

Pre-equilibrium particles emission to study Clustering in nuclei

D. Fabris

INFN Sezione di Padova
on behalf of Nucl-Ex collaboration



FUSTIPEN Topical Meeting

Dynamical cluster formation and correlations in heavy-ion collisions,
within transport models and in experiments

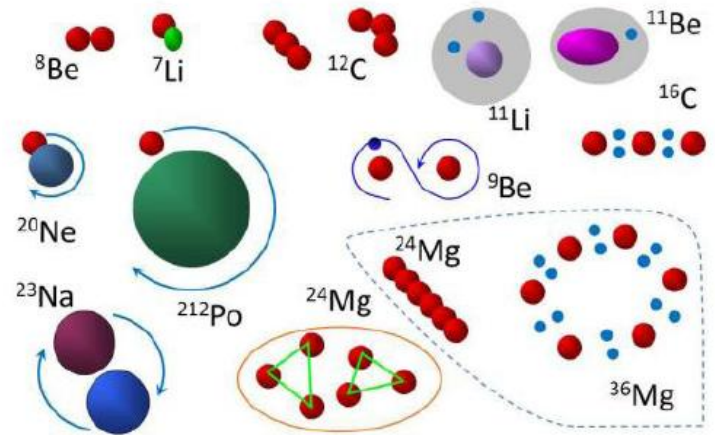
May 17 – 19, 2016 GANIL, Caen, France

Nuclear Clustering

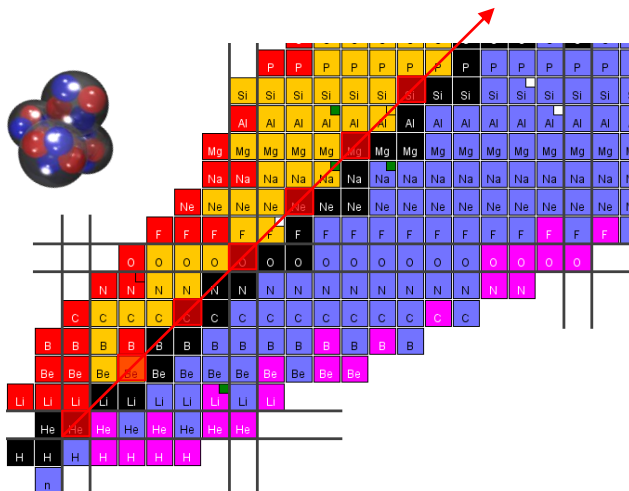
‘Clustering reactions’ are a good tool to study the interplay between nuclear structure and reaction dynamics

α -particle is the most likely cluster structure observed in $N=Z$ nuclei at E^* close to the α -decay threshold

Different other types of clustering have been experimentally investigated



W.N. Catford J. Phys. Conf. Series 436, 012095



Interest in nuclear clustering renewed due to the study of **exotic weakly-bound nuclei**

In **light nuclei** at drip-lines, clustering might be the preferred structural mode

P.E. Hodgson, E. Běták, Phys. Rep. 374 (2003) 1-89
W. Von Oertzen et al. Phys. Rep. 432 (2006) 43
M. Freer et al. , Rep. Progr. Phys. 70 (2007) 2149

Nuclear Clustering

Pre-formation

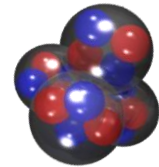


α - cluster are pre-formed inside nuclear matter

Dynamical formation Coalescence



Clusters are formed in a course of a reaction

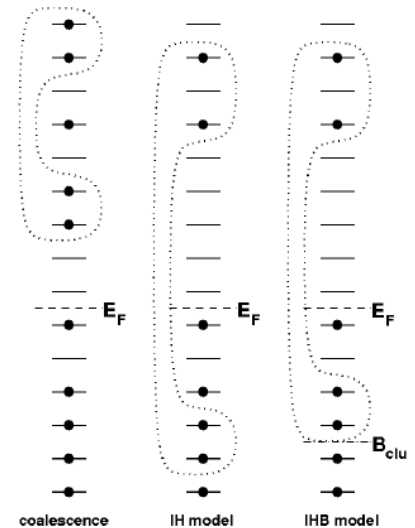


- Different phenomena of clustering effects can be related to either their **structural presence** (pre-formation) or to their **dynamical formation**.
- Links between **Cluster Emission** and its connection with nuclear structure and dynamics have been evidenced in light-mass nuclei.

Studying **Medium Mass systems** through reaction dynamics

→ **Pre-Equilibrium particles emission**

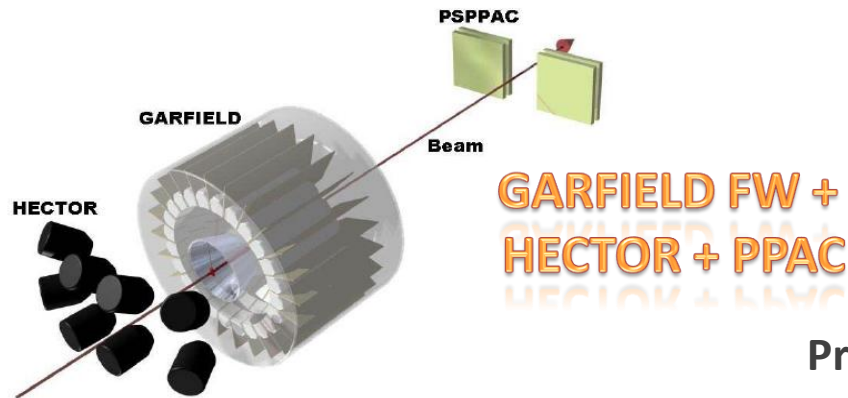
Studying the competition between evaporation (surface) and fast (volume) emission of LCP and clusters



**Different
Pre-equilibrium Models**

E. Běták EPJ Web of Conf. 21 (2012) 09004

Previous Experimental results: $^{16}\text{O} + ^{116}\text{Sn}$ @ 130, 250 MeV (8, 16 AMeV)



