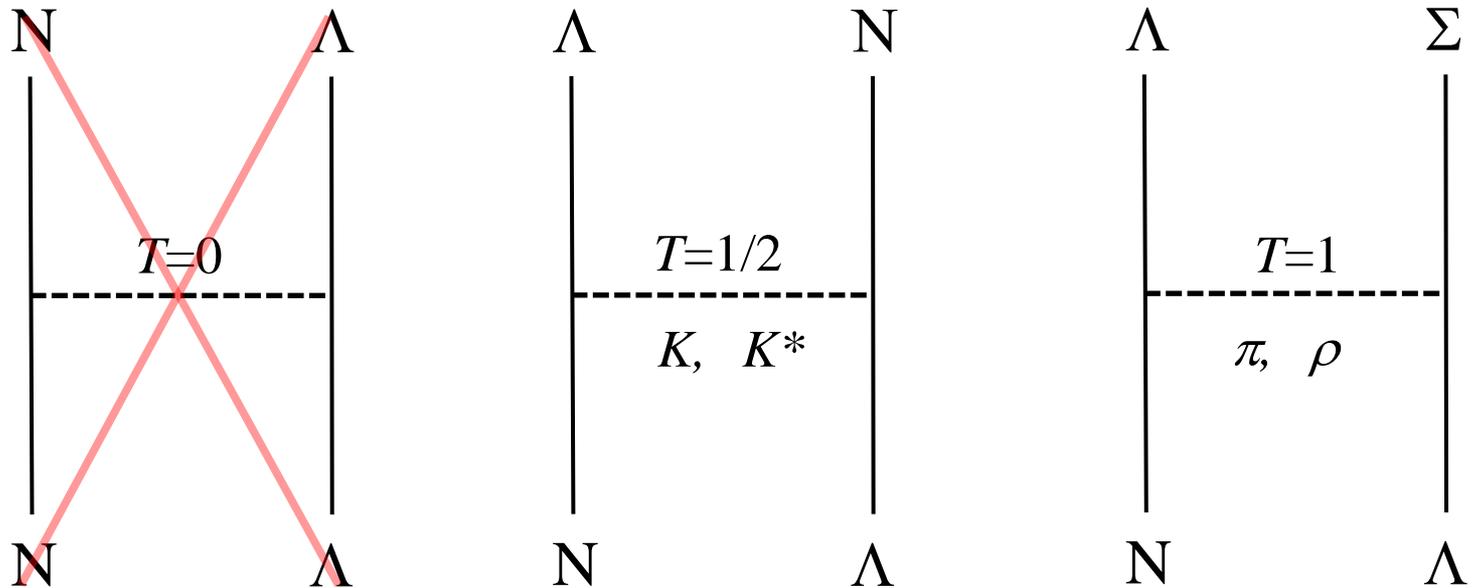
PRL **86** 4255(2001)  
 PRC **65** 034607(2002)

$(\text{K}^-, \pi^-)$  E930 @BNL  
 Hyperball



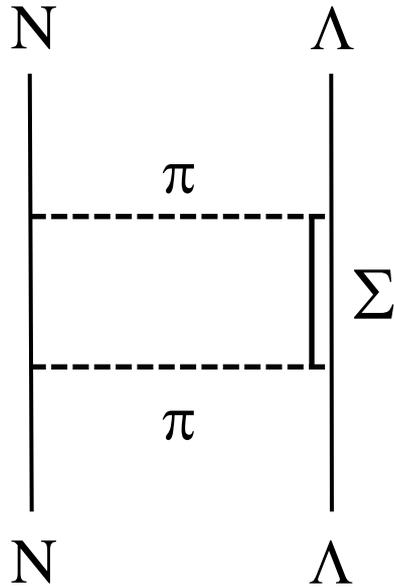
H. Akikawa et al, PRL **88** 082501 (2002)

# $\Lambda N$ interaction

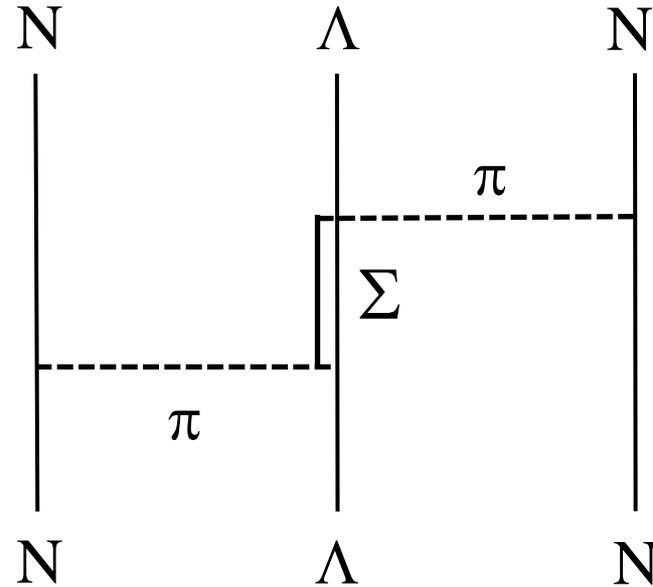


No one pion exchange because of isospin conservation  
→  $\Lambda N$  interaction is medium to short in range

# $\Lambda N$ interaction: $\Lambda N$ - $\Sigma N$ coupling



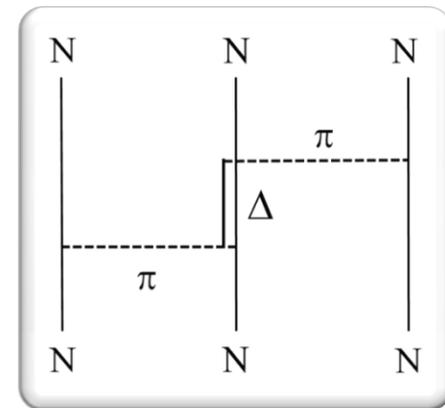
Two-body



Three-body

$$(m_{\Sigma} - m_{\Lambda}) \approx 75 \text{ MeV} < (m_{\Delta} - m_{N}) \approx 300 \text{ MeV}$$

➔  $\Lambda NN > NNN$



# Summary on $\Lambda$ N interaction studies

- Experimentally most well studied among YN interaction
- Spin dependent term determined for p-shell by  $\gamma$ -ray spectroscopy
- Independent particle picture is valid for also  $\Lambda$ 
  - $U_{\Lambda}/U_N \sim 2/3$
- Small spin-orbit force (by an order of magnitude)
  - Magic number for  $\Lambda \rightarrow$  HO shell gap
- One pion exchange forbidden (medium to short range nuclear force)
  - Zero isospin of  $\Lambda$
- $\Lambda$ N- $\Sigma$ N coupling is stronger than the nuclear counter part
  - $m_{\Sigma}-m_{\Lambda} \approx 75$  MeV

Large charge symmetry breaking (CSB) ?

# Experimental breakthroughs in 2015

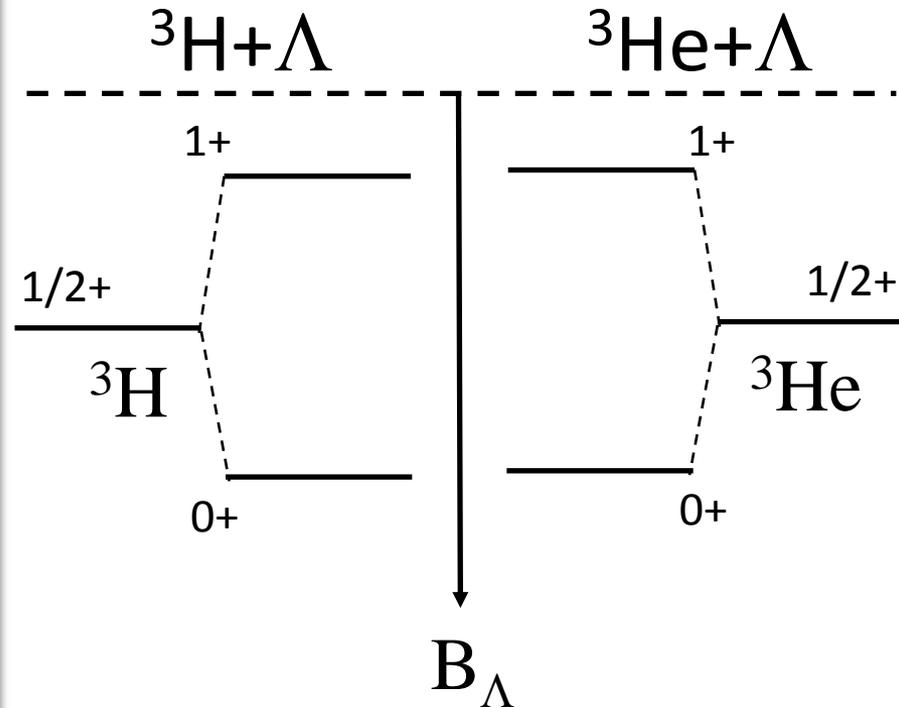
Experimental confirmation of large charge symmetry breaking (CSB) in  $\Lambda N$  interaction

# How much energy ( $B_\Lambda$ ) the system will gain by adding $\Lambda$ in $A=3$ nuclear system?

$\Lambda$  has no charge!!

