



Clustering effects in reactions with light even-even $N=Z$ nuclei. From the Hoyle state to cluster emission in ^{24}Mg .

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NUCL-EX Collaboration

¹ University and INFN, Bologna, Italy

FUSTIPEN Topical Meeting

Dynamical cluster formation and correlations in heavy-ion collisions, within transport models and in experiments

May 17-19, 2016, GANIL, Caen, France

Outline

❑ Scientific Motivation:

- ✓ Fusion-evaporation reaction.
- ✓ Monte Carlo Hauser-Feshbach Code.
- ✓ Clustering.
- ✓ Hoyle state.

❑ The experimental set-up @ LNL-INFN

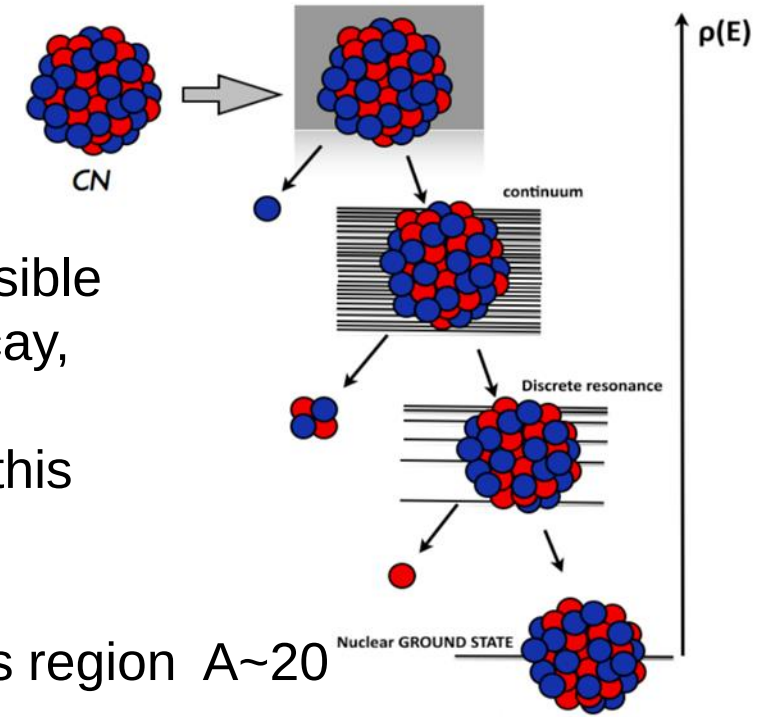
❑ The $^{12}\text{C}+^{12}\text{C}$ and $^{14}\text{N}+^{10}\text{B}$ experiments:

- Fusion Evaporation Analysis.
- Hoyle state in central and peripheral collision.

❑ Conclusions and perspectives

Fusion-Evaporation Reactions

- The statistical theory of compound nucleus decay
- Above the thresholds for particle decay, level densities are only accessible in evaporation reactions through the theory of compound nucleus decay,
- mainly inclusive experiments have been used up to now to constrain this fundamental quantity
- few studies exist concerning the evaporation of light nuclei in the mass region $A \sim 20$



EXP: highly exclusive detection

NUCL-EX collaboration campaign:

STATistical properties of LIGHT nuclei from Fus-Evap.

- ❖ low multiplicity evts. & high detection coverage
- ❖ high energy and angular resolution
- ❖ complete evt. Reconstruction
- ❖ global control on the decay mechanism

GARFIELD+RCO @ LNL

TH: decay codes constrained to available data

- ❖ Compound Nucleus formation and decay
- ❖ Level Density for $A \sim 20$, $e^* \sim 3 A$. MeV

AMD calculations for $^{12}\text{C}+^{12}\text{C}$

Monte Carlo Hauser-Feshbach

G. Baiocco PhD thesis <http://amsdottorato.cib.unibo.it/4295/>

G. Baiocco et al 2013 Phys. Rev. C **87** 054614.

Monte Carlo Hauser-Feshbach HFl

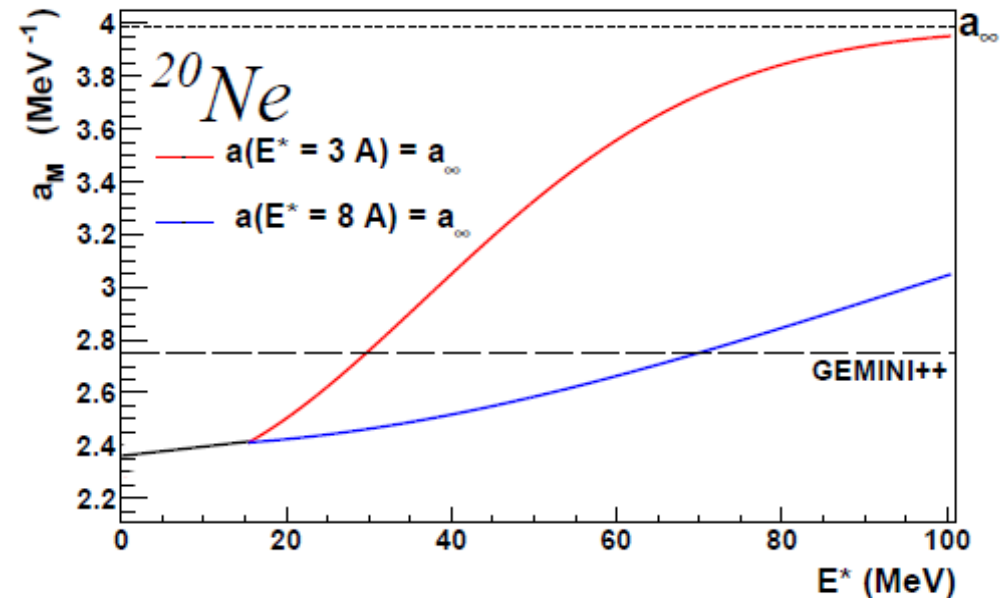
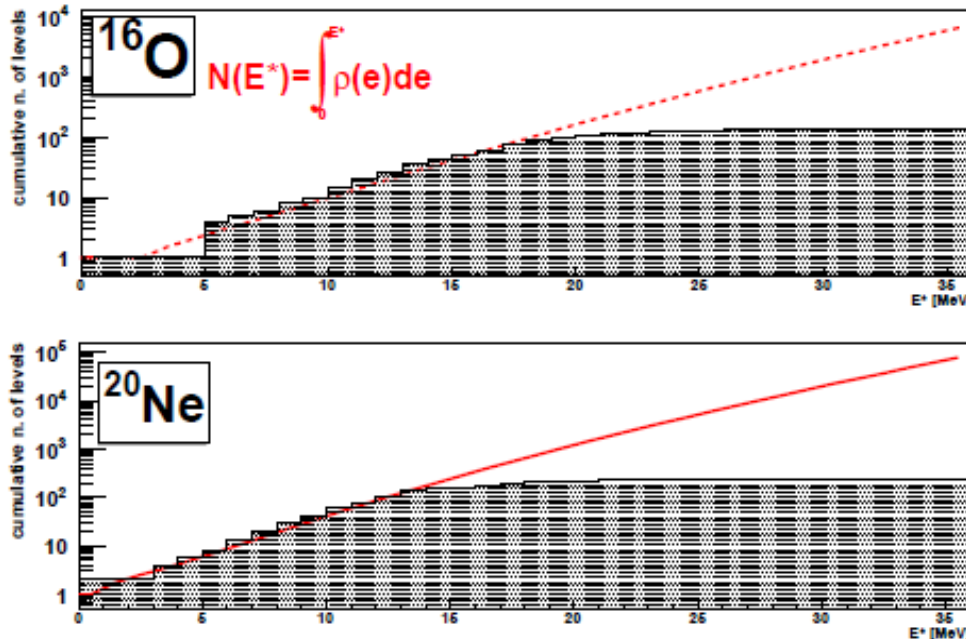
Systematics of LD parameters

D.Bucurescu, PRC 72, 044311 (2005)

Back-Shifted Fermi Gas with $a(E)$
fitted nuclei between ^{18}F and ^{251}Cf ;

$$a_{\infty} = \frac{A}{14.6} \left(1 + \frac{3.114}{A^{1/3}} + \frac{5.626}{A^{2/3}} \right)$$

J.Toke, Nucl. Phys. A 372 141 (1981)



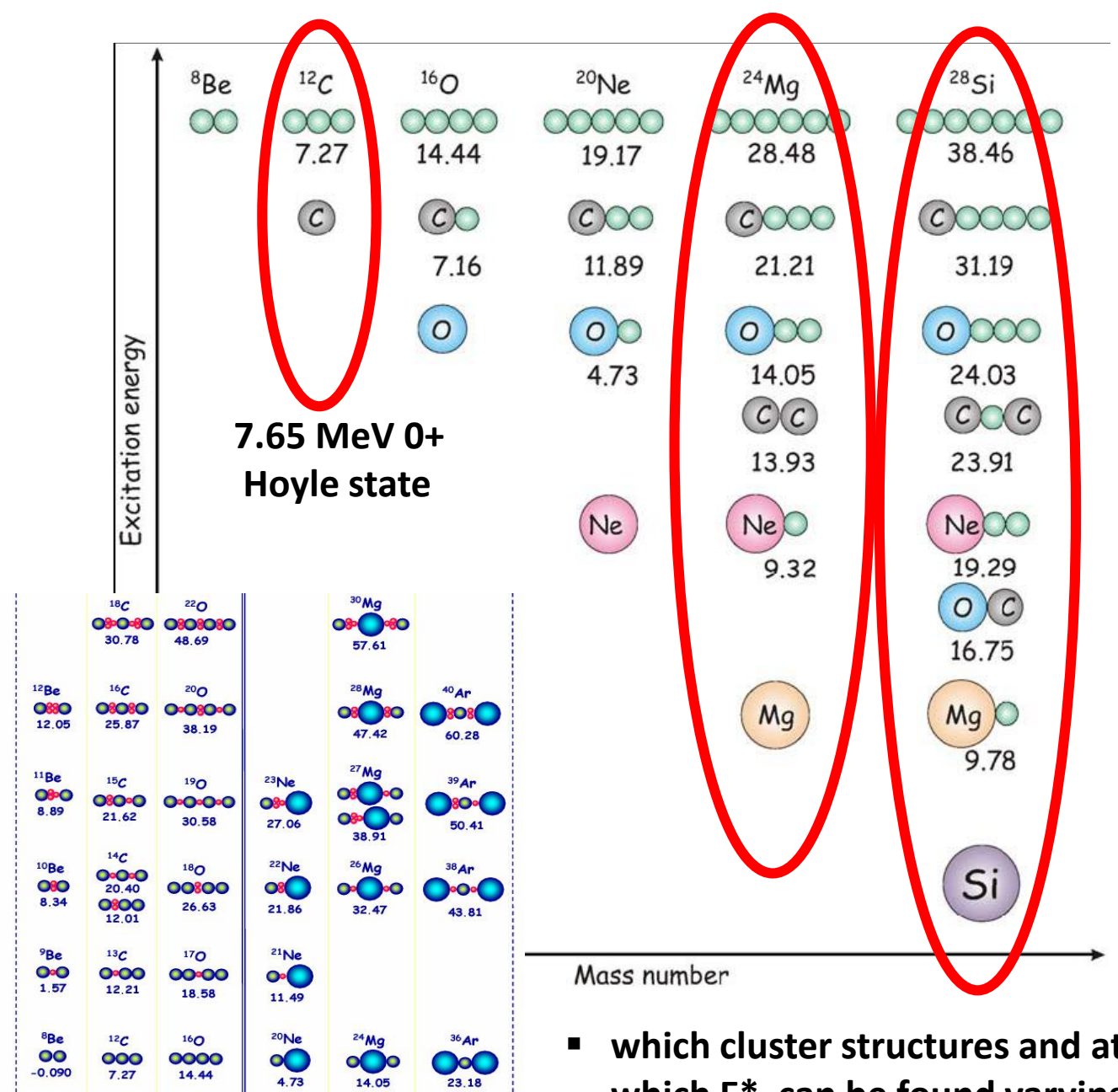
a_{∞}

- rapidity of the increase as the only model free parameter
- GEMINI++ as a reference:
<http://www.chemistry.wustl.edu/~rc/gemini++/>
- R. J. Charity, Phys. Rev. C 82 014610 (2010)

G. Baiocco PhD thesis <http://amsdottorato.cib.unibo.it/4295/>
G. Baiocco et al 2013 Phys. Rev. C 87 054614.

Clustering

- Cluster structures appear mainly at excitation energies close to the thresholds for nucleus decomposition into clusters;
- Evidence for cluster structures comes from decay widths and branching ratios
- Preferential decay to α -structures in daughter nuclei
- Molecular resonances at higher excitation energy.

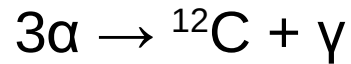


- which cluster structures and at which E^* can be found varying the N/Z in a given isotopic chain?