Light Charged Particles & High Energy γ -rays
in coincidence with
Evaporation Residues

Moving Source Fit

Protons

Alphas

130 MeV

250 MeV

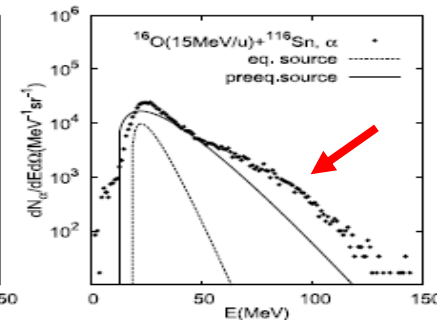
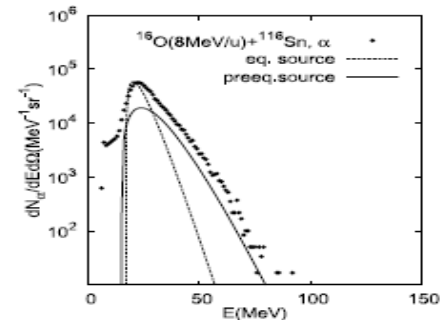
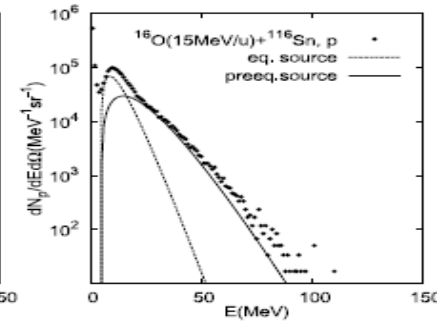
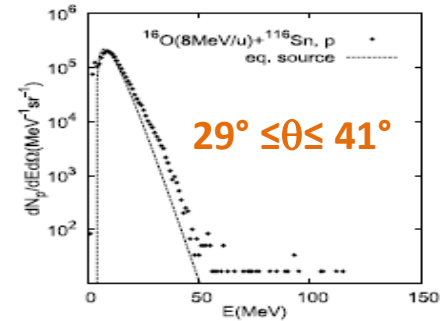


Table 3. Moving source fit parameters for the reaction $^{16}\text{O} + ^{116}\text{Sn}$ at 8.1 and 15.6 AMeV.

E (AMeV)	LCP	$\frac{N_2}{N_1}$	E_{C1} (MeV)	T_1 (MeV)	E_{C2} (MeV)	T_2 (MeV)	$\frac{v_2}{v_{CN}}$
8.1	p	0.0	2.77 ± 0.46	3.02 ± 0.16	-	-	-
8.1	α	0.21	11.0 ± 1.50	3.20 ± 0.35	12.4 ± 1.70	3.80 ± 0.75	3.83
15.6	p	0.30	3.16 ± 0.44	3.55 ± 0.47	4.49 ± 1.53	4.68 ± 0.83	5.49
15.6	α	1.30	12.3 ± 0.20	4.38 ± 0.28	12.2 ± 0.90	7.10 ± 0.60	2.85

A. Corsi et al., PLB 679 (2009) 197

Moscow Pre-equilibrium Model: statistical + pre-equilibrium emission

Evaporative (statistical) emission:

Statistical decay of a Compound Nucleus is analyzed using **modified PACE2** Monte Carlo code , with level density parametrization [**A.V. Ignatyuk et al. Sov. J.Nucl. Phys. 29 (1979) 450**] , decay competition probability (n, p, α , γ or fission), kinetic energy of emitted particles, binding energy, transmission coefficients, angular momentum.

- Insertion of **non-equilibrium** stage in the fusion reaction
- All the process probabilities are calculated within the Hauser-Feshbach model

Pre-equilibrium emission:

The Relaxation process in the nuclear system after fusion reaction is described by the **Hybrid exciton model** based on Griffin model [**J.J.Griffin PRL 17 (1966) 478, M. Blann PRL 27 (1971) 337**].

The state of nuclear system produced in the collision is determined by the **exciton number** $n_o = p_o + h_o$ where p is the number of valence particles over the Fermi energy and h the number of holes located under the Fermi energy, and by excitation energy E^* .

- The **exciton number** n_o can be determined from the empirical trend [**N.Cindro et al. Phys. Rev. Lett. 66 (1991) 868; E. Běták Fizika B12 (2003) 11**]

Model Parameters:

$n_o = p_o + h_o$	Number of excitons
$K \rightarrow M ^2 = KA^{-3}e^{-1}$	100 – 800 MeV ³
$g = 6a/p^2$	Level density parameter

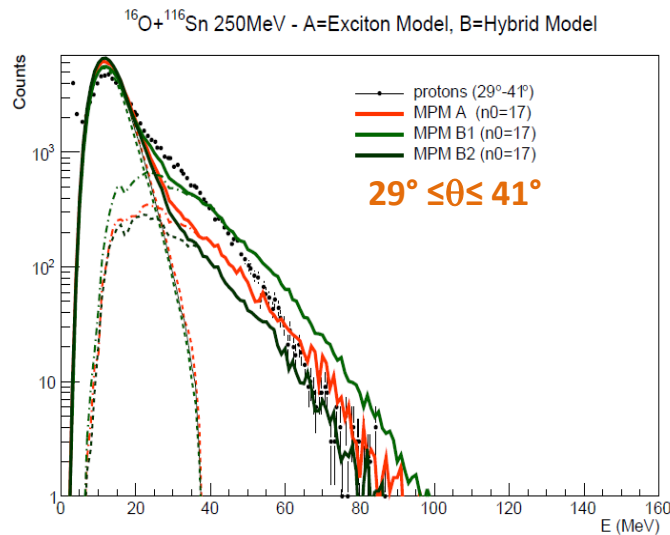
O.V. Fotina et al. Int. Journ. Mod. Phys. E19 (2010) 1134
D.O. Eremenko et al. Phys Atom. Nucl. 65 (2002) 18
O.V. Fotina et al. Phys. Atom. Nucl. 73 (2010) 1317