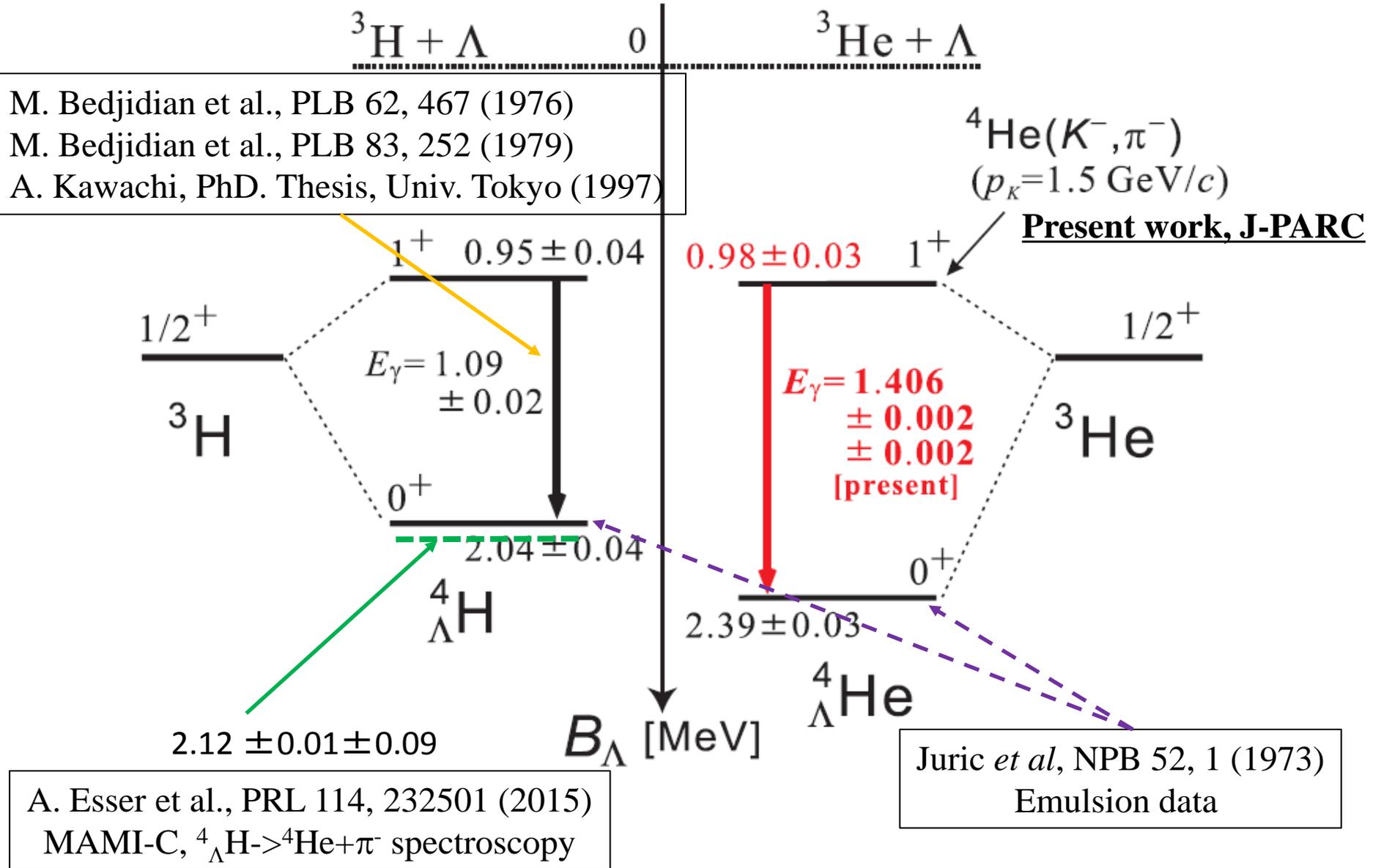
- $\Delta B_\Lambda$ : measure of pure (no Coulomb contribution) CSB effect of  $\Lambda N$  interaction.
- $\Delta B_\Lambda$  would be the same or much smaller than NN
- A few keV sensitivity via  $\gamma$ -ray spectroscopy with bound excited states.

naïve expectation



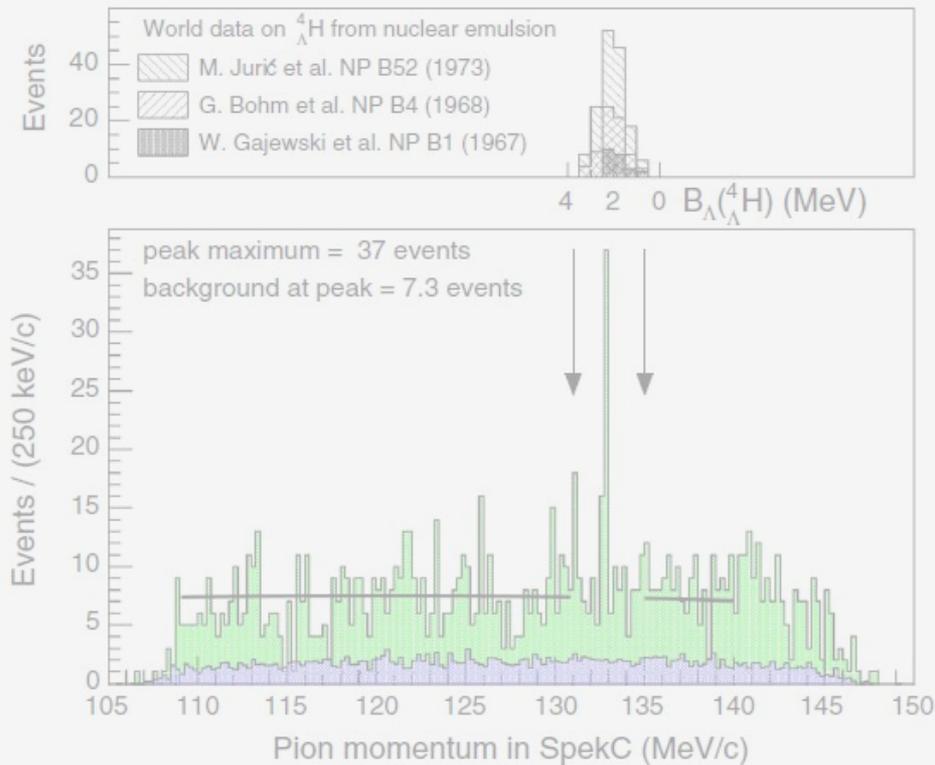
$$(J_{core} = \frac{1}{2}) \otimes (J_\Lambda = \frac{1}{2})$$

# A=4 mirror $\Lambda$ -hypernuclei



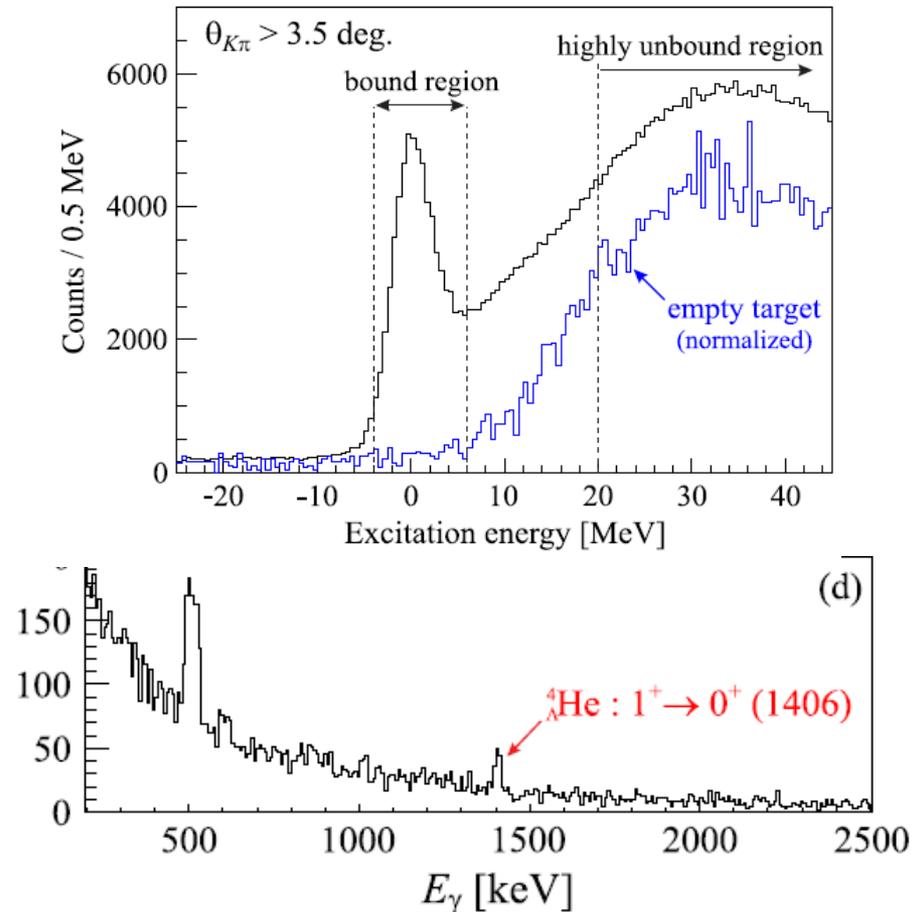
# Experimental breakthroughs

## Binding energy of ${}^4_{\Lambda}\text{H}$ ( $0^+$ )



*Phys. Rev. Lett.* 114, 232501 (2015)

## Energy of ${}^4_{\Lambda}\text{He}$ ( $1^+ \rightarrow 0^+$ )



*Phys. Rev. Lett.* 115, 222501 (2015)



## Observation of Spin-Dependent Charge Symmetry Breaking in $\Lambda N$ Interaction: Gamma-Ray Spectroscopy of ${}^4_{\Lambda}\text{He}$