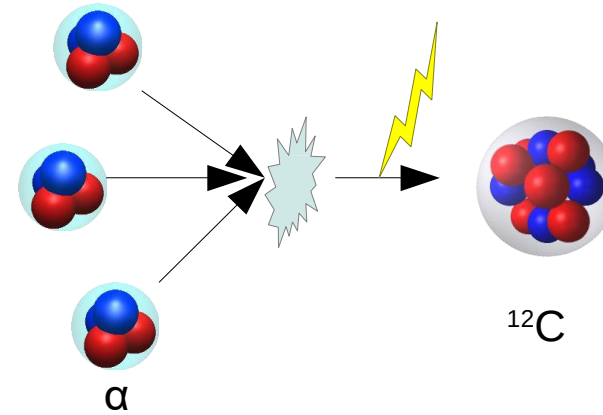
Hoyle state

The theory of stellar evolution:

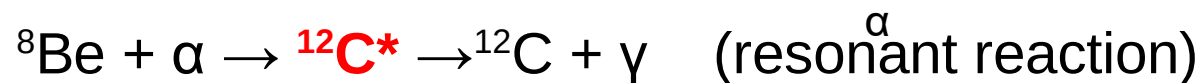
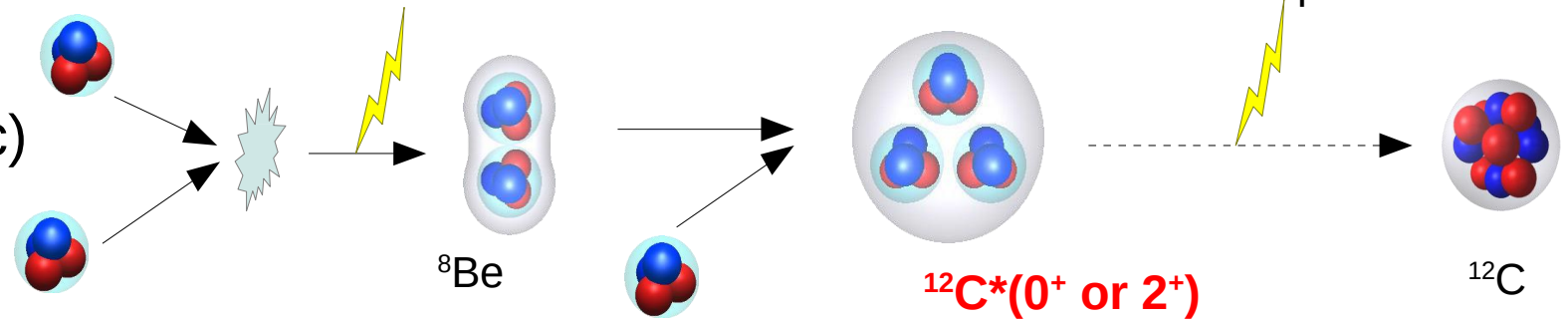
Triple- α reaction (Bethe, Phys. Rev. 55(1939)434)



Two-step process (E. Salpeter, Astrophys. J. 115(1952)326)
(non-resonant)



In 1953, Fred Hoyle predicted the third α could be captured through the **resonance level in ${}^{12}\text{C}$** . (F. Hoyle, Astrophys. J. Suppl. 1(1954)121)



The 7.65 MeV 0^+ state in ${}^{12}\text{C}$ was found in β -decay of ${}^{12}\text{B}$

C.W. Cook, W.A. Fowler, C.C. Lauritsen, and T. Lauritsen, Phys. Rev. 107(1957)508

Hoyle state and α cluster model

^{12}C , 7.65 MeV 0_2^+ = Hoyle state

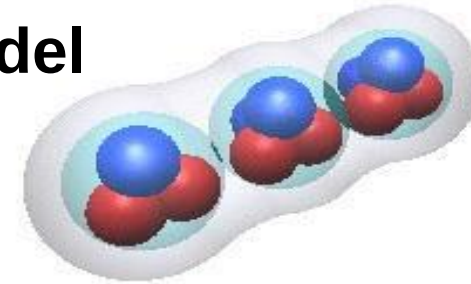


Difficult to explain the structure by the shell model

3α cluster structure (α cluster model)

Linear chain structure

(Morinaga, Phys.Rev.101(1956)254)

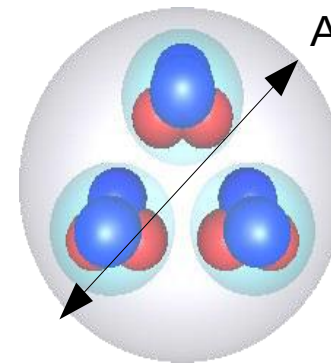


Loosely coupled 3α clusters (gas-like)

(3α OCM: Horiuchi, PTP51(1975)1266)

(3α GCM: Uegaki *et al*, PTP57(1977)1262)

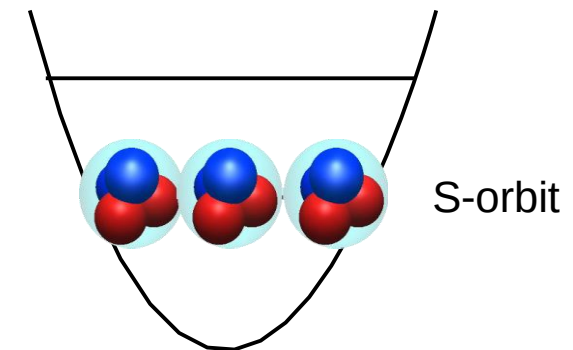
(3α RGM: Kamimura, NPA351(1981)456)



About twice
of the 0_1^+

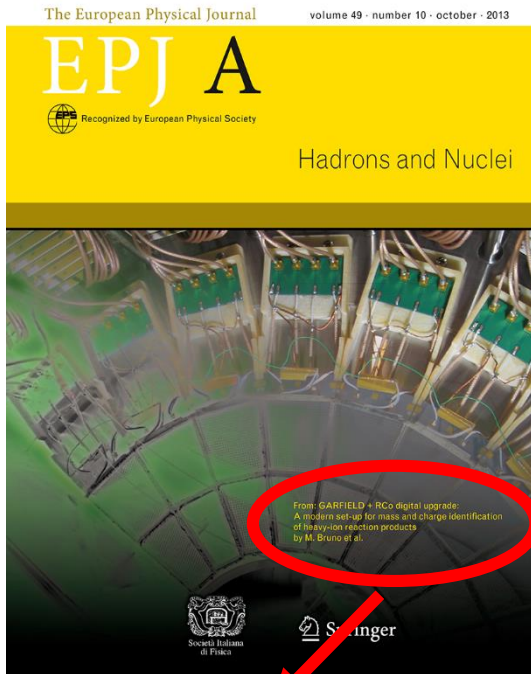
3α -clusters condensate in the lowest S-orbit

(Tohsaki *et al*, PRL87(2001)192501)



Experimental set-up @ LNL-INFN

European Physical Journal A



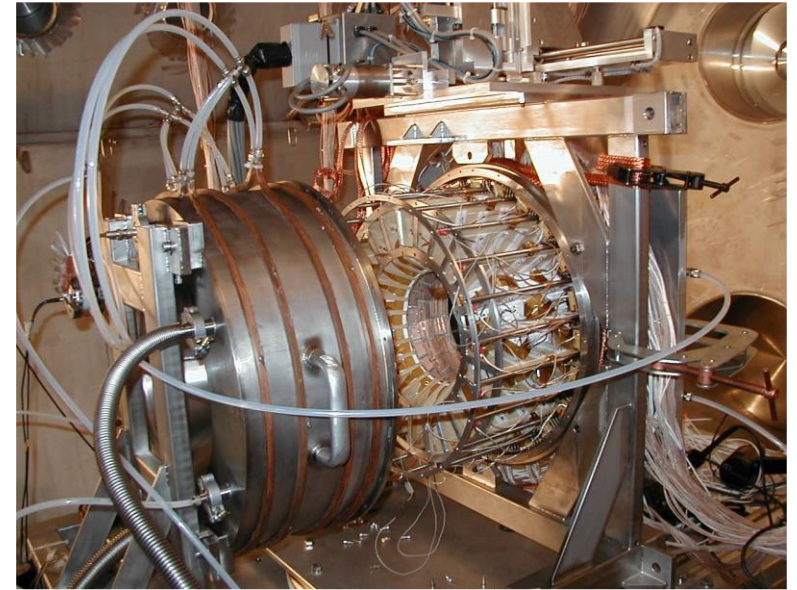
GARFIELD + RCo digital upgrade.....

By M. Bruno et al.

Eur. Phys. J. A (2013) 49: 128

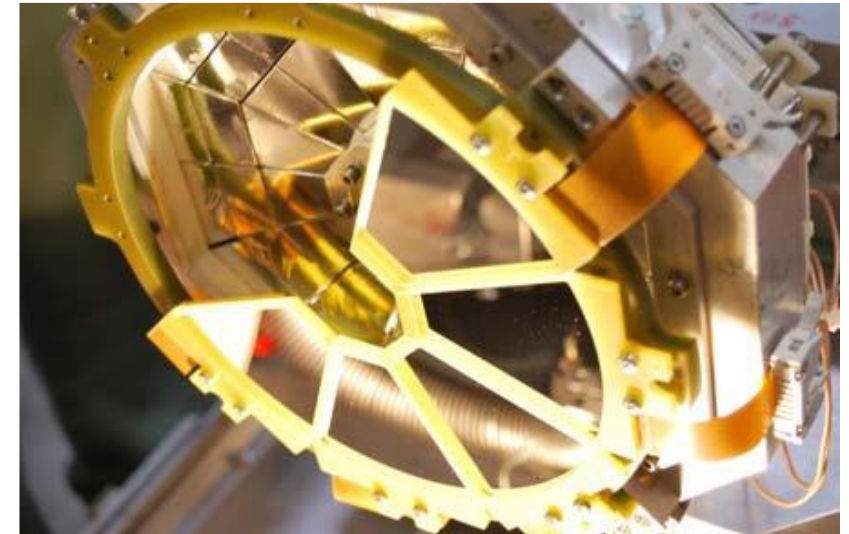
μ SGC + CsI(Tl), 180 CsI
detection of LCP and fragments:

- ✓ low identification thresholds (0.8–1 MeV/u)
- ✓ angular coverage $30^\circ < \theta_{\text{lab}} < 150^\circ$
24 azimuthal sector
- ✓ Z identification, A identification for $1 \leq Z \leq 3$



IC+Si+CsI(Tl), 64 telescopes

- ✓ detection of ER, low E thresholds
- ✓ high granularity and θ -resolution: 0.8° for $5^\circ < \theta_{\text{lab}} < 17^\circ$
- ✓ energy resolution of Si strips and CsI(Tl) given by 0.3% and 2-3%



Experimental set-up at LNL-INFN

^{12}C (95 MeV) + ^{12}C
 ^{14}N (80 MeV) + ^{10}B } ^{24}Mg at 2.6 A.MeV

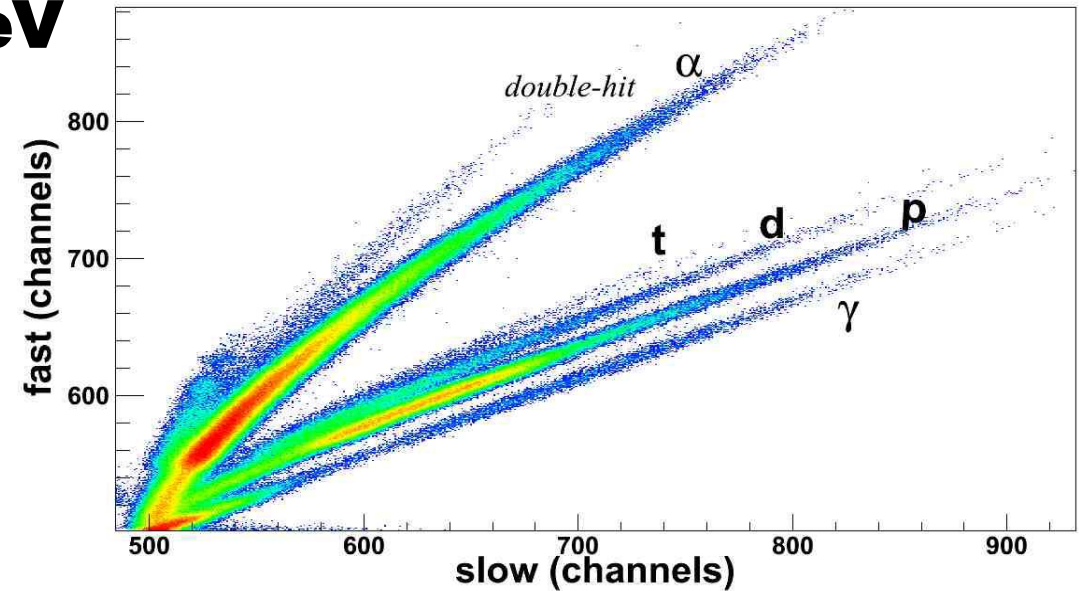
LCP isotopical identification + energy calib. in CsI