Comparison with *Moscow Pre-equilibrium Model*

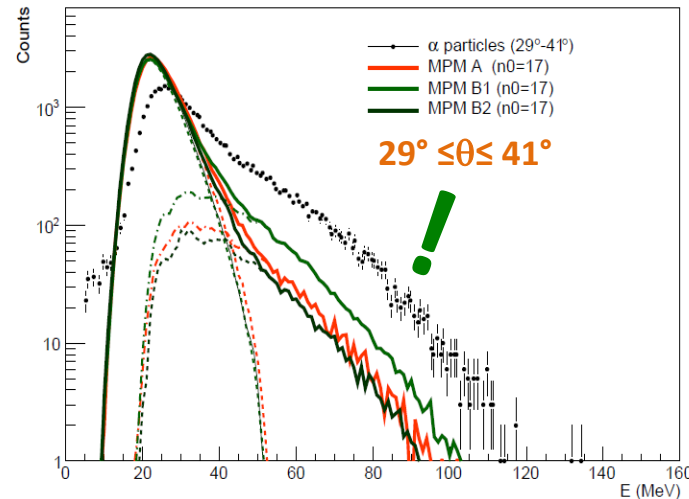
$^{16}\text{O} + ^{116}\text{Sn} @ 250 \text{ MeV}$

$n_0 = 17 (16p + 1h)$

Protons



α -particles



$$\begin{aligned} \text{B1} & \left\{ \begin{array}{l} \beta = 1.8 \\ pf_{\text{CN}} = 0.5 \end{array} \right. \\ \text{B2} & \left\{ \begin{array}{l} \beta = -1 \\ pf_{\text{CN}} = 0.95 \end{array} \right. \end{aligned}$$

Different simulations with different Pre-equilibrium particles Angular Distributions:

Caso A : based on *Exciton Model*

-> Angular Distribution from optical model

Caso B : based on *Hybrid Exciton Model*

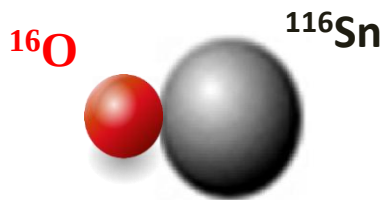
-> $q(n, \Omega, t)$ with Ω direction of fast particle
 β nuclear finite size effect

Adding α -clusters structure effect to the model

Clustering:

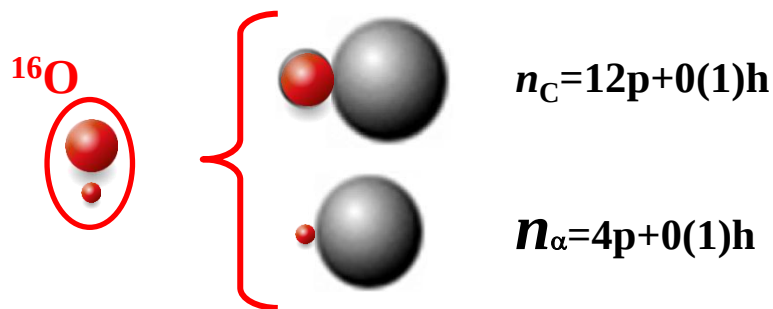
Pre-formation probability of cluster in the projectile and exciton energies for cluster/light ion induced reactions

→ 2 possible starting configurations are considered in ^{16}O nucleus



$$n_0 = 16p + 0(1)h$$

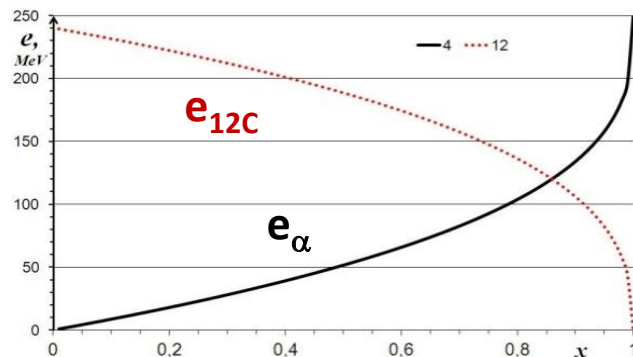
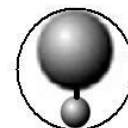
$$100 - N(\%)$$



$$N(\%) = ??$$

$$\begin{array}{ll} 2^+ & \text{--- } 6,917 \text{ MeV} \\ 0^+ & \text{--- } 6,049 \text{ MeV} \end{array}$$

$$0^+ \text{ --- Stable } Q_\alpha = -7,162 \text{ MeV}$$



$$e = E(1 - (1 - x)^{1/(n-1)}).$$

e – clusters energy
 x – random number

PHYSICAL REVIEW C, VOLUME 62, 034604

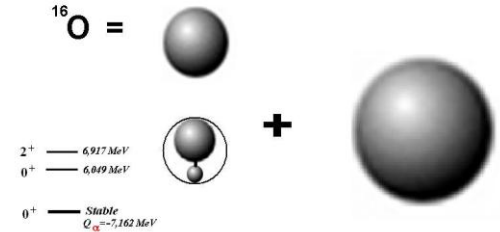
Precompound Monte-Carlo model for cluster induced reactions