T. O. Yamamoto,<sup>1</sup> M. Agnello,<sup>2,3</sup> Y. Akazawa,<sup>1</sup> N. Amano,<sup>4</sup> K. Aoki,<sup>5</sup> E. Botta,<sup>3,6</sup> N. Chiga,<sup>1</sup> H. Ekawa,<sup>7</sup> P. Evtoukhovitch,<sup>8</sup> A. Feliciello,<sup>3</sup> M. Fujita,<sup>1</sup> T. Gogami,<sup>7</sup> S. Hasegawa,<sup>9</sup> S. H. Hayakawa,<sup>10</sup> T. Hayakawa,<sup>10</sup> R. Honda,<sup>10</sup> K. Hosomi,<sup>9</sup> S. H. Hwang,<sup>9</sup> N. Ichige,<sup>1</sup> Y. Ichikawa,<sup>9</sup> M. Ikeda,<sup>1</sup> K. Imai,<sup>9</sup> S. Ishimoto,<sup>5</sup> S. Kanatsuki,<sup>7</sup> M. H. Kim,<sup>11</sup> S. H. Kim,<sup>11</sup> S. Kinbara,<sup>12</sup> T. Koike,<sup>1</sup> J. Y. Lee,<sup>13</sup> S. Marcello,<sup>3,6</sup> K. Miwa,<sup>1</sup> T. Moon,<sup>13</sup> T. Nagae,<sup>7</sup> S. Nagao,<sup>1</sup> Y. Nakada,<sup>10</sup> M. Nakagawa,<sup>10</sup> Y. Ogura,<sup>1</sup> A. Sakaguchi,<sup>10</sup> H. Sako,<sup>9</sup> Y. Sasaki,<sup>1</sup> S. Sato,<sup>9</sup> T. Shiozaki,<sup>1</sup> K. Shirotori,<sup>14</sup> H. Sugimura,<sup>9</sup> S. Suto,<sup>1</sup> S. Suzuki,<sup>5</sup> T. Takahashi,<sup>5</sup> H. Tamura,<sup>1</sup> K. Tanabe,<sup>1</sup> K. Tanida,<sup>9</sup> Z. Tsamalaidze,<sup>8</sup> M. Ukai,<sup>1</sup> Y. Yamamoto,<sup>1</sup> and S. B. Yang<sup>13</sup>

(J-PARC E13 Collaboration)

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<sup>5</sup>*Institute of Particle and Nuclear Studies (IPNS), High Energy Accelerator Research Organization (KEK), Tsukuba 305-0801, Japan*

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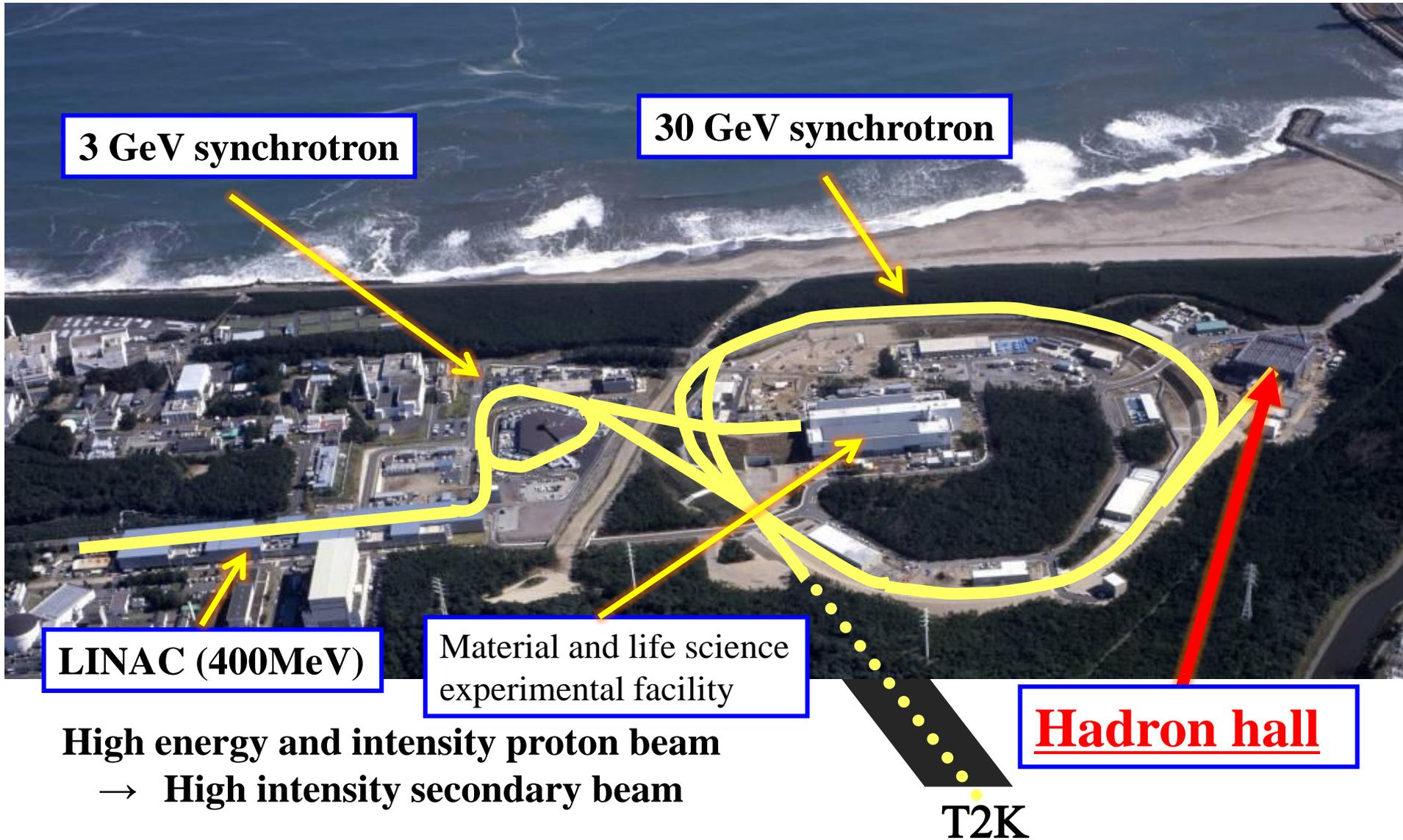
<sup>13</sup>*Department of Physics and Astronomy, Seoul National University, Seoul 151-747, Korea*

<sup>14</sup>*Research Center of Nuclear Physics, Osaka University, Ibaraki 567-0047, Japan*

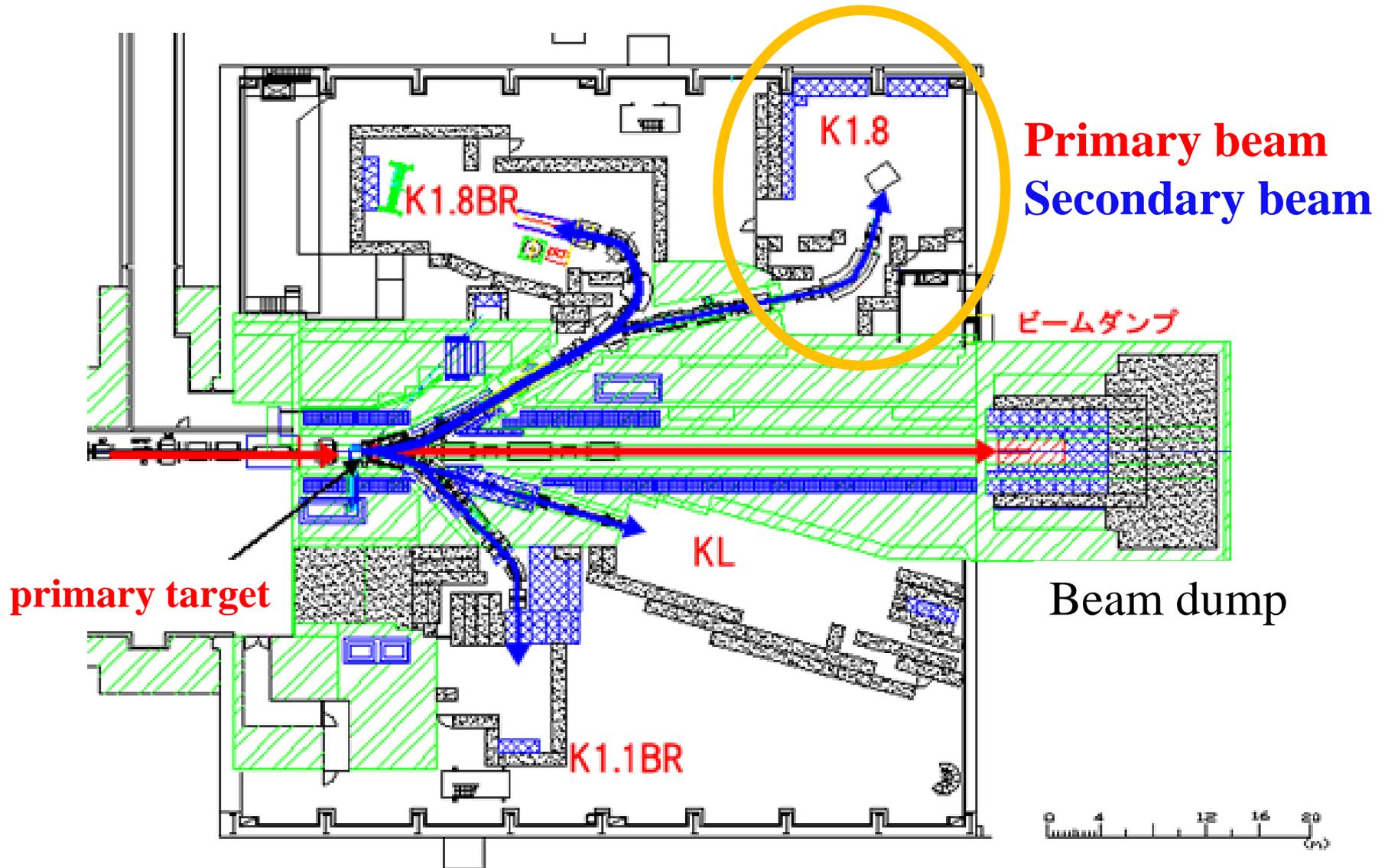
(Received 12 August 2015; published 24 November 2015)