L. Morelli et al.

Nucl. Instr. and Meth. A 620 305 (2010)

energy spectra of evaporated particles

GARFIELD CsI Fast Slow

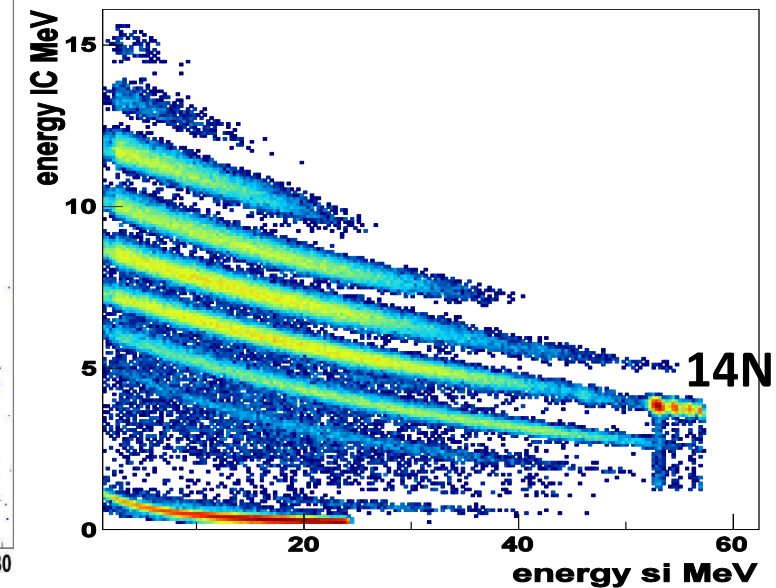
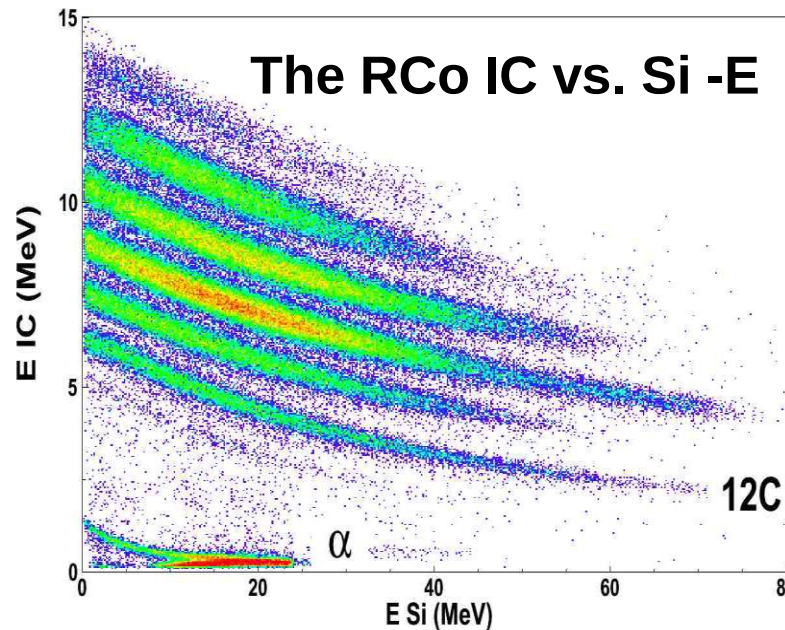


ΔE -E Z identification

N. Le Neindre, et al.,

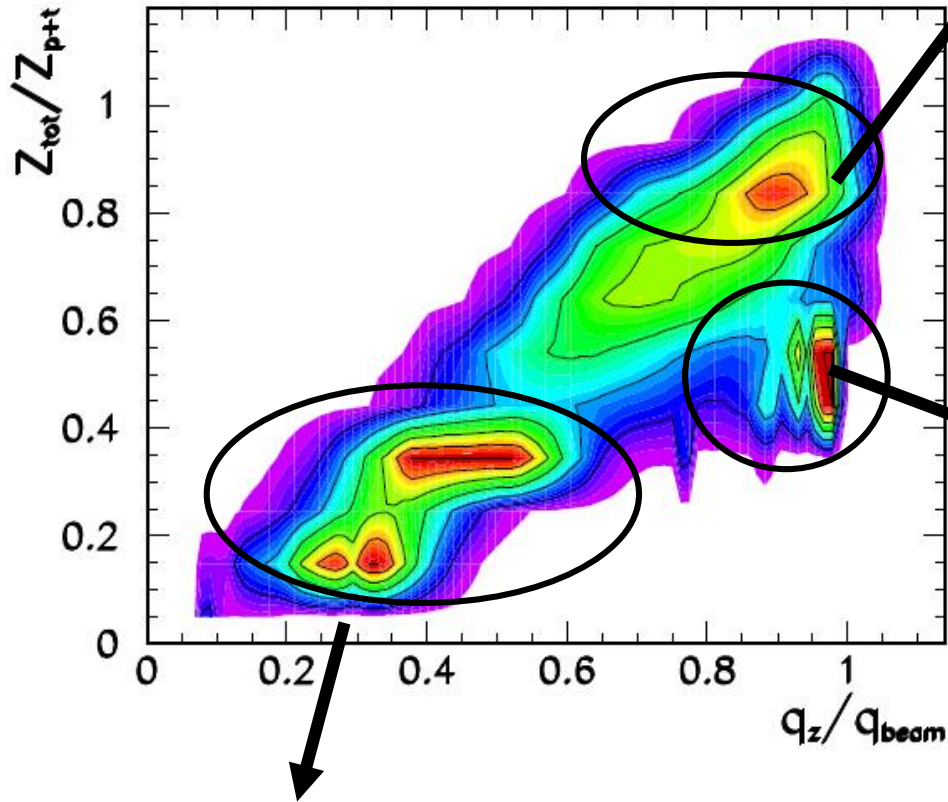
Nucl. Instr. and Meth. A 490 251 (2002).

gate on evaporation residue



Event selection

Total events



- Incomplete events
- No ER detection
- Only LCP in GARFIELD

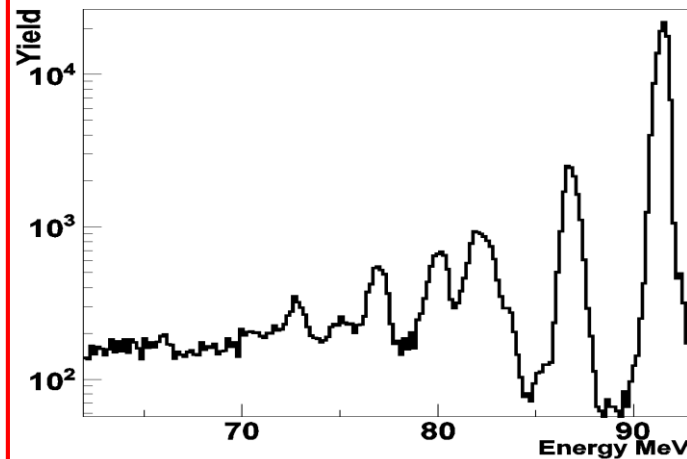
Fusion-Evaporation channel selection:

- completeness of the detection $Z_{\text{det}} 100\%$ ($Z_{\text{proj}+\text{targ}}$)
- Longitudinal momentum $q_z/q_{\text{beam}} > 0.8$
- coincidence between LCP in GARFIELD and Evaporation Residue in RCo

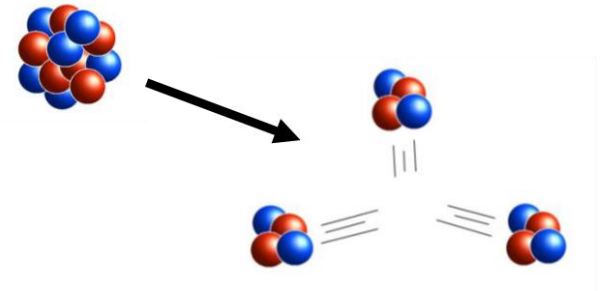
G. Baiocco 2013 *Phys. Rev. C* **87** 054614.

PROJECTILE

- ^{12}C excited state

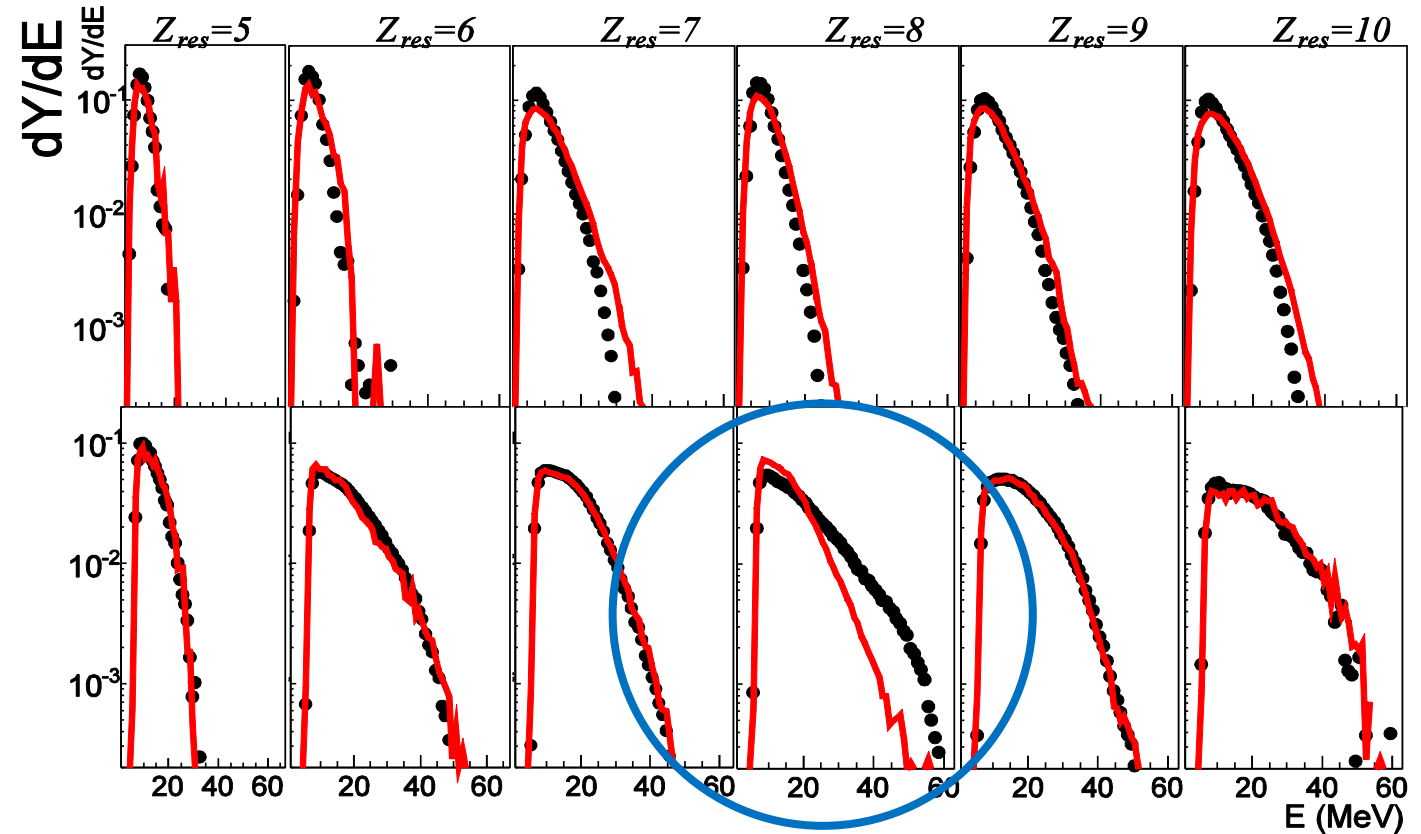
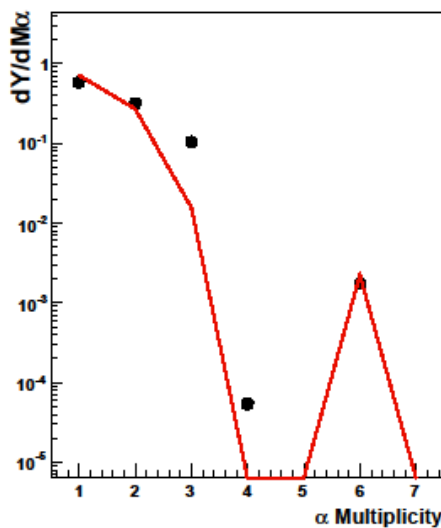
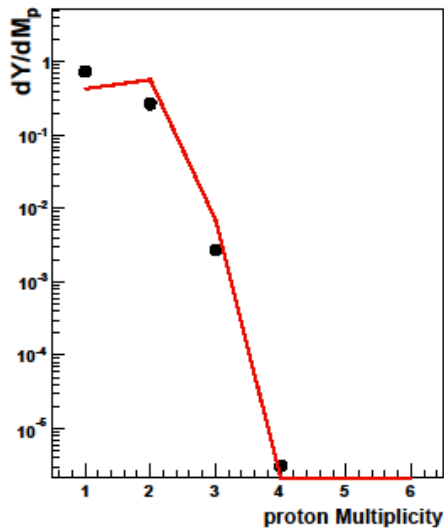
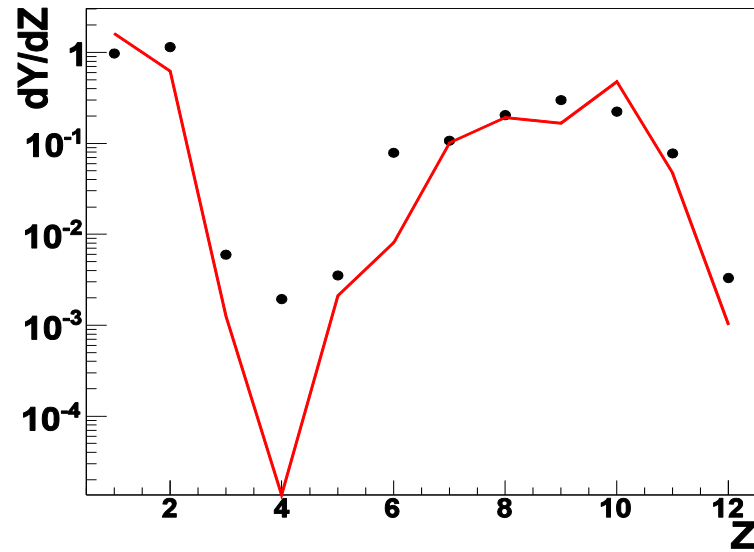