M. Blann¹ and M. B. Chadwick²

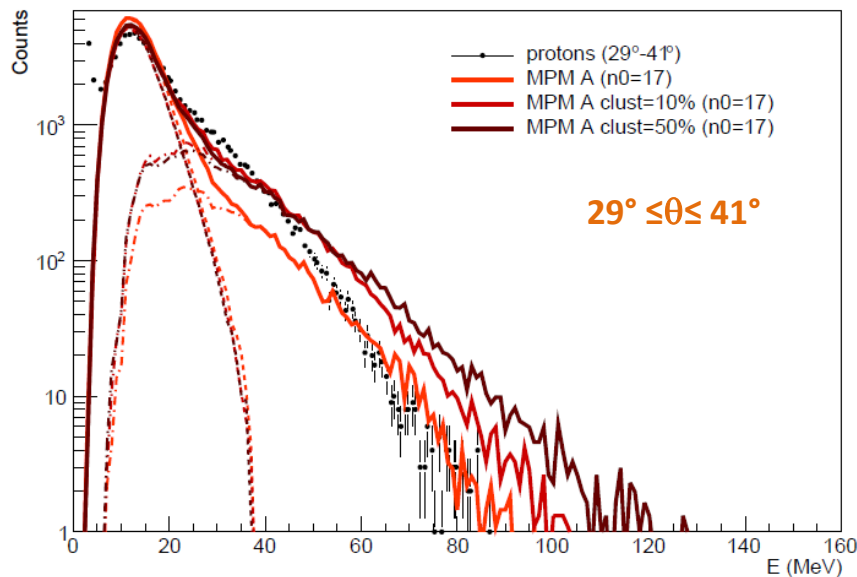
Comparison with *Moscow Pre-equilibrium Model* : projectile **Clustering**

$^{16}\text{O} + ^{116}\text{Sn} @ 250 \text{ MeV}$

- Exp
- No α -clustering in ^{16}O
- 10% α -clustering in ^{16}O
- 50% α -clustering in ^{16}O

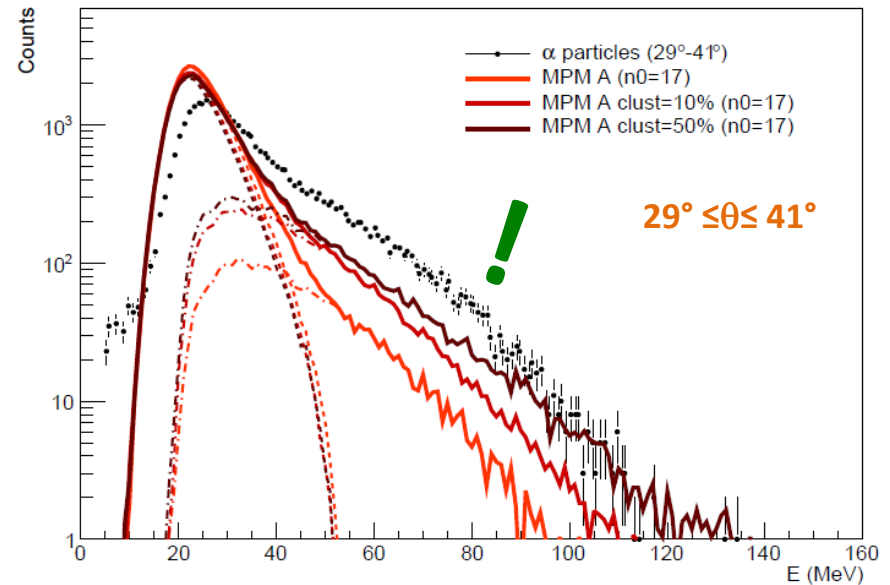


Protons



Protons : No α -clustering

α -particles

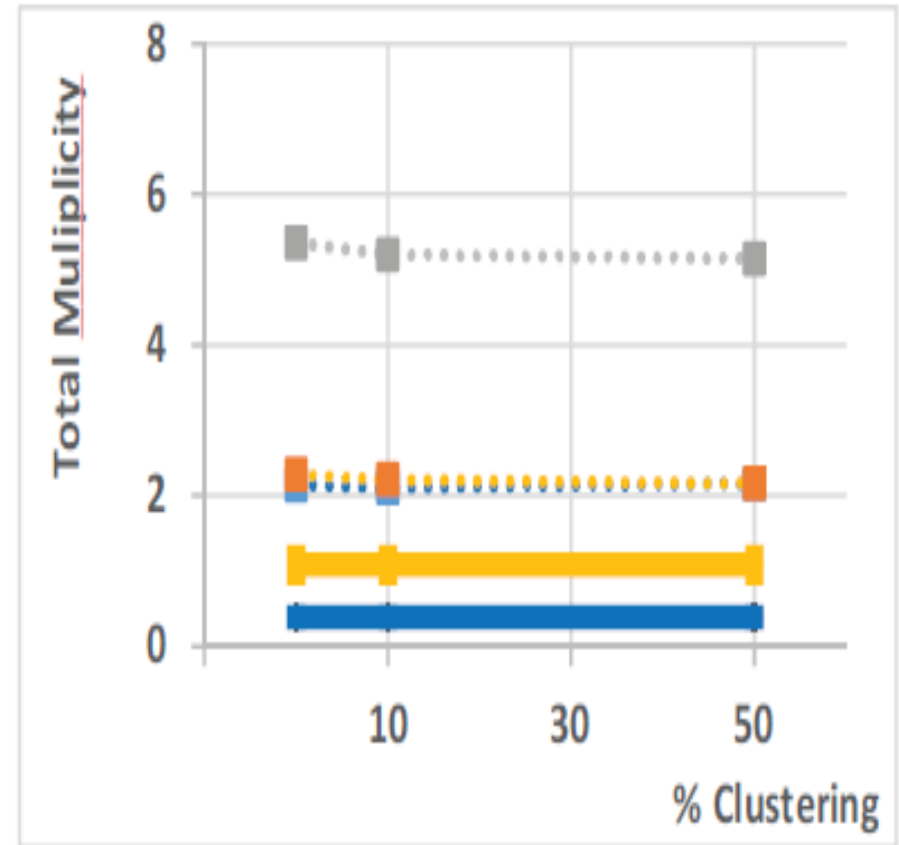
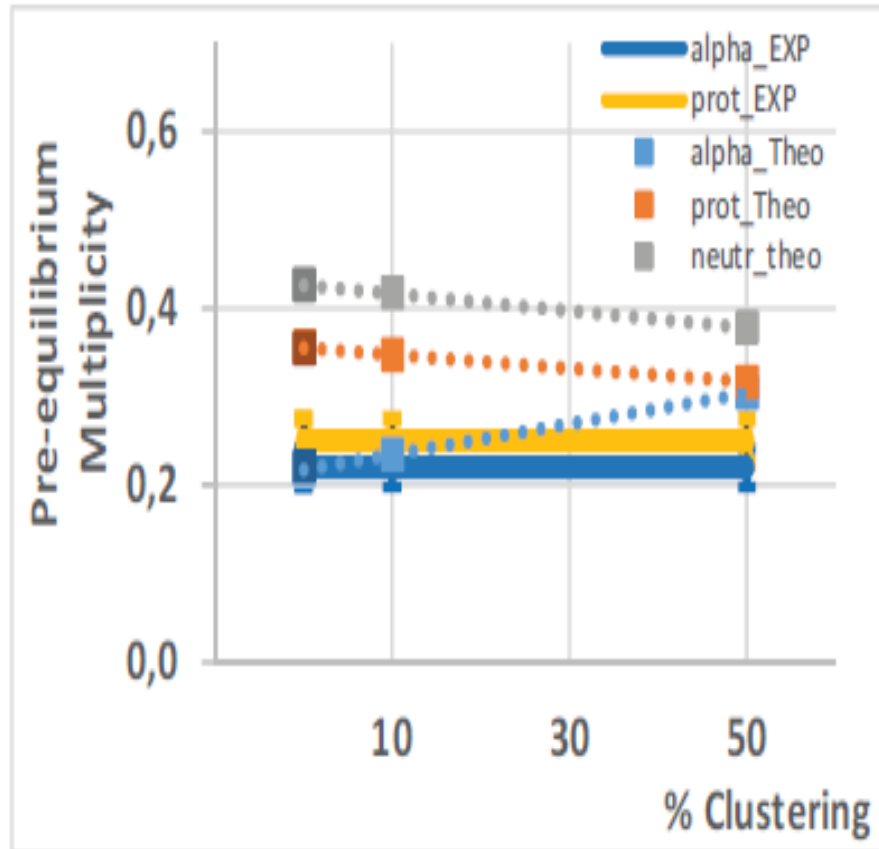