# J-PARC

(Japan Proton Accelerator Research Complex)

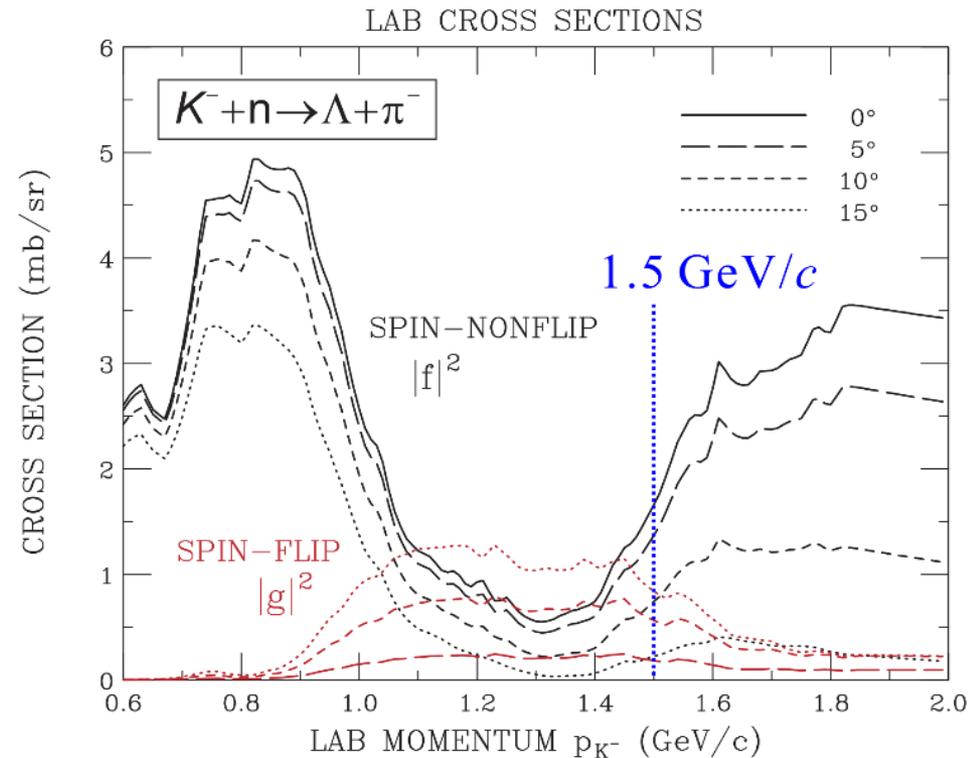


# Hadron Experimental Facility



# $\gamma$ -ray spectroscopy of ${}^4_{\Lambda}\text{He}$ (J-PARC E13)

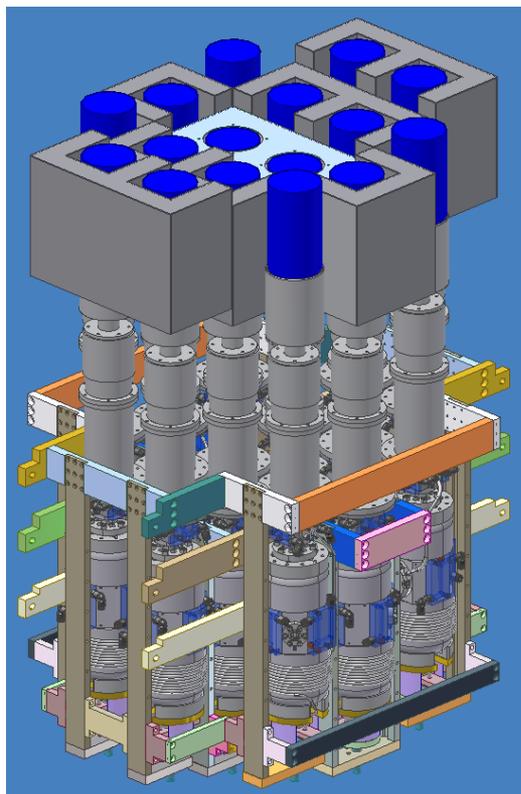
Reaction:  ${}^4\text{He}(K^-, \pi^-){}^4_{\Lambda}\text{He}$   
Beam mom.:  $P_{K^-} = 1.5 \text{ GeV}/c$   
Target: Liq.  ${}^4\text{He}$ ,  $2.8 \text{ g}/\text{cm}^2$   
Reaction- $\gamma$  coincidence



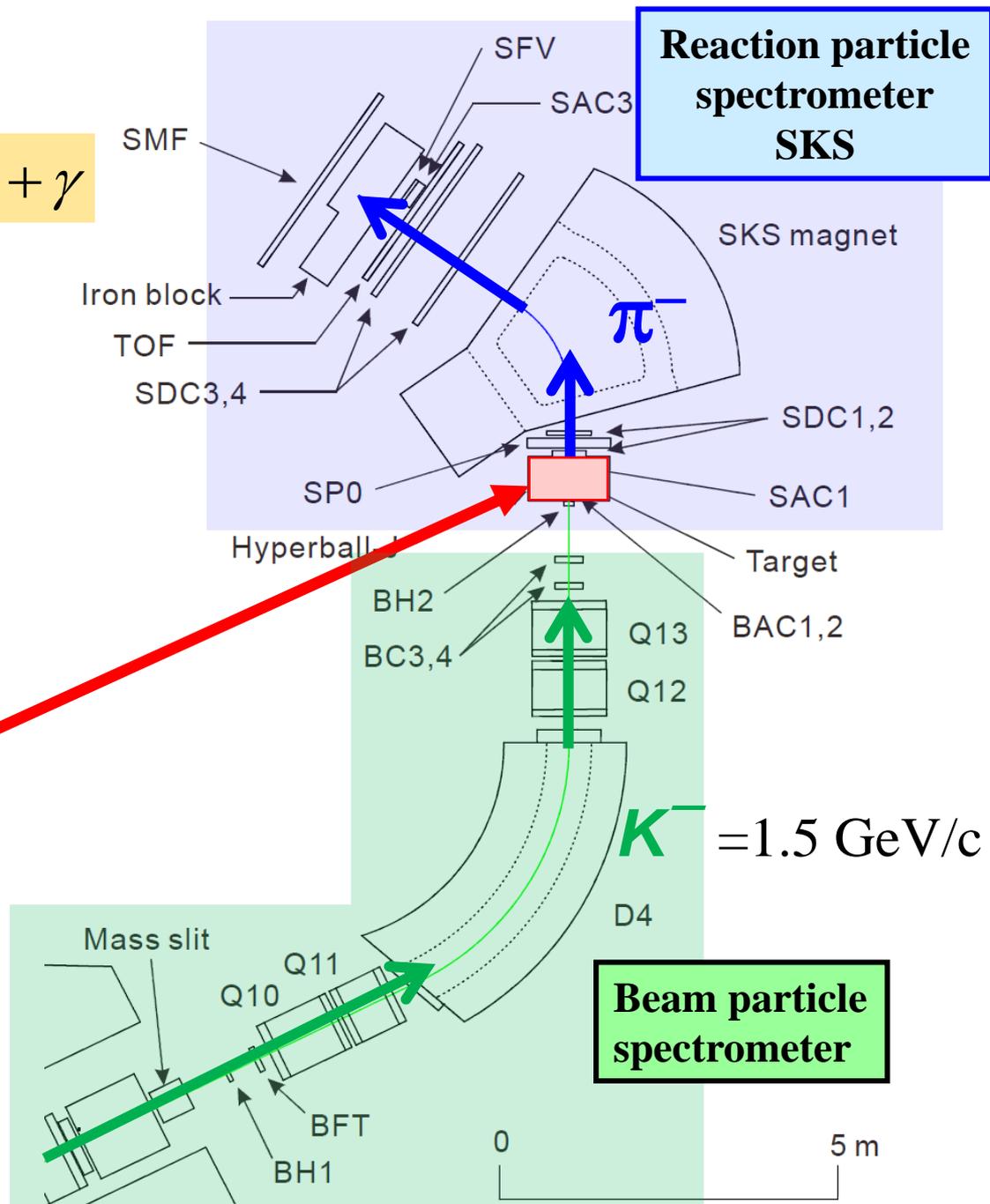
*T. Harada, private communication (2006)*