- $^{12}\text{C}^*$ decay in 3 α particles



Fusion Evaporation Analysis: $^{12}\text{C} + ^{12}\text{C}$ *exp* (@95 MeV)

- data — HFI calculation



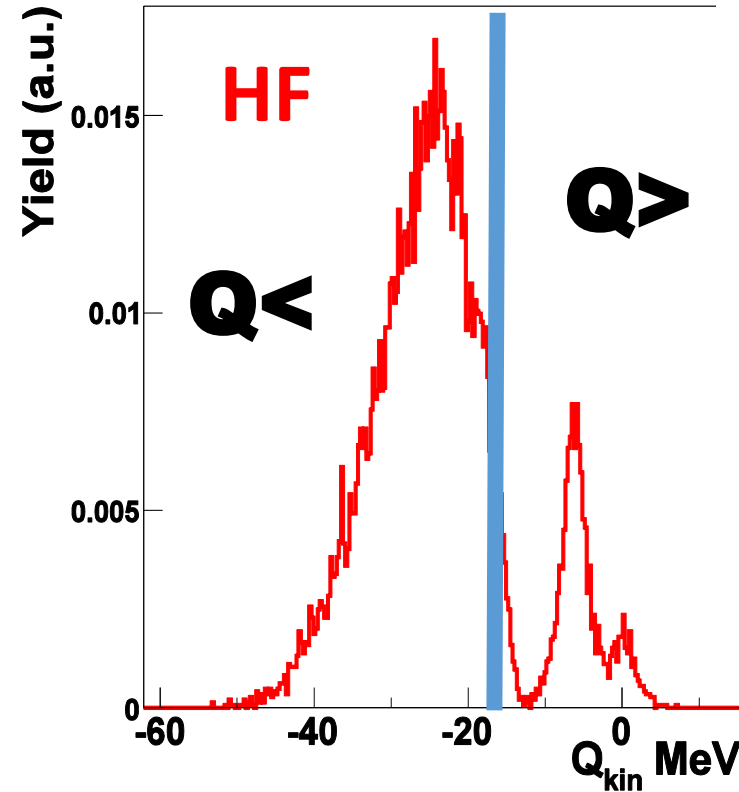
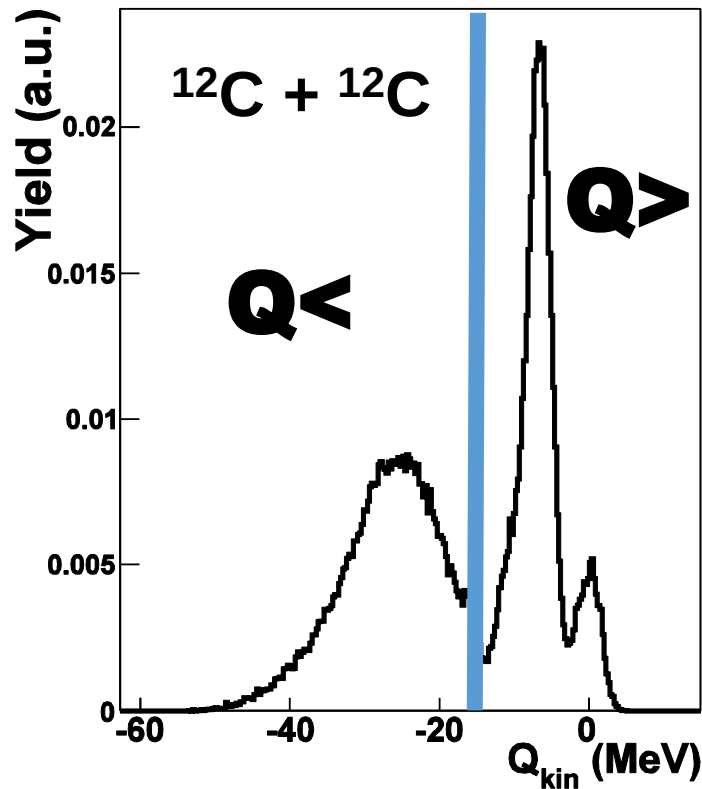
HFI calculation for ^{24}Mg ($E = 62$ MeV) decay

- good reproduction of global variables ($Y(Z)$, multiplicities...)
- energy spectra and angular distributions of protons and alpha particles in coincidence with a residue
- **biggest discrepancy for α 's in coincidence with $Z=8$ fragments**

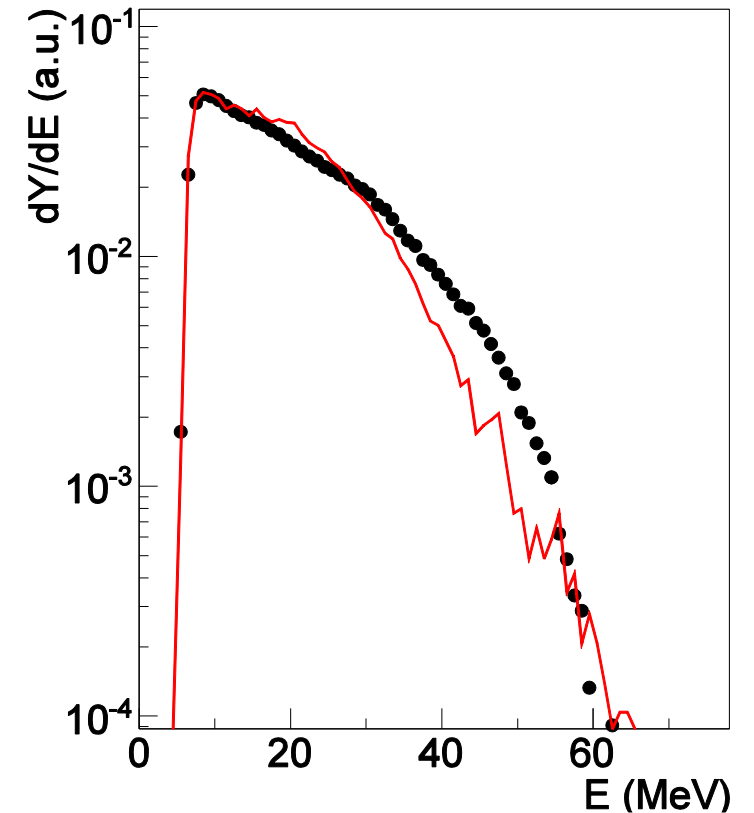
Fusion Evaporation Analysis: $^{12}\text{C} + ^{12}\text{C}$ *exp* (@95 MeV)

$$Q_{kin} = E_{kin} - E_{beam} = \sum_{i=1}^N E_i - E_{beam}$$

Oxygen + 2 α + neutron(s) channel



α Zres=8 (O+2 α +xn)

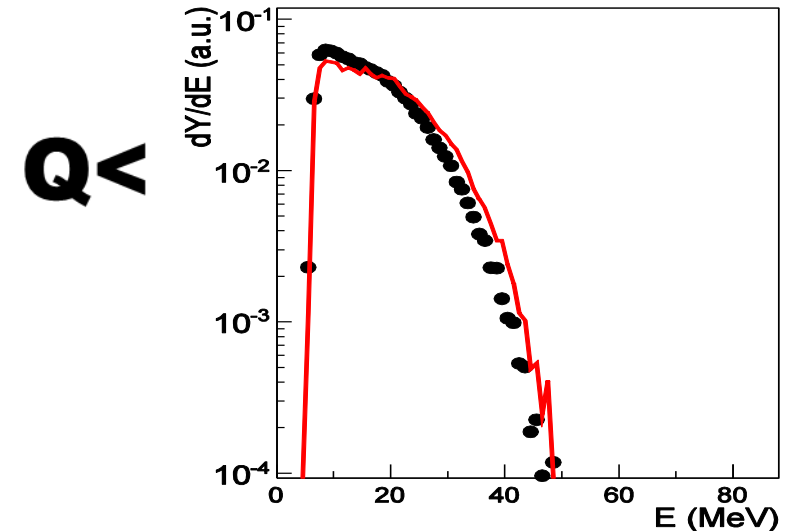
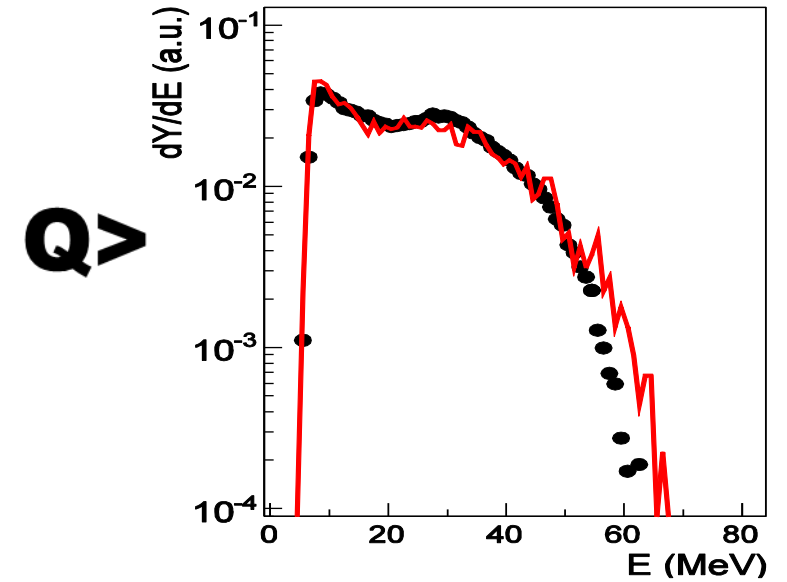
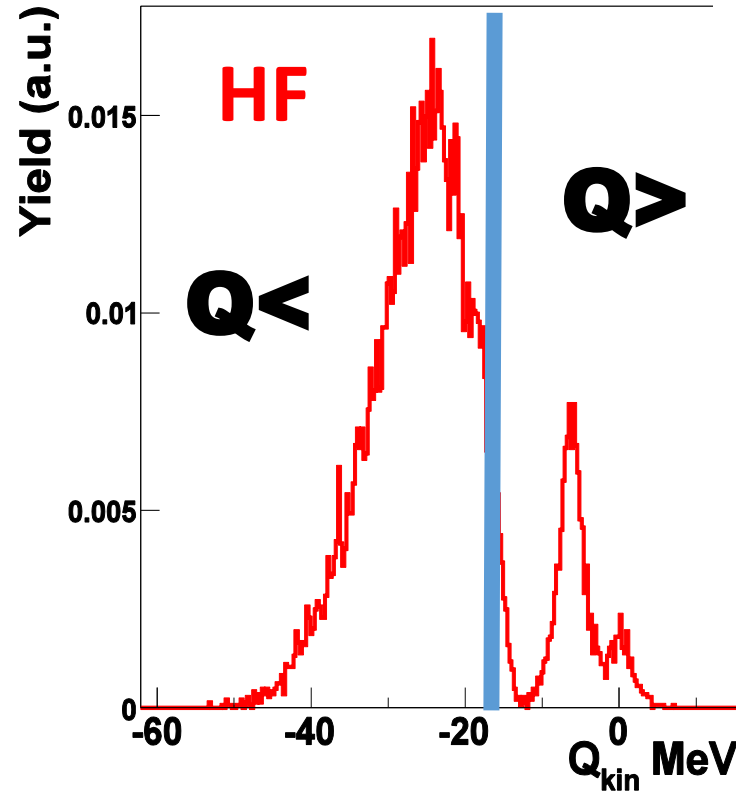
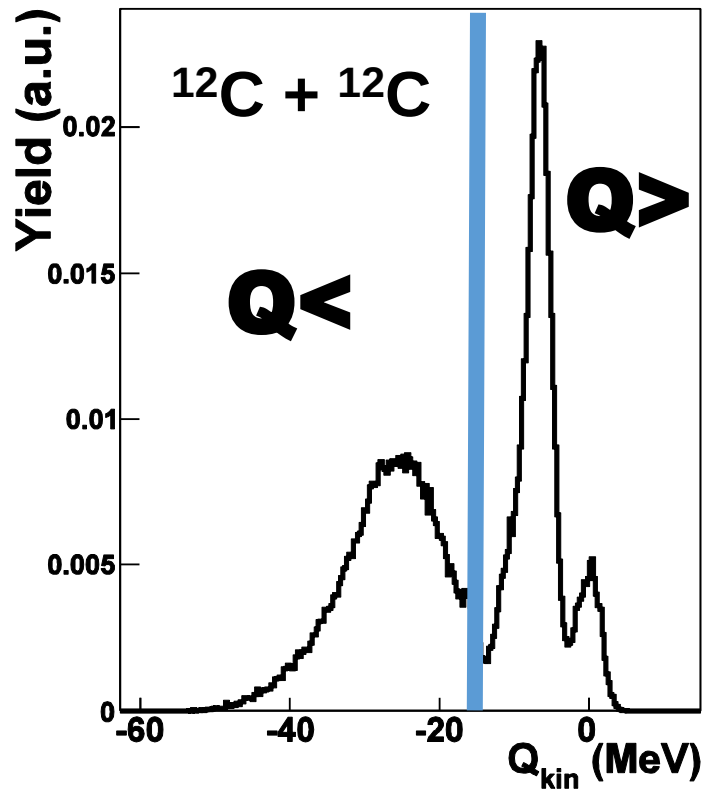


- common pattern for theoretical and experimental Q_{kin}
- Differences in the relative population of the different regions.