α -particles : not completely described by 50% α -clustering , but it is going in the right direction..

Comparison with *Moscow Pre-equilibrium Model* : projectile **Clustering**

$^{16}\text{O} + ^{116}\text{Sn}$ @ 250 MeV

Multiplicities



$$[M^{\alpha}_{\text{pre}}/M^{\alpha}_{\text{tot}}]_{\text{exp}} \sim 0.5$$



$$[M^{\alpha}_{\text{pre}}/M^{\alpha}_{\text{tot}}]_{\text{theo}} \sim 0.1$$

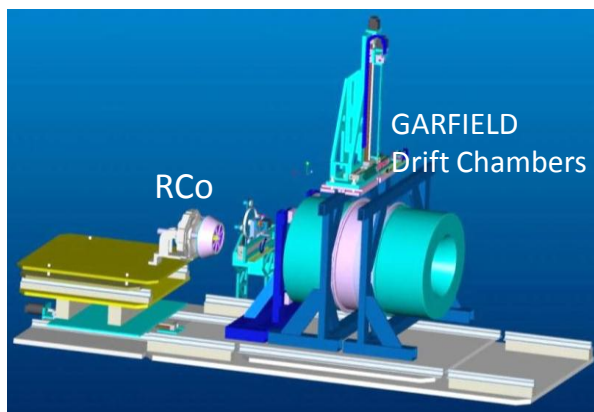
- To study possible effects of **α -cluster structure** in the **projectile** :
 - comparing light charged particles emitted in **two fusion reactions** with different N/Z projectiles
 - studying **pre-equilibrium particles emission**



$$\begin{array}{l}
 \text{CN } {}^{81}\text{Rb}^* \quad E^*({}^{16}\text{O}) = 209 \text{ MeV} \\
 \quad \quad \quad E^*({}^{19}\text{F}) = 240 \text{ MeV}
 \end{array}$$

- Two systems with the **same projectile velocity** -> **Pre-equilibrium emission** depends mainly on the projectile energy per nucleon

J. Cabrera et al., Phys rev C68(2003) 034613



M. Bruno et al., EPJ A 49 (2013) 128

- Set-up:** **GARFIELD** 4 π apparatus at Legnaro National Laboratory for Fragments and Light Charged Particles identification with **Ring Counter (Rco)** at forward angles fully equipped with digital electronics

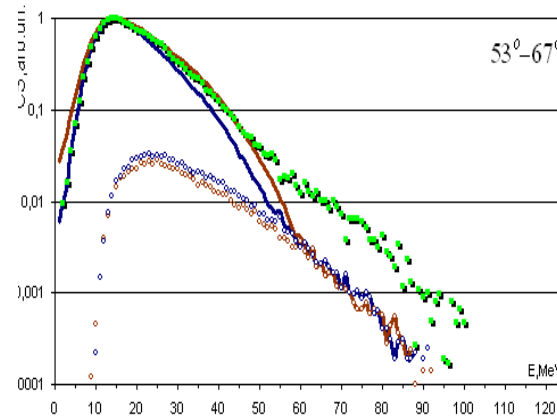
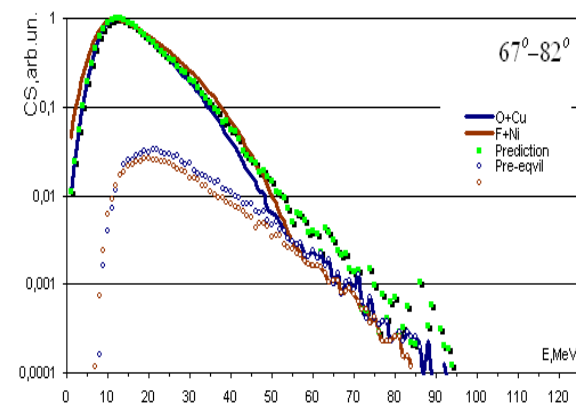
Moscow Pre-equilibrium Model: plus **Clustering**