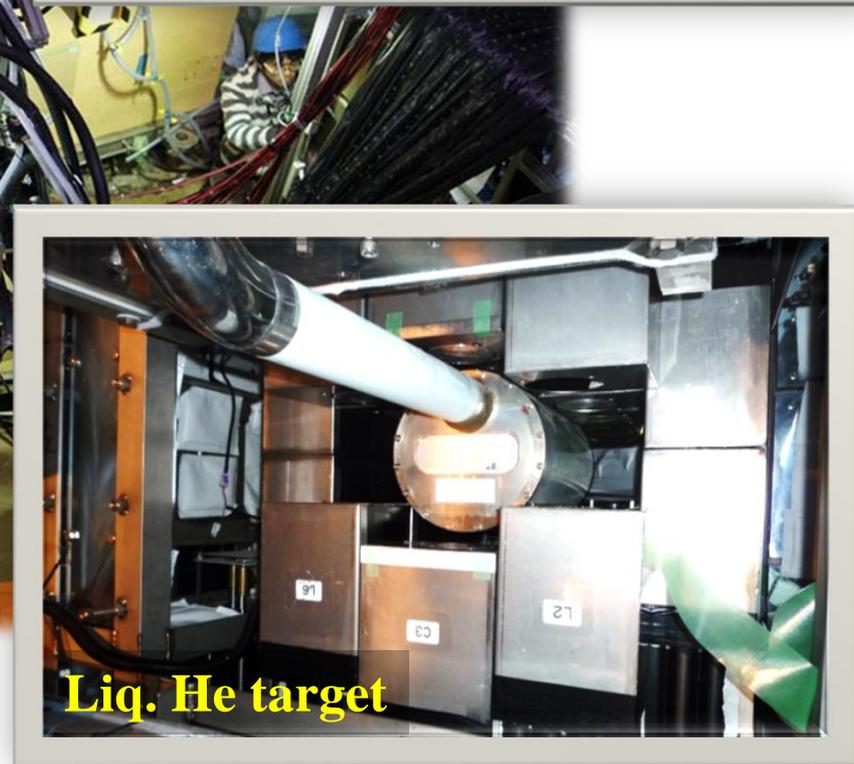
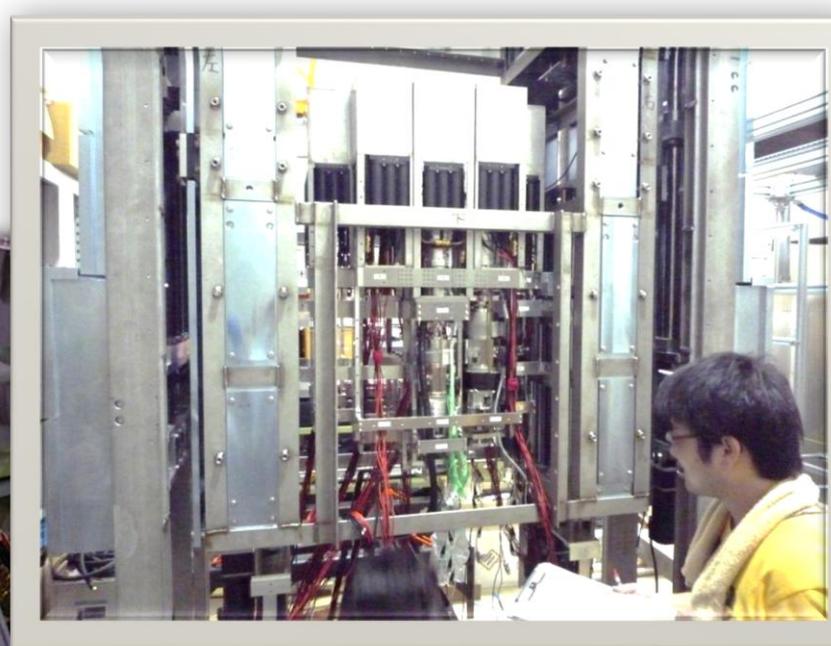
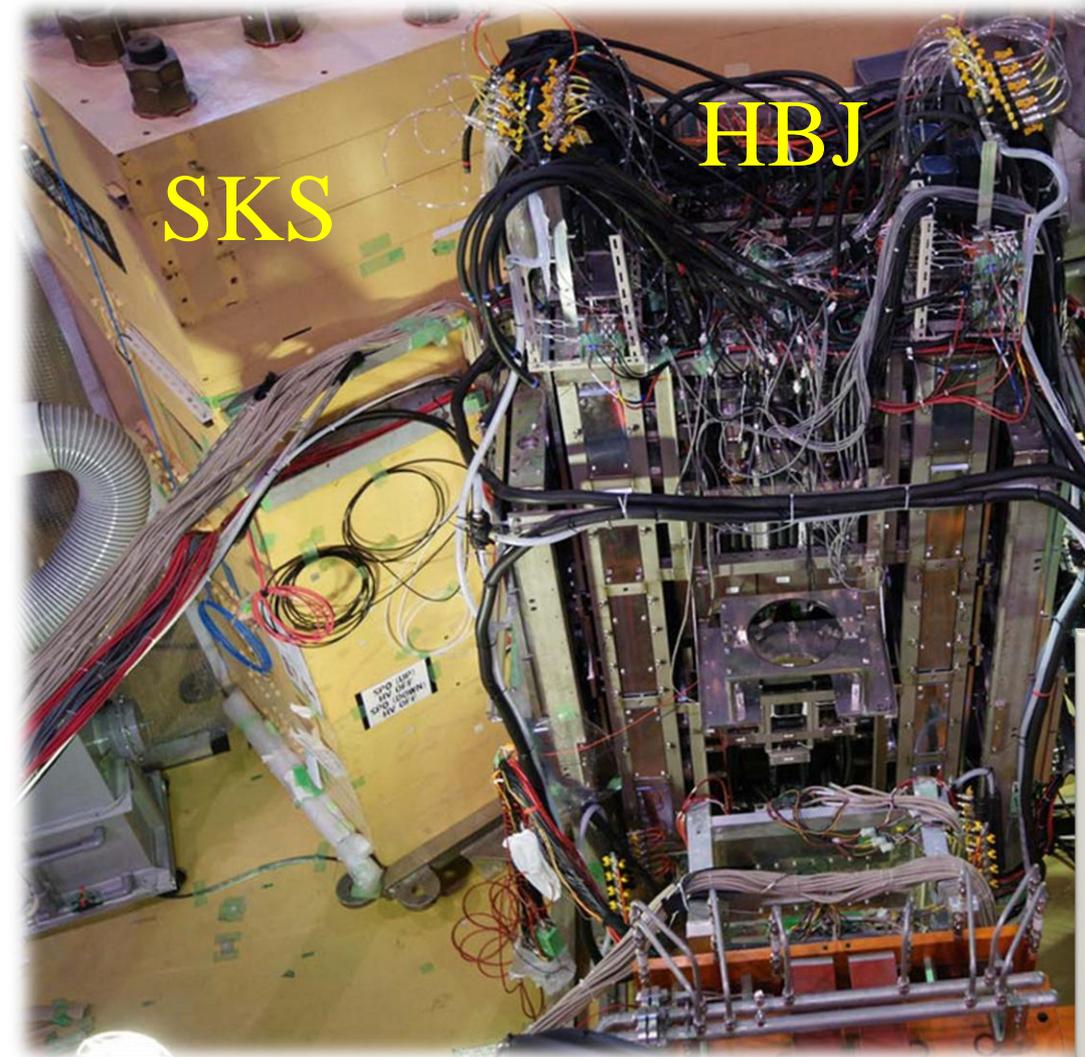


Ge-array



Hyperball-J





# A=4 mirror $\Lambda$ -hypernuclei

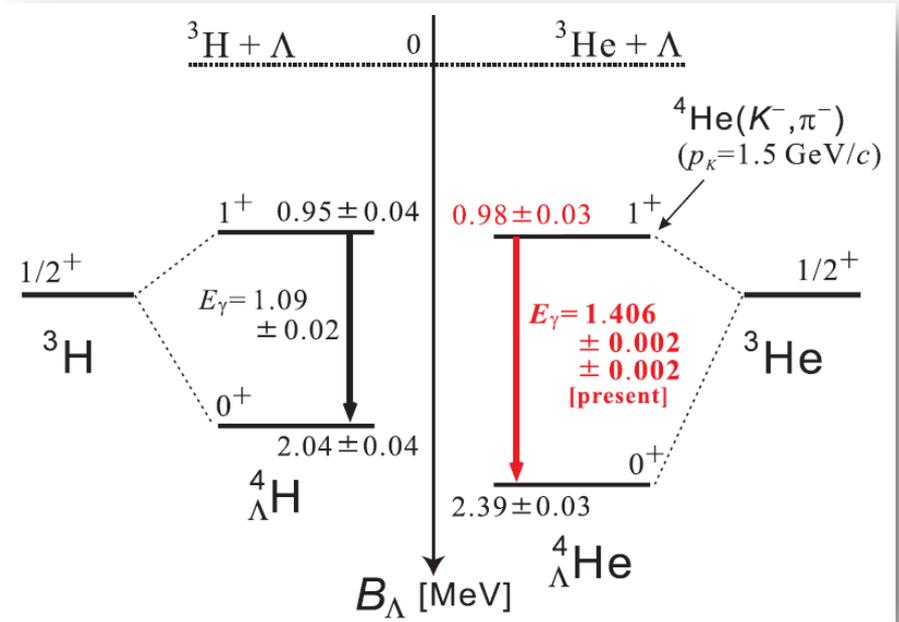
$$\Delta B_{\Lambda}(\text{g.s.}) = B_{\Lambda}(0^{+}; {}^4_{\Lambda}\text{He}) - B_{\Lambda}(0^{+}; {}^4_{\Lambda}\text{H}) = 270 \pm 100 \text{ keV}$$

$$\Delta E_{\gamma}(1^{+} \rightarrow 0^{+}) = E_{\gamma}({}^4_{\Lambda}\text{He}) - E_{\gamma}({}^4_{\Lambda}\text{H}) = 316 \pm 40 \text{ keV}$$

$$\Delta B_{\Lambda}(1^{+}) = B_{\Lambda}(1^{+}; {}^4_{\Lambda}\text{He}) - B_{\Lambda}(1^{+}; {}^4_{\Lambda}\text{H}) = 50 \pm 100 \text{ keV}$$

## CSB effect in $\Lambda\text{N}$

- Sizable
- Spin dependent



# CSB in mirror nuclei: ${}^3\text{H}$ & ${}^3\text{He}$

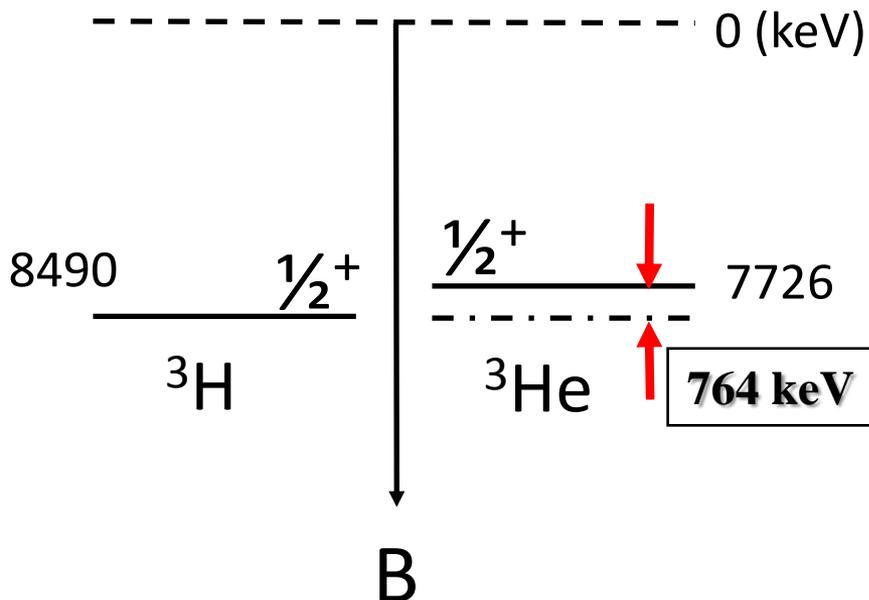


TABLE IV. Contributions of the various terms of the interaction to the  ${}^3\text{H}$ - ${}^3\text{He}$  mass difference  $D$ . The AV18+UIX potential has been used.