Fusion Evaporation Analysis: $^{12}\text{C} + ^{12}\text{C}$ *exp* (@95 MeV)

$$Q_{kin} = E_{kin} - E_{beam} = \sum_{i=1}^N E_i - E_{beam}$$

Oxygen + 2 α + neutron(s) channel



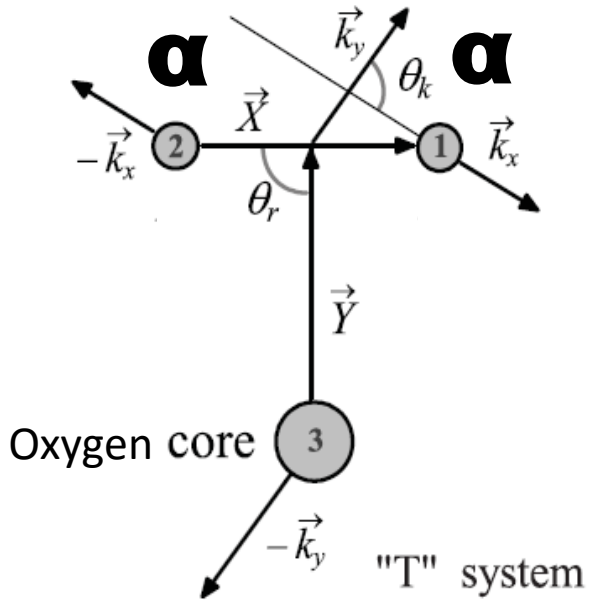
- common pattern for theoretical and experimental Q_{kin}
- Differences in the relative population of the different regions.

Oxygen – α – α correlations

Jacobi coordinates (T system)

$$E_x = \frac{(m_1 + m_2)k_x^2}{2m_1m_2} \rightarrow E_{\alpha-\alpha}$$

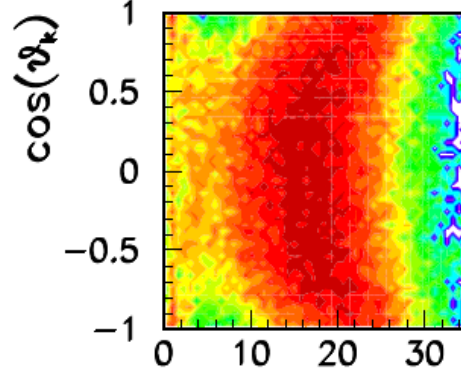
$$\cos \theta_k = \frac{\vec{k}_x \cdot \vec{k}_y}{k_x k_y} \rightarrow \frac{(K_O \cdot K_{\alpha-\alpha})}{(K_O K_{\alpha-\alpha})}$$



R. J. Charity Phys. Rev. C 84 (2011)

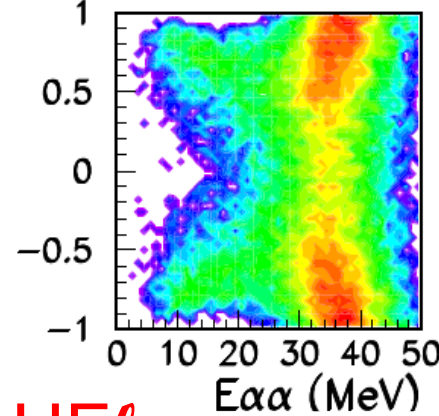
Q<

O+2alpha+xn



Q>

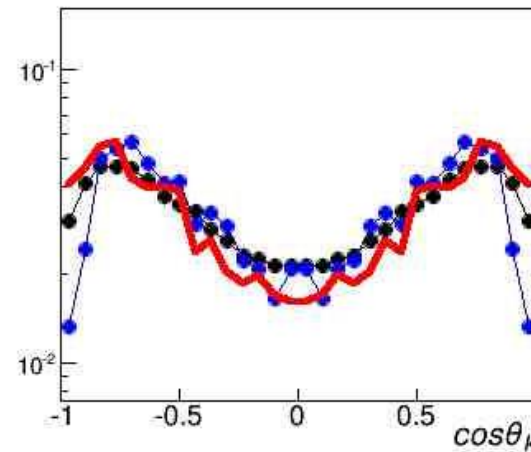
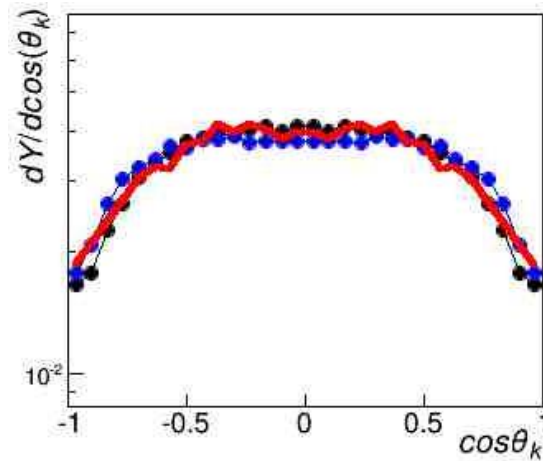
¹⁶O+2alpha



¹²C + ¹²C

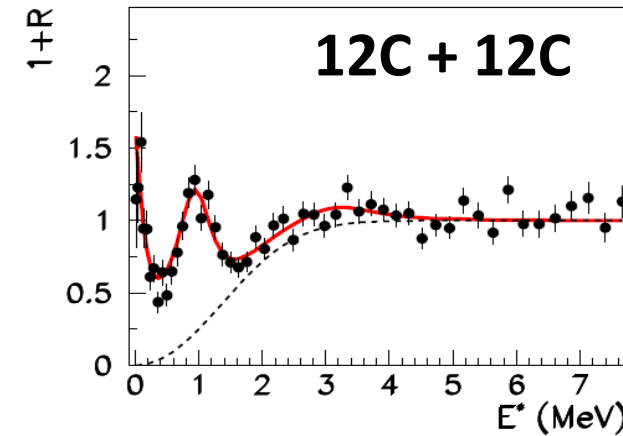
¹⁴N + ¹⁰B

Hfℓ



Jacobi angular correlations are compatible with sequential decay from an evaporation source.

Correlation function of the relative α – α energy in the α-α-O channel



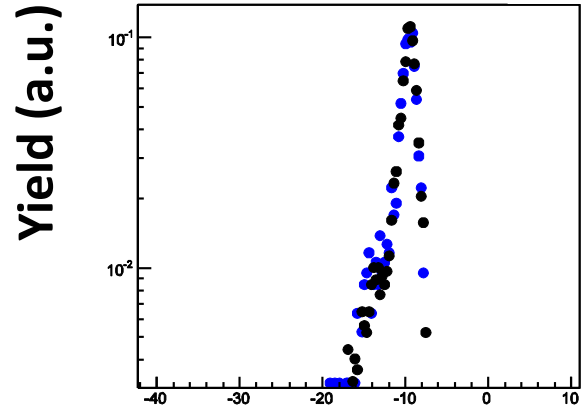
the formation of discrete Be levels does not represent more than 3% of the experimental yield in the ^AO–2α channel

Fusion Evaporation Analysis: $^{12}\text{C} + ^{12}\text{C}$ & $^{14}\text{N} + ^{10}\text{B}$

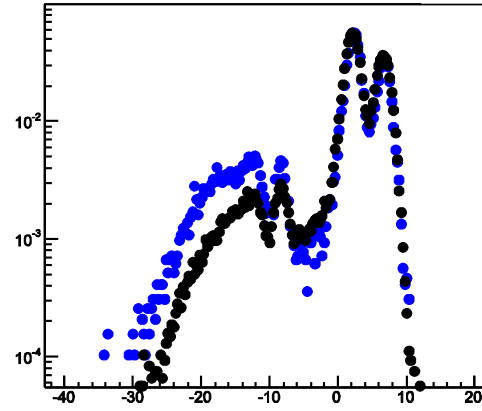
$$Q_{kin} = E_{kin} - E_{beam} = \sum_{i=1}^N E_i - E_{beam}$$

- Channels with maximum α multiplicity for each residue

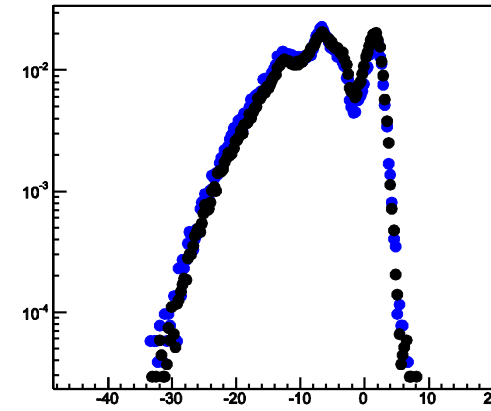
B + 3 α + p



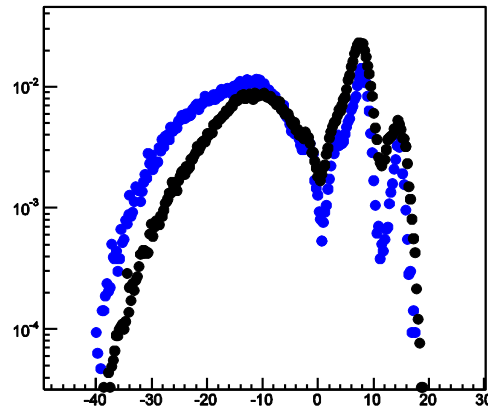
C + 3 α + xn



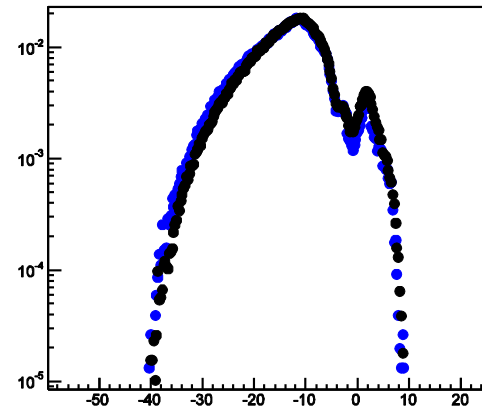
N + 2 α + p + xn



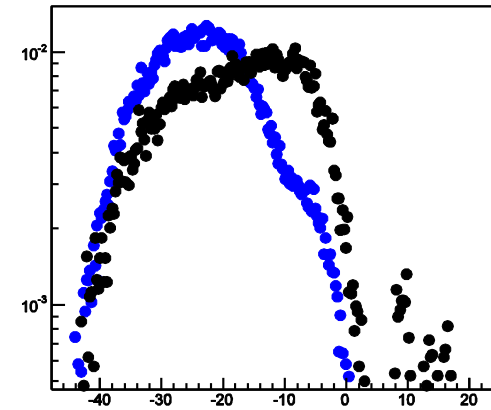
O + 2 α + xn



F + α + p + xn



Ne + α + xn



- Common pattern for the Q_{kin} -value
- Difference in the relative $Q > / <$ population
- Entrance channel effects confirmed

Q_{kin} MeV

Fusion Evaporation Analysis: $^{12}\text{C} + ^{12}\text{C}$ && $^{14}\text{N} + ^{10}\text{B}$