Predictions

$^{16}\text{O} + ^{65}\text{Cu}$

$^{19}\text{F} + ^{62}\text{Ni}$

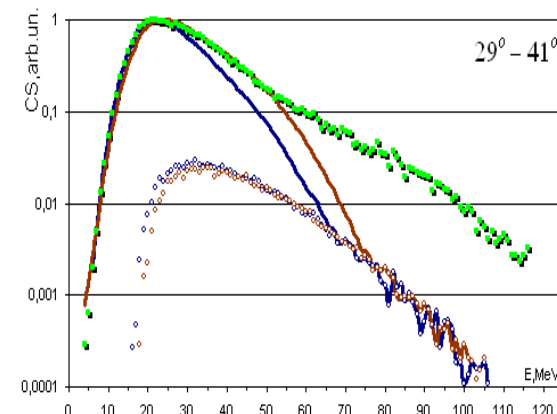
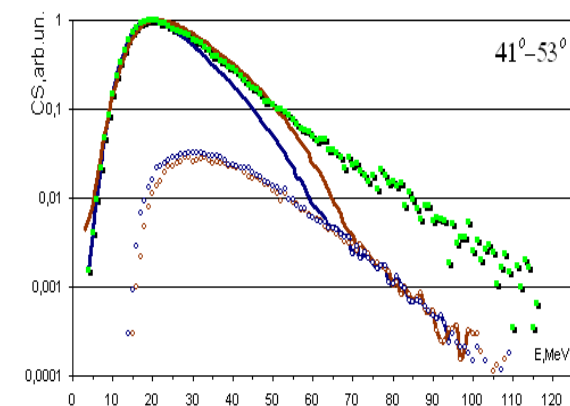
α -particles



□ Evaporative : small differences

□ Pre-equilibrium: same

□ 50% α -clustering in ^{16}O :
high energy tail increase

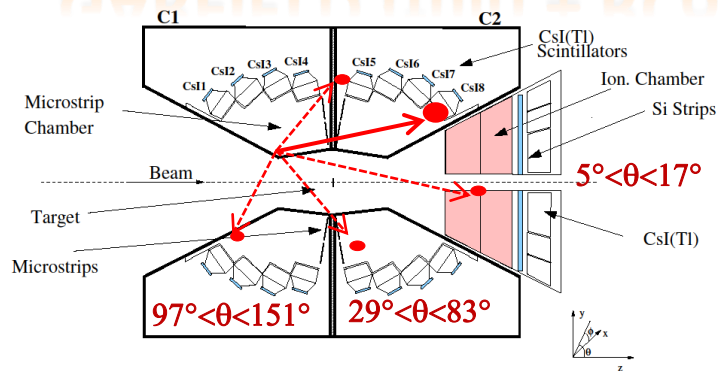


If any differences

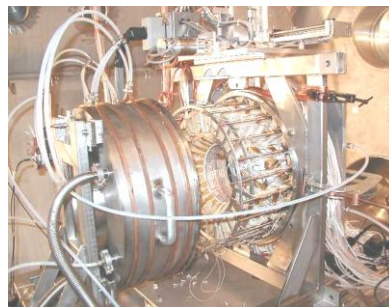
-> **clusterization of ^{16}O projectile**

Experimental set-up: GARFIELD + RCo

GARFIELD (full) + RCo

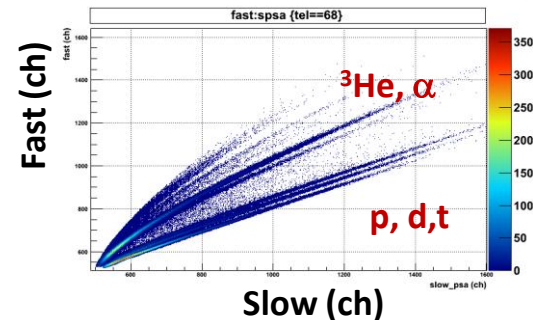


GARFIELD

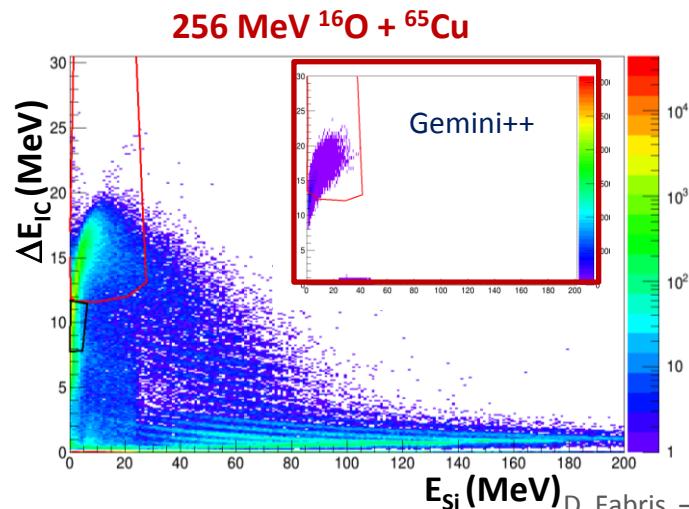


- Two Drift Chambers
- Double stage ΔE -E:
 μ Strip Gas Counter + CsI(Tl)
- Z identification
- A identification ($1 \leq A \leq 3$)
(in total **180+180** for the 2 chambers)