Interaction term	$D$ (keV)
<u>Nuclear CSB</u>	<u>65</u>
Point Coulomb	677
Full Coulomb	648
Magnetic moment	17
Orbit-orbit force	7
$n$ - $p$ mass difference	14
Total (theory)	751
Experiment	<u>764</u>

*Nogga et al., Phys. Rev. C 67 034004 (2003)*

xPT calculation

Coulomb	Breit	$(E_k)$	Two-body	Three-body	Theory	Experiment
648	28	14	65(22)	5	760(22)	764

*J. L. Friar, G. L. Payne, and U. van Kolck, Phys. Rev. C 71, 024003 (2005)*

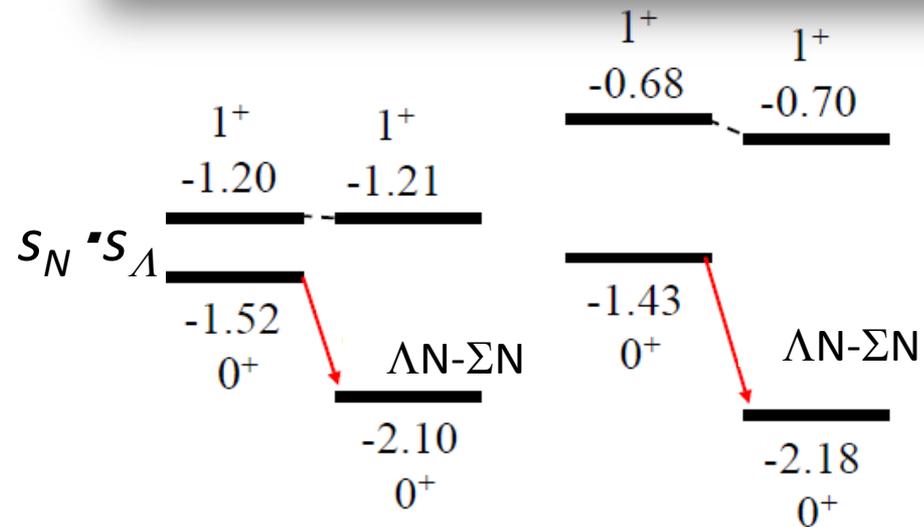
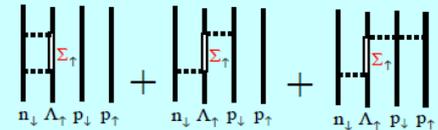
# Effect of $\Lambda N$ - $\Sigma N$ coupling in ${}^4_{\Lambda}\text{He}$

- w.f.: Core +  $\Lambda$
- $\Lambda\text{NN}$ -3BYN
- Simulated Nijmegen soft-core potential
  - SC97e,f(S)
- Spin doublet spacing in  $A=4$  system
  - $s_N \cdot s_{\Lambda} + \Lambda N$ - $\Sigma N$
- Large effect on  $0^+$ 
  - Coherent coupling

*Hyperon-mixing*

${}^4_{\Lambda}\text{He}$

$\Lambda\text{NN}$  three-body force



$$P_{\text{coh.}\Sigma} = 0.7\%$$

$$P_{\text{coh.}\Sigma} = 0.9\%$$

SC97e(S)

SC97f(S)

# Relatively recent theoretical studies

- a. A. Nogga et al., PRL88 172501 (2002)
  - $\Lambda$ NNN four-body calculation
  - NSC97e ( $\Lambda$ N- $\Sigma$ N tensor term strong)
- b. A. Gal PLB 744 352 (2015)
  - Akaishi-formalism + explicit CSB term via mixing of  $\Lambda\Sigma^0$  to  $\Lambda\Sigma$  strong interaction.
- c. D. Gazda and A. Gal PRL (in press) ,  
arXiv:1512.01049 (2016)
  - Ab-initio No Core Shell Model (NCSM) with  $\chi$ EFT YN interaction
    - N3LO NN + N2LO NN + LO/NLO YN
    - Inclusion of explicit  $\Lambda$ N- $\Sigma$ N interaction

(Unit in MeV)	Exp	a	b	c
$B_{\Lambda}(0^+)$	0.27(10)	0.07	0.22	0.18(10)
$B_{\Lambda}(1^+)$	0.05(10)	-0.01	0.03	-0.20(2)

# Summary

- NN strong interaction to more general baryon-baryon interaction
  - $\Lambda$ N interaction is the first step with Strangeness=-1
  - YN scattering experiments difficult  $\rightarrow$  study of hypernuclei
- New data on  $A=4$   ${}^4_{\Lambda}\text{H}$  and  ${}^4_{\Lambda}\text{He}$  from MAMI-C and J-PARC
- $\Lambda$ N CSB is confirmed.
  - Larger than NN (unexpected)  $\rightarrow$  role of  $\Lambda$ N- $\Sigma$ N 3-body interaction
  - Strongly spin dependent

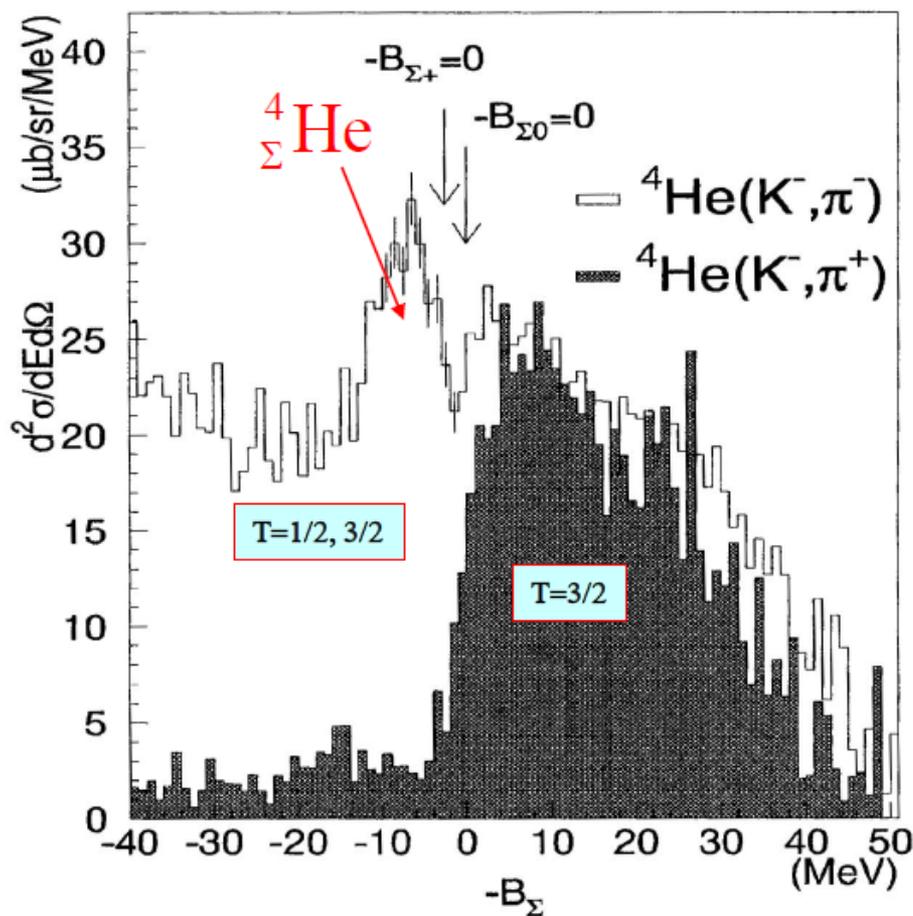
Experimental progresses have opened a new testing ground for a nuclear few-body calculations.