N+B reaction

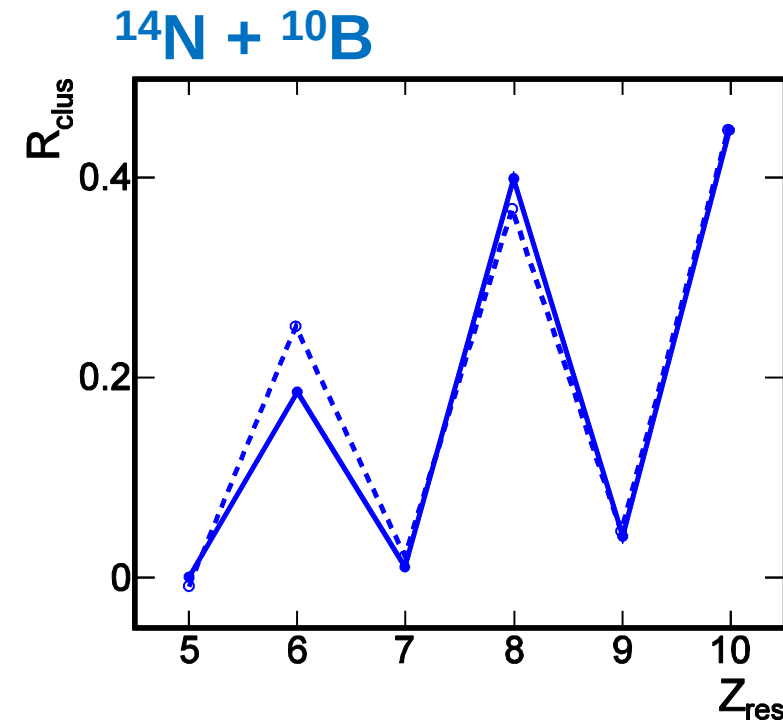
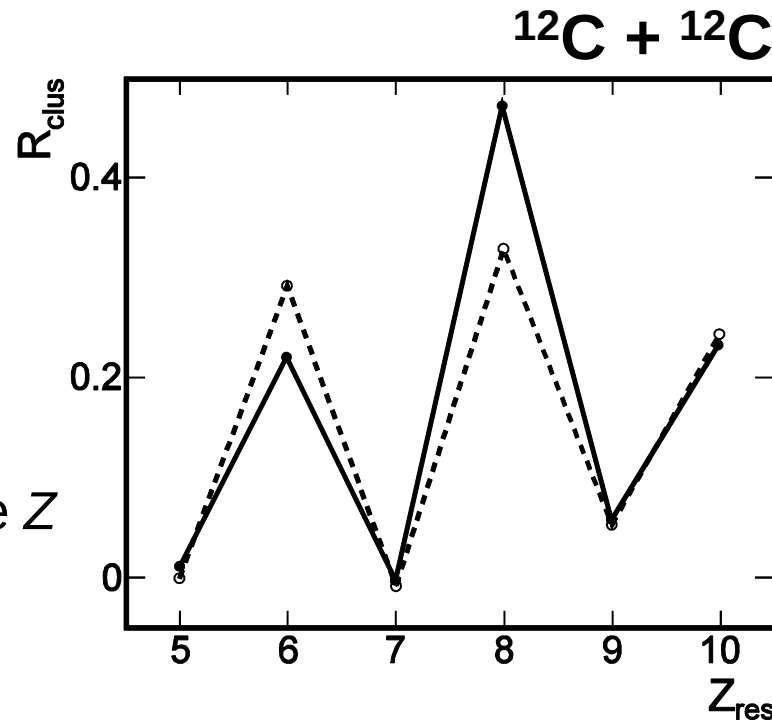
C+C reaction

Z_{res}	channel	BR_e (N+B)	BR_t (N+B)	BR_e (C+C)	BR_t (C+C)
6	C+3 α + xn	96%	77%	98%	78%
8	O+2 α + xn	56%	15%	63%	15%
10	Ne+ α + xn	47%	3%	26%	3%

experimental branching ratio
excess towards α emission

$$R_{\text{clus}}(Z) = \frac{Y_{\text{exp}}(Z; n_Z \alpha)}{Y_{\text{exp}}(Z)} - \frac{Y_{\text{HFl}}(Z; n_Z \alpha)}{Y_{\text{HFl}}(Z)}$$

- $Y(Z; n_Z \alpha)$ coincidence yields
- $Y(Z)$ inclusive yields
- $n_Z \rightarrow$ maximum α multiplicity associated to the residue of charge Z



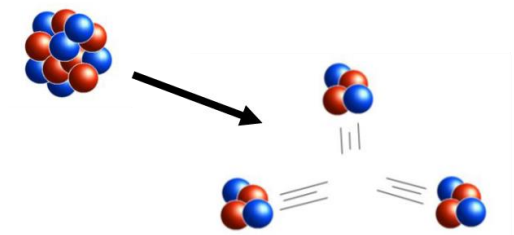
- ✓ channels with Carbon, Oxygen and Neon residues show a preferential α decay.
- ✓ residual α structure correlations in the excited ^{24}Mg or in its daughter nucleus.

Hoyle State

$^{12}\text{C}^* \rightarrow \text{Hoyle State}$

First proposed by Fred Hoyle in 1953 to explain the abundance of carbon in the universe.

- Later found experimentally at the energy which Hoyle had predicted.
- Cannot be explained by the shell model.
- Formed through the 'triple- α ' process and thought to have a clustered structure.

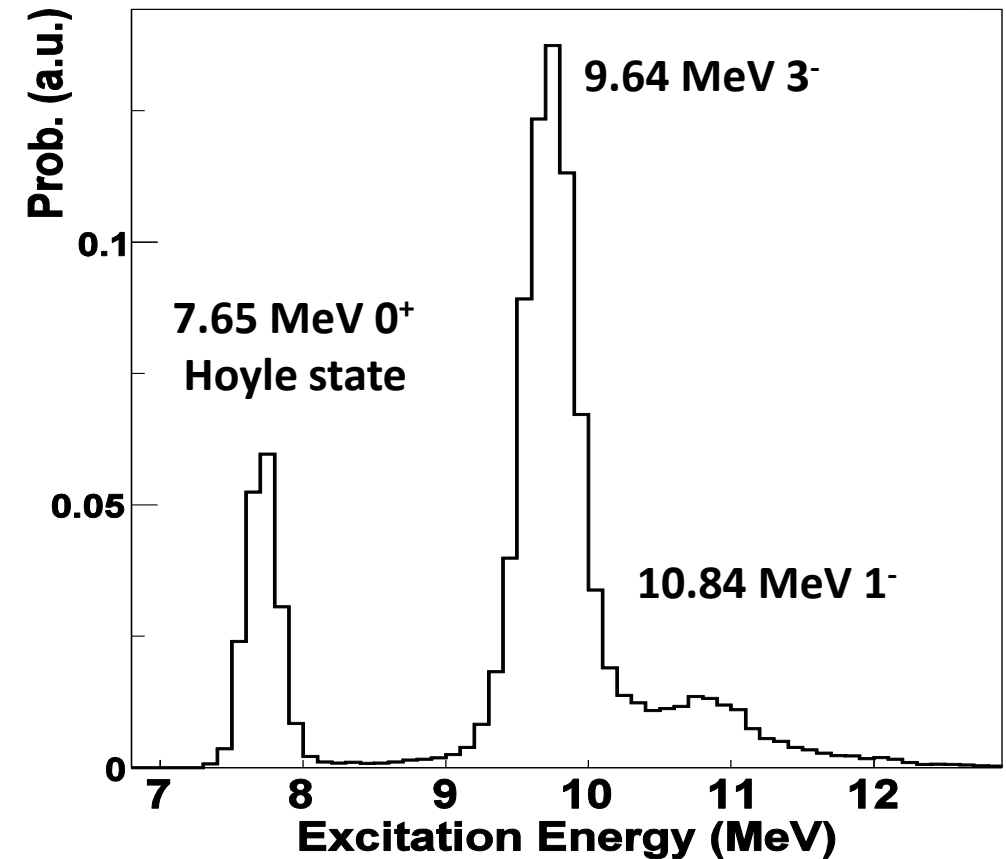
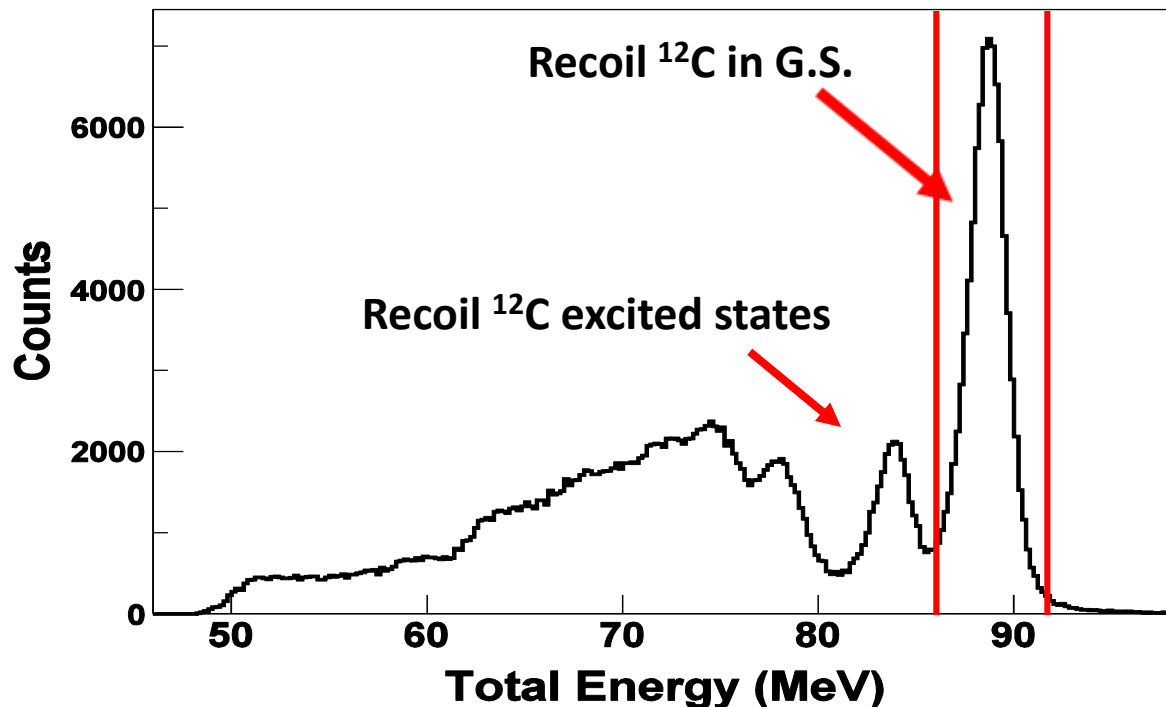


^{12}C Excitation Energy Spectrum

$$E_{^{12}\text{C}}^* = \sum_{i=1}^3 E_{\alpha_i} - \frac{P^2}{2MC} + Eth$$

Total Energy Spectrum

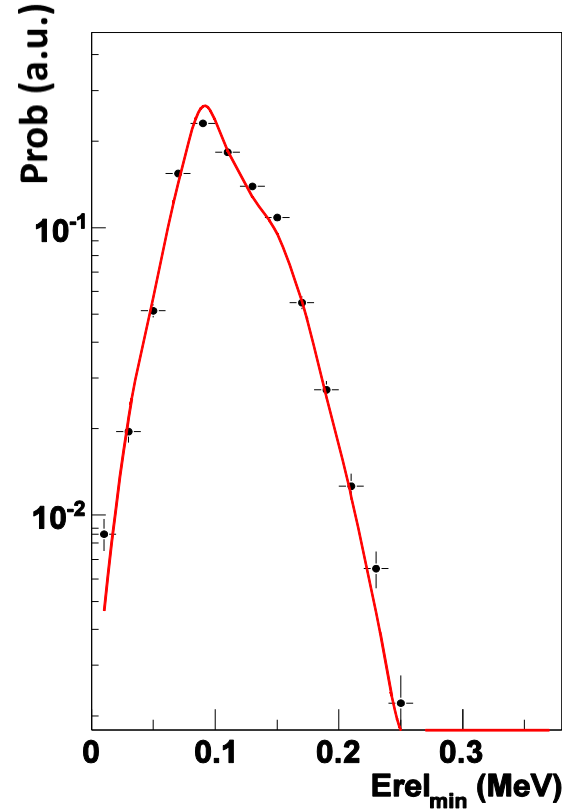
$$E_{tot} = \sum_{i=1}^3 E_{\alpha_i} + E_{rec} = E_{beam} + Q \quad (Q = -7.272 \text{ MeV})$$