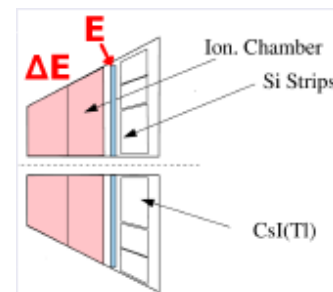
PSA CsI GARFIELD



Evaporation Residues identified in
RCo IC-Si : $\Delta\theta = 8.6^\circ \div 17^\circ$



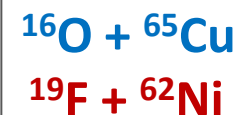
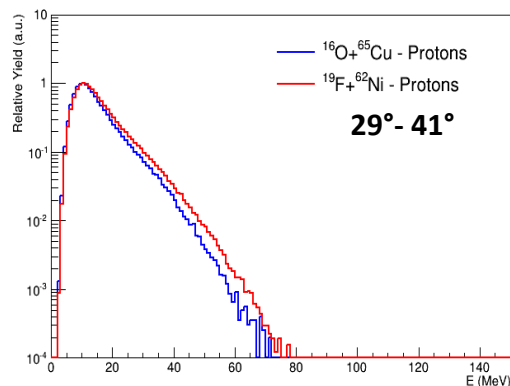
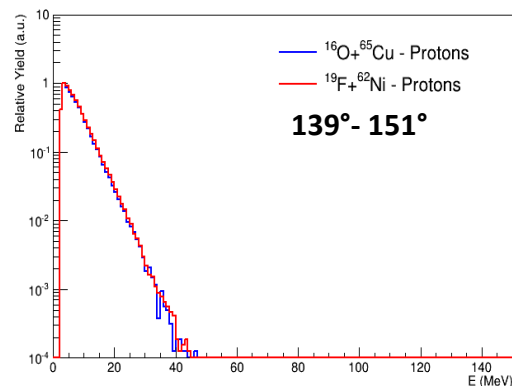
RCo



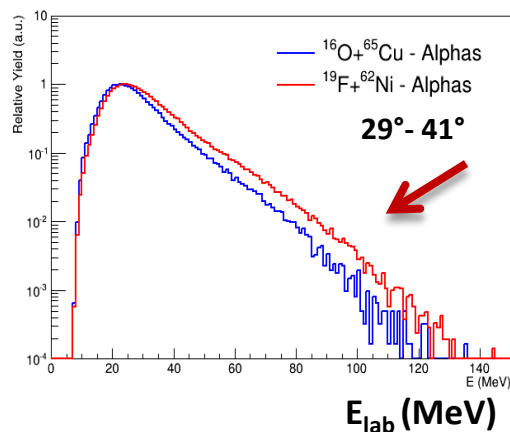
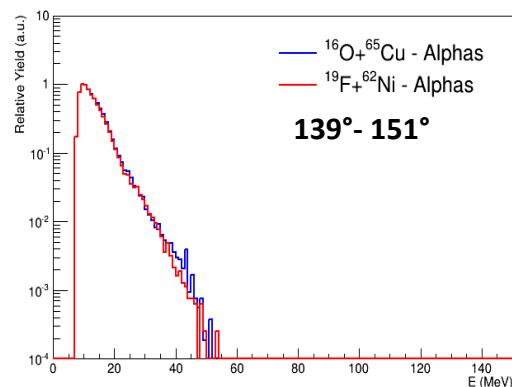
- Three stage telescope:
IC + Si Strip + CsI(Tl).
- Z, A identification

Experimental spectra in Lab

Protons



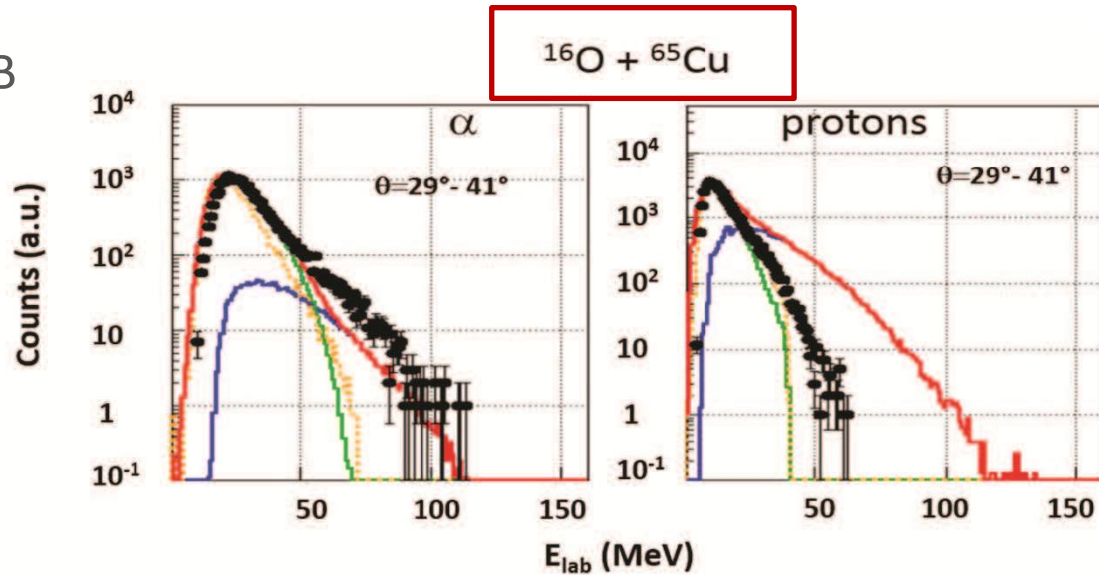
α -particles



Larger Pre-equilibrium contribution from **^{19}F induced reaction** α -spectra with respect to ^{16}O