# Observation of a ${}^4_{\Sigma}\text{He}$ Bound State

VOLUME 80, NUMBER 8

PHYSICAL REVIEW LETTERS

BNL-AGS (1995-)



T. Nagaie, T. Miyachi, T. Fukuda, H. Outa,  
T. Tamagawa, J. Nakano, R. S. Hayano,  
H. Tamura, Y. Shimizu, K. Kubota,  
R. E. Chrien, R. Sutter, A. Rusek,  
W. J. Briscoe, R. Sawafuta,  
E. V. Hungerford, A. Empl, W. Naing,  
C. Neerman, K. Johnston, M. Planinic,  
*Phys. Rev. Lett.* **80**(1998)1605.

$$B_{\Sigma^+} = 4.4 \pm 0.3 \text{ MeV}$$

$$\Gamma = 7 \pm 0.7 \text{ MeV}$$

4.6 MeV

7.9 MeV

$$T \approx 1/2$$

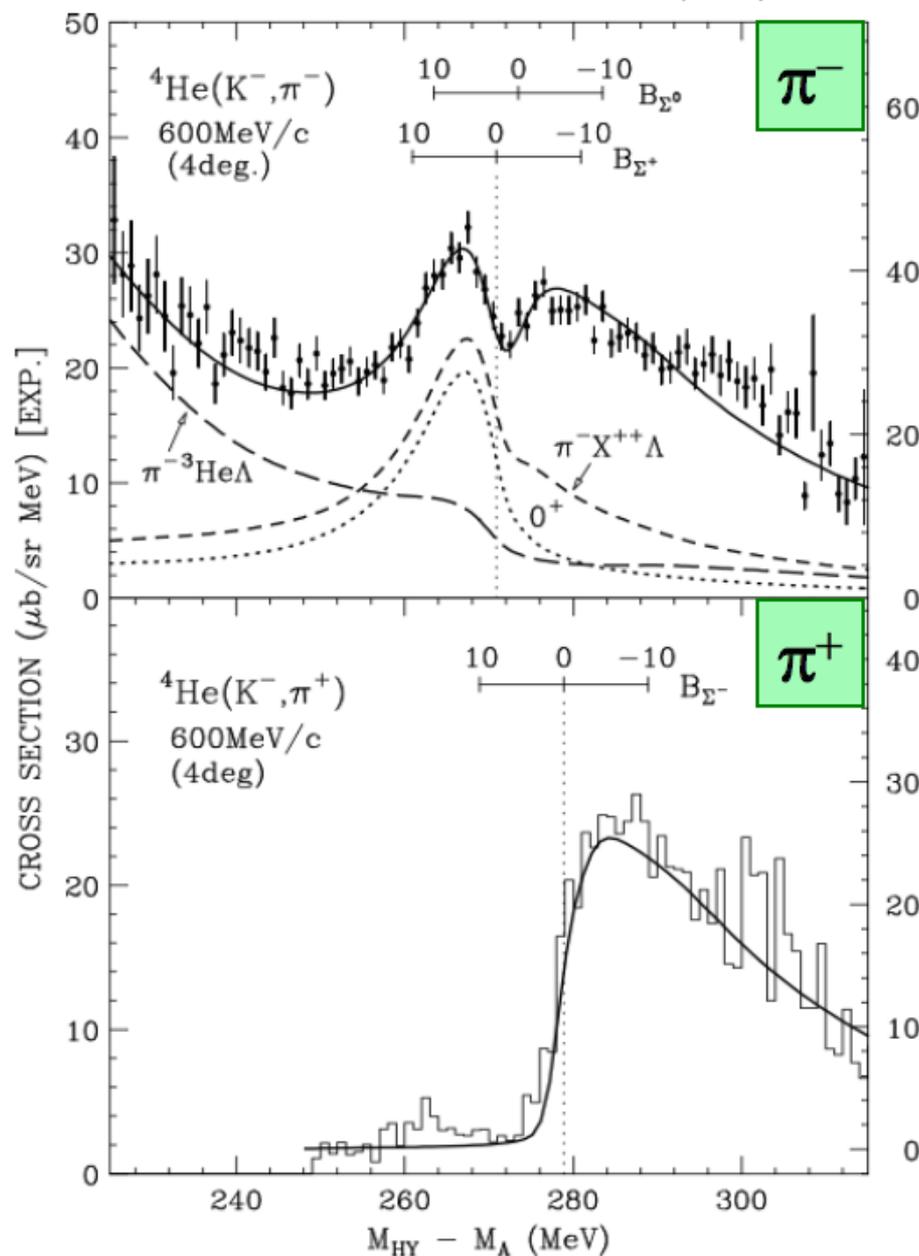
$$J^{\pi} = 0^{+}$$

*Theoretical Prediction*

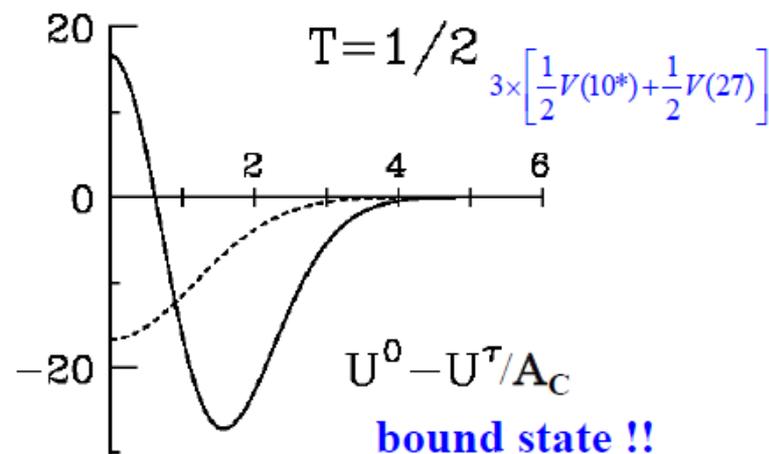
T. Harada, S. Shimura,  
Y. Akaishi, H. Tanaka,  
*NPA* **507**(1990)715.

# Isospin dependence of the (3N)- $\Sigma$ potentials

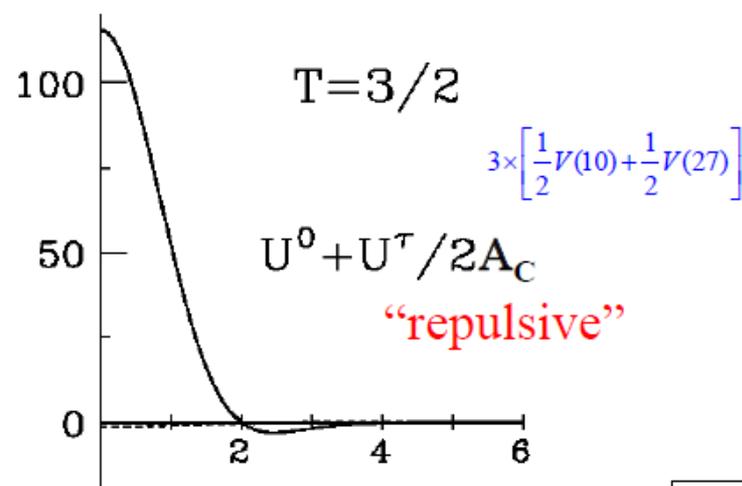
T.Harada, PRL81(1998)5287.



T.Harada, NPA507 (1990) 715.



*“repulsive core  
 + attractive pocket”*



■  $\Lambda N$

$U_0(\Lambda) \sim (-30) \text{ MeV}$ ,  $U_{LS}(\Lambda) \sim 2 \text{ MeV} \rightarrow$  精密測定  
E13@J-PARC  
-38 MeV?

■  $\Sigma N$

$U_0(\Sigma) \sim$  斥力的,  $U_{LS}(\Sigma) ? \rightarrow \Sigma^+ p (= \Sigma^- n)$  散乱 E40@J-PARC

■  $\Lambda N - \Sigma N$

a few % mixing,  $\Lambda NN3$ 体力  $\rightarrow$  中性子過剰ハイパー核  
E10@J-PARC

■  $\Xi N$

$U_0(\Xi) \sim (-14) - (-0) \text{ MeV} ? \rightarrow (K^-, K^+)$  反応,  $\Xi$ -原子X線  
E03,05@J-PARC