Hoyle State -> decay mechanism

Relative energy distribution of 8Be-like pairs

Sequential -> 92KeV Direct-> ≈188KeV

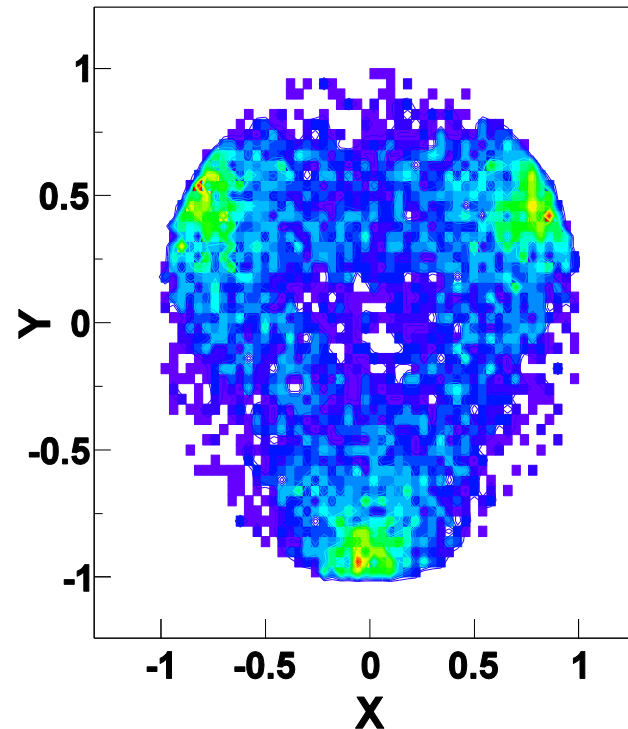


• data
-- HFI

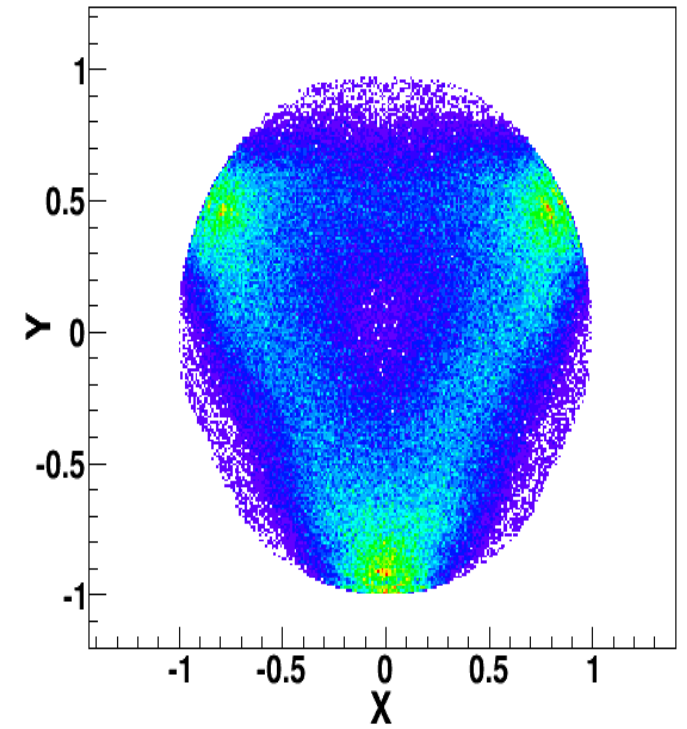
Energy DALITZ Plot

$$X = \frac{\sqrt{3}(E_i - E_j)}{E_{tot}}$$

$$Y = \frac{2E_k - E_i - E_j}{E_{tot}}$$



DATA



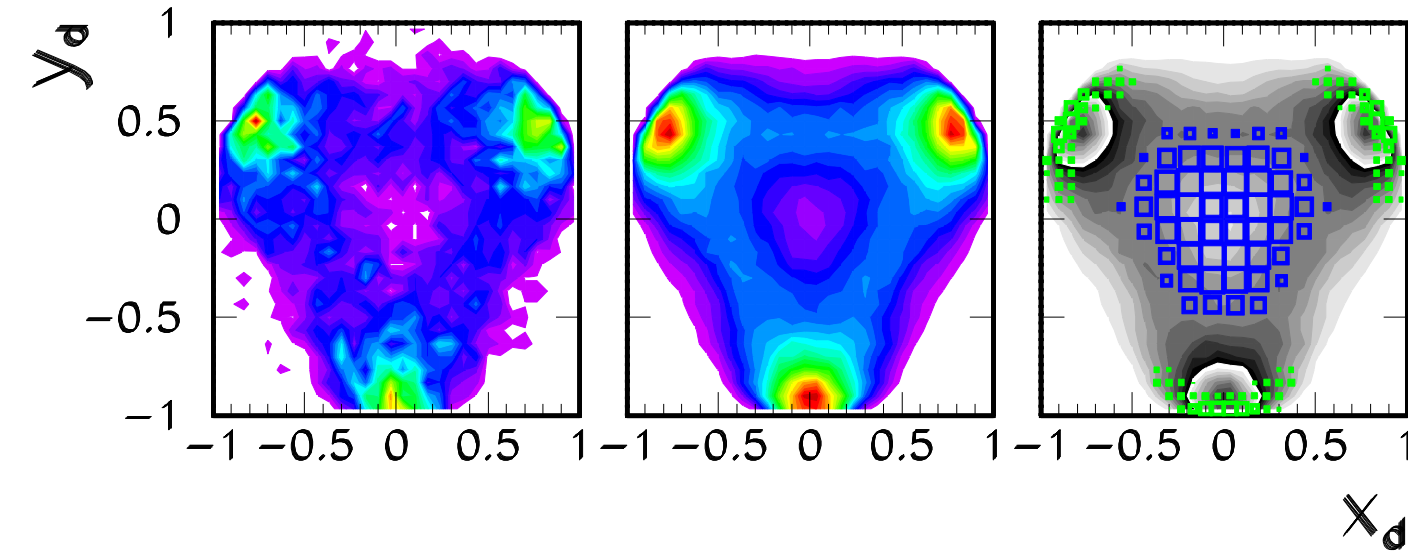
HFI (sequential)

Raduta PLB 705, 65 (2011) (α -particle condensation)

O.S.Kirsebom PRL 108 (2012) (sequential)

J.Manfredi PRC 85 (2012) (sequential)

Hoyle State -> decay mechanism



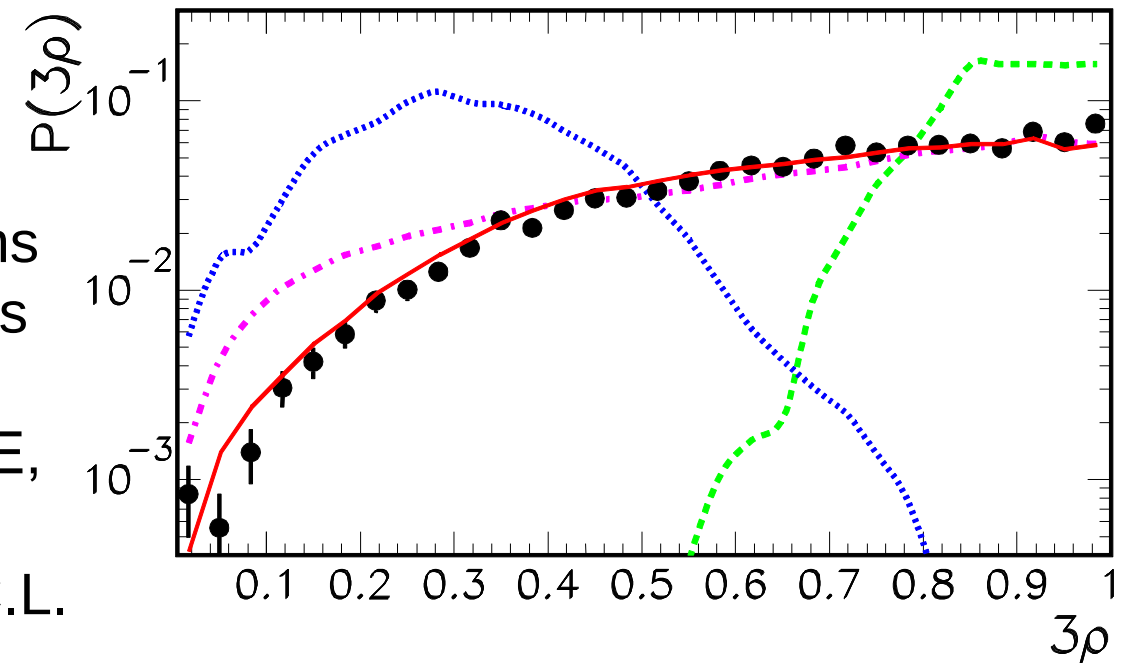
Possible direct decay (DD)

- DDE direct decay with equal energies.
- DDL direct decay in linear chain.
- DD ϕ direct decay with uniform population of the phase space

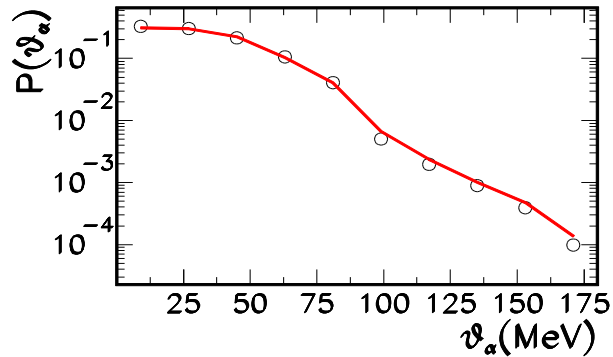
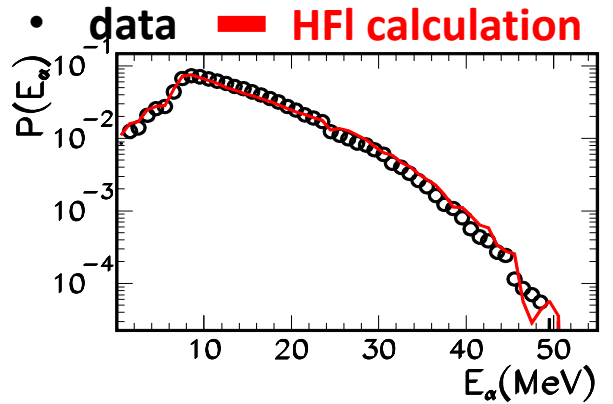
radial projection of the Dalitz plot

$$(3\rho)^2 = x_d^2 + y_d^2$$

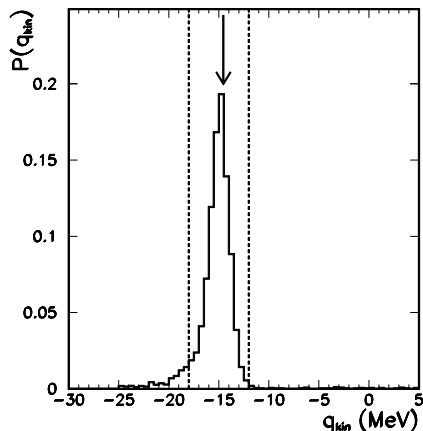
- data are very well reproduced by HF ℓ calculations
- DDE, DDL and DD ϕ give bumps at the extremes of the distribution.
- Fit performed on the 3ρ variable, when HF ℓ , DDE, DDL and DD ϕ are included.
- Total DD contribution $1.1 \pm 0.4\%$ with a 95% of C.L.



$^{12}\text{C} + ^{12}\text{C} \rightarrow ^{24}\text{Mg} \rightarrow 6 \alpha$ decay channel: the Hoyle state properties



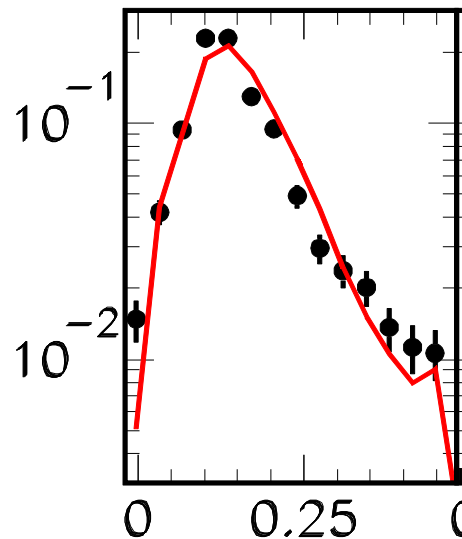
Q_{kin} distribution



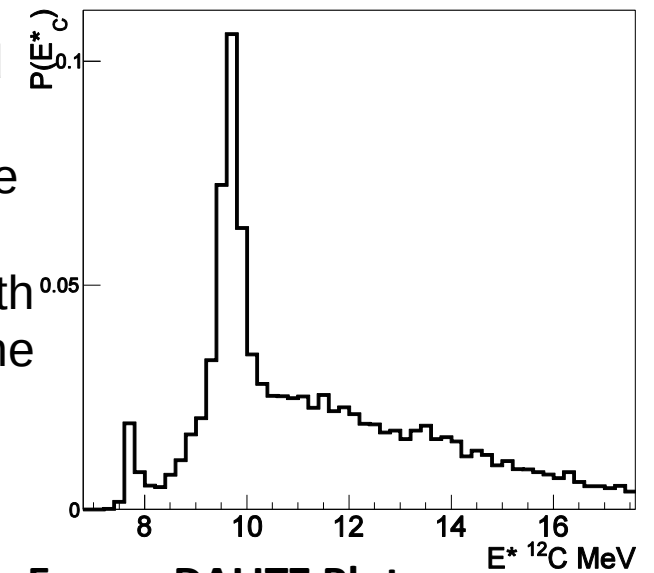
- 6 α particles detected by the apparatus.
- sequential evaporation of the $^{24}\text{Mg}^*$ formed in central collisions the decay has to go through the formation of a $^{12}\text{C}^*$ intermediate nucleus .
- selected the three (over six) α particles with the minimum total energy and calculate the $^{12}\text{C}^*$ excitation energy.