■  $\Lambda\Lambda - \Xi N - \Sigma\Sigma$

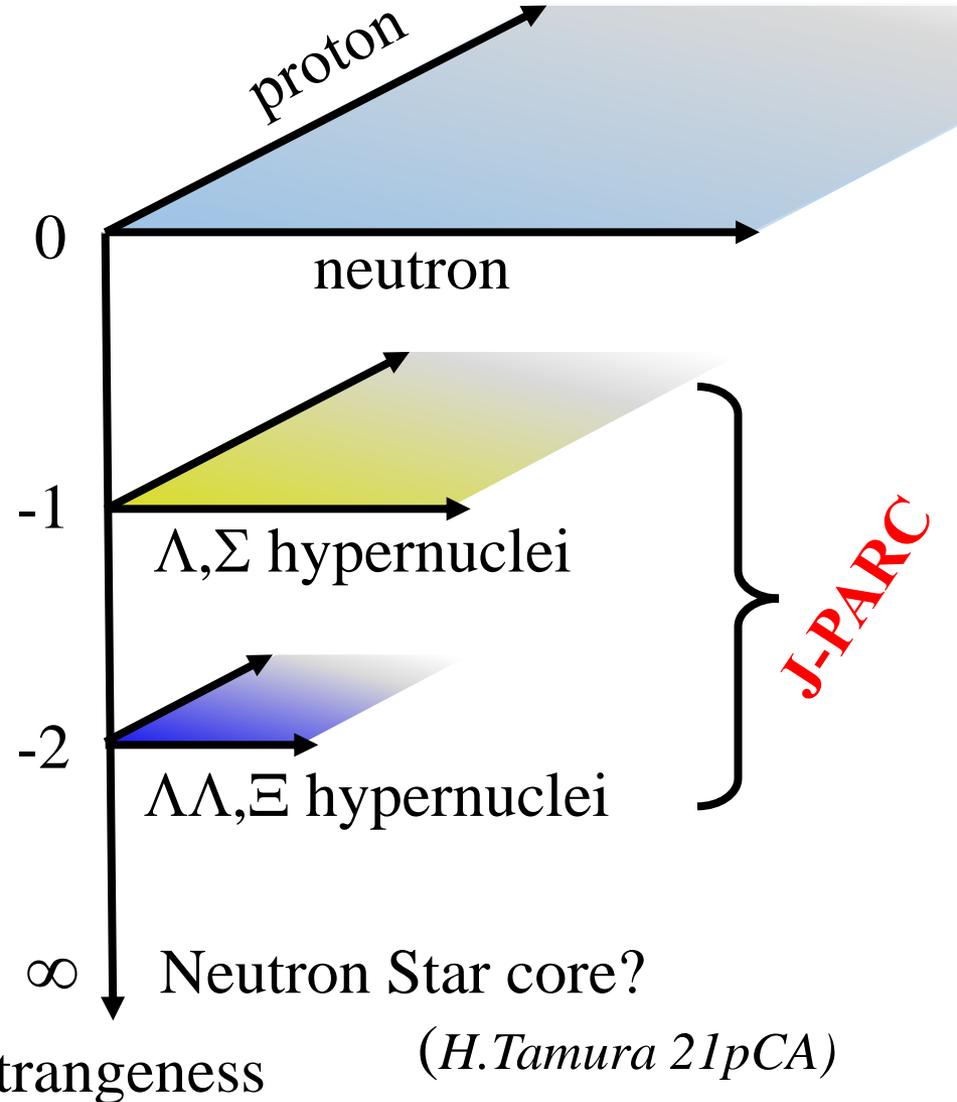
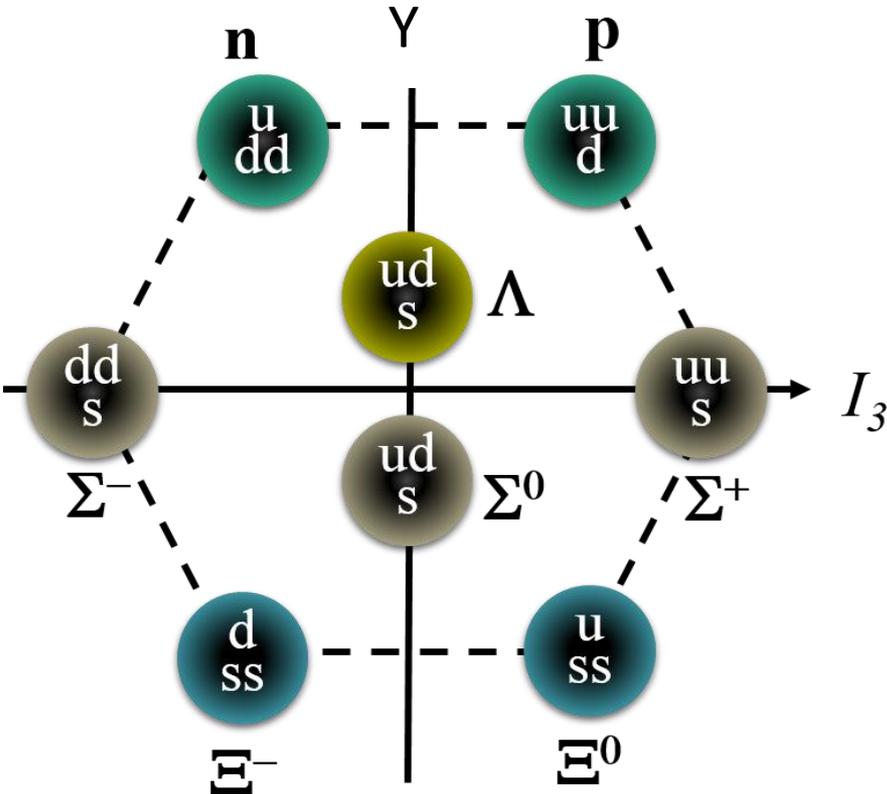
mixing prob. ?, H-particle ?  $\rightarrow$  Hybrid-emulsion,  $\Lambda\Lambda$  相関  
E07, P42@J-PARC

■  $K^- N - \Lambda(1405) - \pi\Sigma$

$U_0(K^-) \sim -200 \text{ MeV} / -50 \text{ MeV} ?$ , “K-pp” ?  
 $\rightarrow (K^-, N), (\pi^+, K^+)$  反応  
E15, E23@J-PARC

# Strange baryon & Hypernucleus

Baryon octet: spin:1/2



# CSB in $\Lambda N$ interaction

$$B_{\Lambda}(^4_{\Lambda}\text{He}; I) = [M_{\text{core}} + M_{\Lambda}] - M(^4_{\Lambda}\text{He}; \text{g.s.}) + E_x(^4_{\Lambda}\text{He}; I)$$

-)

$$B_{\Lambda}(^4_{\Lambda}\text{H}; I) = [M_{\text{core}} + M_{\Lambda}] - M(^4_{\Lambda}\text{H}; \text{g.s.}) + E_x(^4_{\Lambda}\text{H}; I)$$

---

$$\Delta B_{\Lambda}(I) = - \Delta M_{\text{HYP}}^{\text{gs}} + \Delta E_x(I)$$

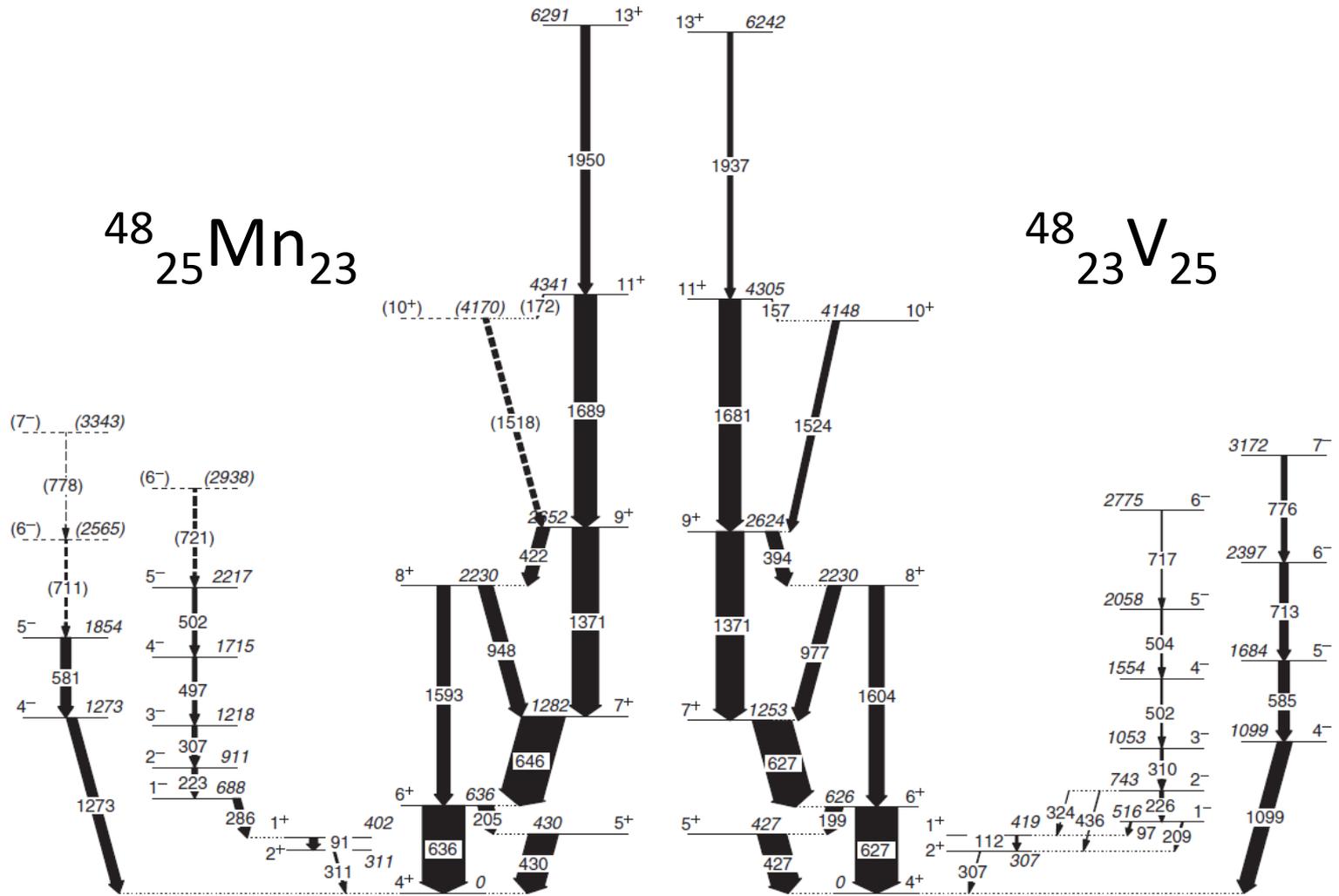
$$\Delta B_{\Lambda}(1^+) - \Delta B_{\Lambda}(0^+; \text{g.s.}) = \Delta E_x(1^+) = \Delta E_{\gamma}(1^+ \rightarrow 0^+)$$

Measure of almost pure CSB in  
 $\Lambda N$  interaction

$[M_{\text{core}} + M_{\Lambda}]$  : reference = 0

**$A=7$ ,  $T=1$  iso-triplet hyp. nuclei**

# Charge symmetry



# Isospin invariance and charge symmetry

- Isospin invariance:  $[H_{st}, T^2] = [H_{st}, T] = 0$ 
  - $a_{nn} = a_{pp} = a_{np}$  (scattering length in  $^1S_0; T=1$ )
- Charge symmetry:  $[H_{st}, P_{cs}] = 0$  where  $P_{cs} = \exp(i\pi T_\alpha)$ 
  - $a_{nn} = a_{pp}$

$$\left. \begin{aligned} a_{pp} &= -17.7 \pm 0.4 \text{ fm} \\ a_{nn} &= -18.8 \pm 0.3 \text{ fm} \\ a_{np} &= -23.75 \pm 0.09 \text{ fm} \end{aligned} \right\}$$

$$\frac{\sigma(pp \rightarrow d\pi^+)}{\sigma(pn \rightarrow d\pi^0)} \neq (\approx) \frac{1}{2}$$

Mostly dominated by EM (Coulomb &  $\pi$  mass difference) effects