Relative energy of 8Be

Sequential $\rightarrow 92\text{KeV}$ Direct $\rightarrow \approx 188\text{KeV}$

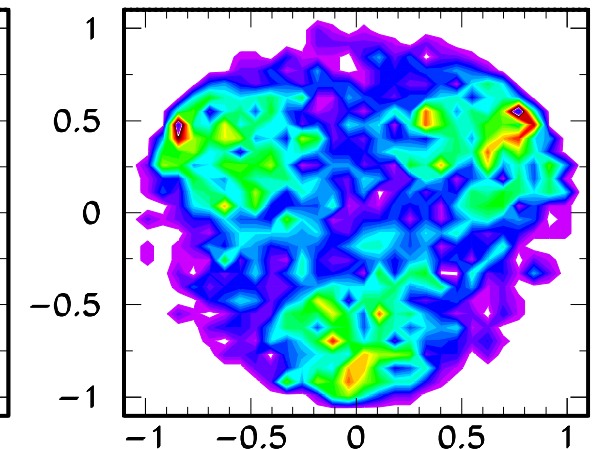
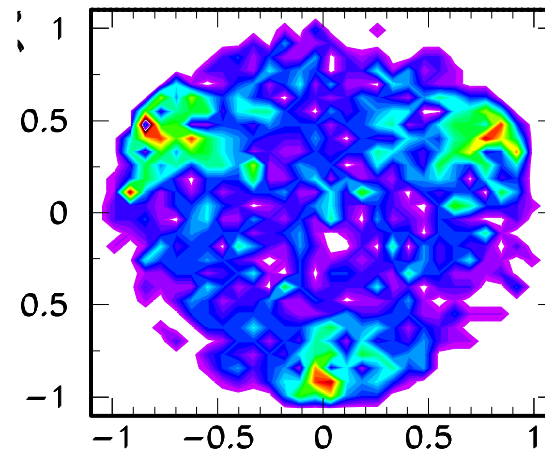


^{12}C Excitation Energy Spectrum



Energy DALITZ Plot

$$X = \frac{\sqrt{3}(E_i - E_j)}{E_{\text{tot}}} \quad Y = \frac{2E_k - E_i - E_j}{E_{\text{tot}}}$$



Conclusions:

- The selected sample is compatible with the expected behavior of a complete fusion-evaporation reaction, with the exception of specific channels corresponding to the emission of multiple α particles in coincidence with Oxygen, Carbon and Neon residue.
- Persistence of anomalous Branching Ratio for alpha decay in the fused hot ^{24}Mg in $^{14}\text{N}+^{10}\text{B}$ reaction.
- The ensemble of these observations tends to indicate the persistence of cluster structures for ^{24}Mg and/or its daughter nucleus ^{20}Ne .
- The decay of the 7.65 MeV ^{12}C Hoyle state, in peripheral and central reactions, give no indications of deviations from the sequential decay mechanisms.

Indications of in-medium structure

Inelastic scattering

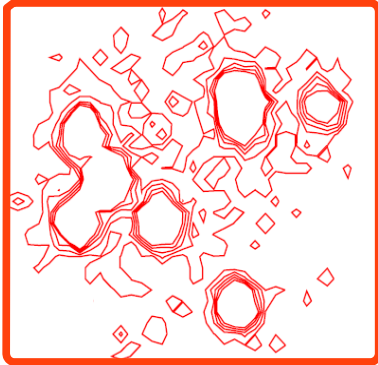
Itoh, PRL **113**(2014)102501 **<0.2 %**

Morelli et al. JoPG 43 (2016) **~1 %**

Raduta, PLB **705**(2011)65 **~17 %**

Direct decay

Fragmentation

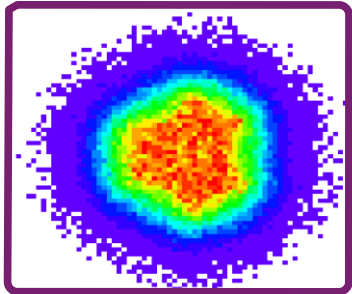


Interaction with the environment

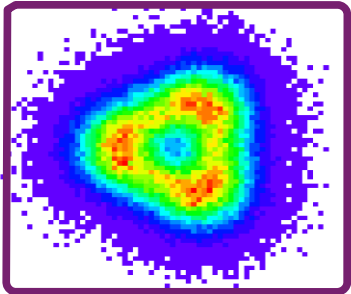
Structure modification ?

Final-state interaction ?

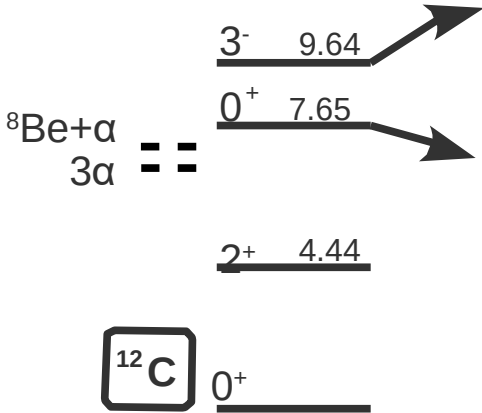
Direct



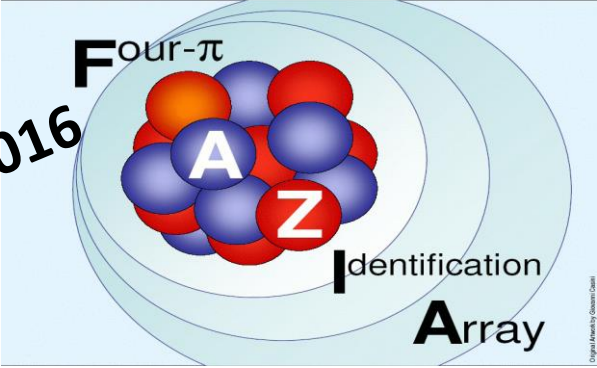
Sequential



L.Quattrocchi, NN2015



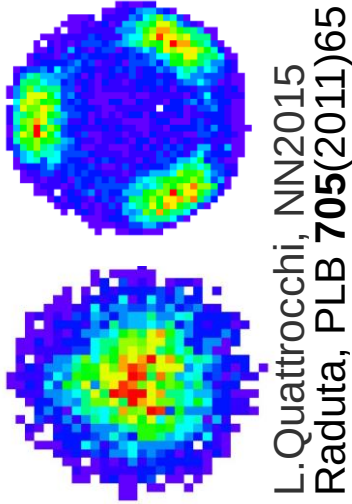
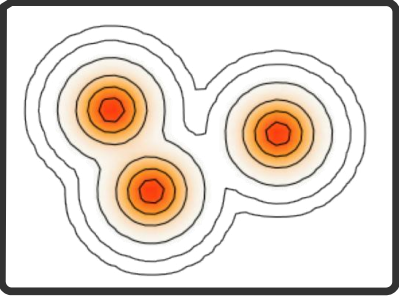
new exp. in 2016
LNS



FAZIA-COR : in-medium properties

G.Verde, IPN Orsay / D.Gruyer, INFN - Firenze

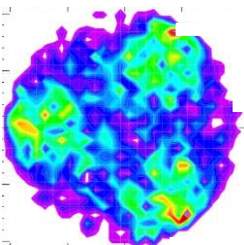
¹²C Hoyle state



Fragmentation

C+Mg@25MeV/A

CHIMERA



Fusion/
evaporation

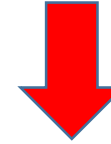
C+C@95MeV

GARFIELD

$^{16}\text{O} + ^{12}\text{C} \rightarrow ^{28}\text{Si}^*$ ongoing analysis

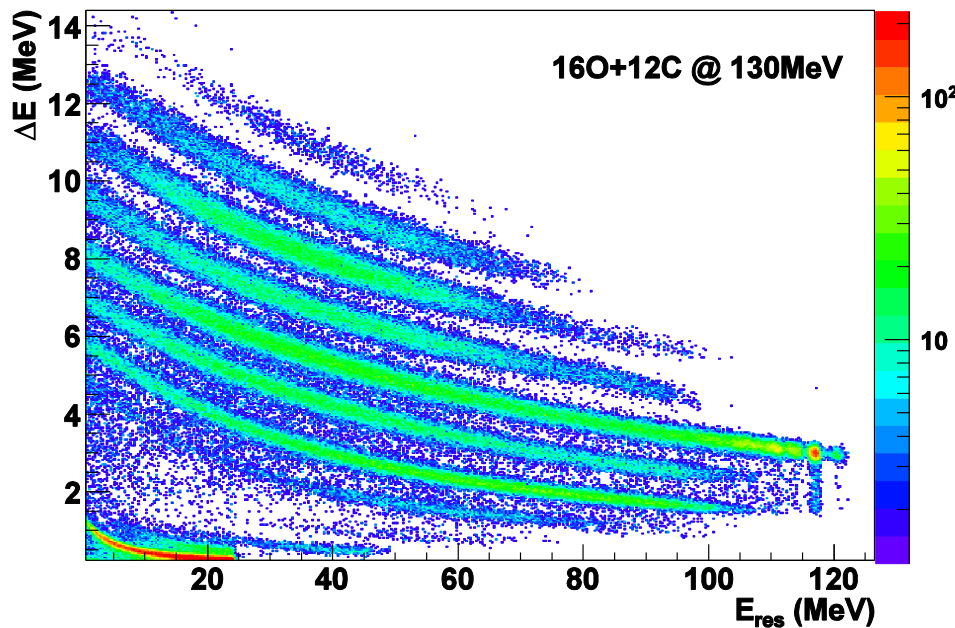
- Systematics study of even-even N=Z nuclei produced in the fusion-evaporation
- $^{16}\text{O} + ^{12}\text{C}$ reaction at three different beam energies
 $E_{\text{beam}} = 90, 110 \text{ and } 130 \text{ MeV}$
- clustering effects can be differently expressed varying the E^* of the system
- investigate R_{clus} as a function of the excitation energy

Proposal approved by LNL PAC in 2014



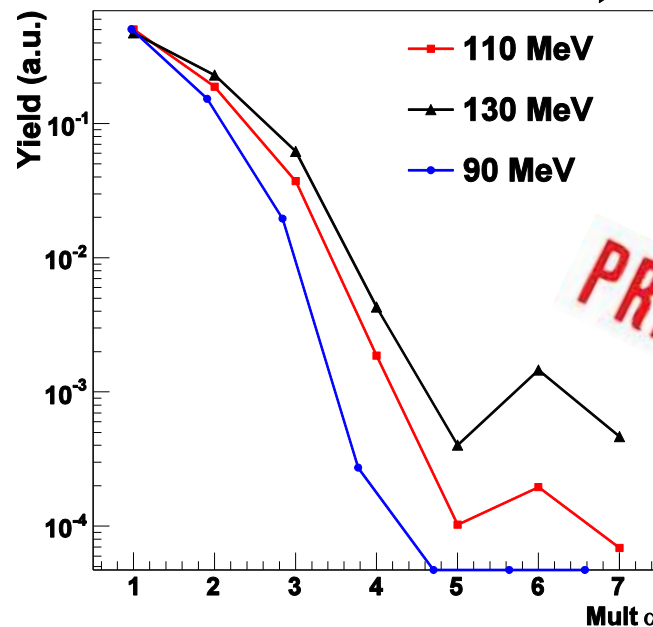
March 2015 : experiment performed

ΔE -E Rco IC-SiE

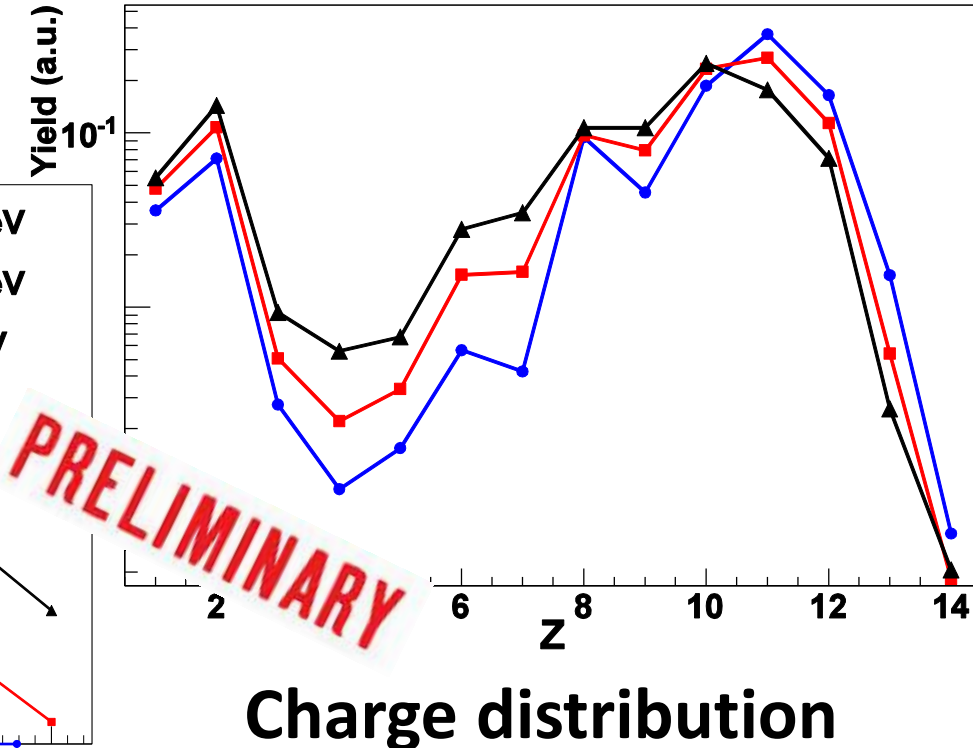


gate on evaporation residue

α multiplicity



□ the possibility that a 7 α -particle gas-like state might exist in ^{28}Si



Charge distribution

...thank you for your attention!

- L. Morelli, G. Baiocco , F. Gulminelli*, M. Bruno, M. D'Agostino, S. Barlini, M. Bini, G. Casini, M. Cinausero, M. Degerlier, D. Fabris, N. Gelli, F. Gramegna, T. Marchi, A. Olmi, G. Pasquali, S. Piantelli, S. Valdré

(NUCL-EX collaboration)

*(LPC Caen France)