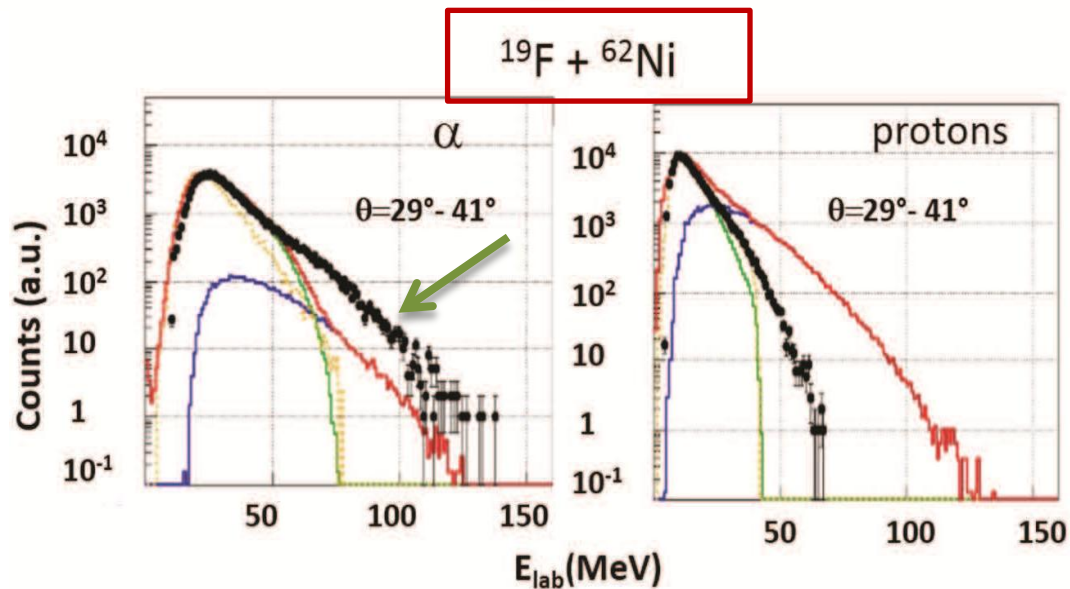
Comparison with *Moscow Pre-equilibrium Model* : **NO clustering**

Case B



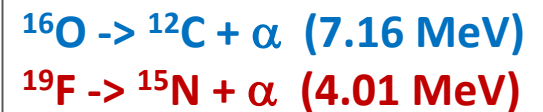
$$n_0 = 17(16p + 1h)$$

- Exp
- Total
- Pre-eq
- Evap
- - - PACE

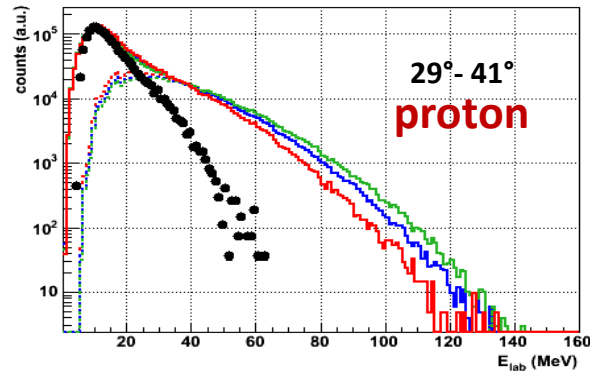
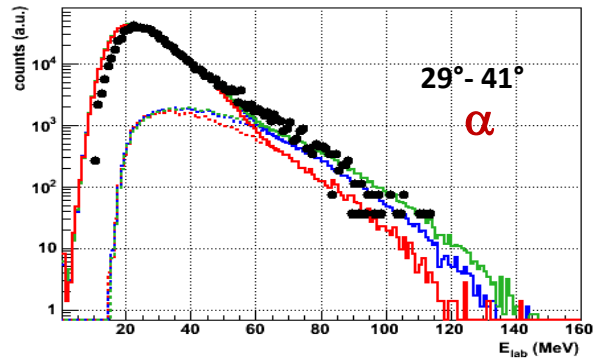


$$n_0 = 20(19p + 1h)$$

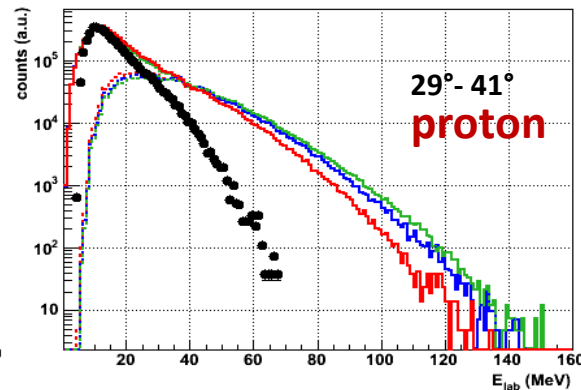
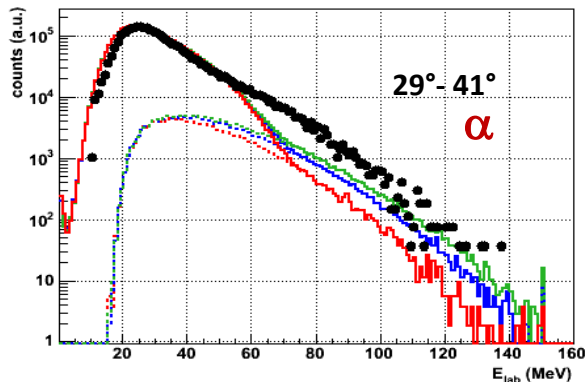
But.....



Comparison with *Moscow Pre-equilibrium Model*: changing exciton number n_0



- Exp
 - $n_0 = 17$ — Total Pre-eq
 - $n_0 = 15$ — Total Pre-eq
 - $n_0 = 14$ — Total Pre-eq



- Exp
 - $n_0 = 20$ — Total Pre-eq
 - $n_0 = 18$ — Total Pre-eq
 - $n_0 = 17$ — Total Pre-eq

Theoretical Models

Statistical Model

- **GEMINI ++ code** - most used Statistical Model in heavy ion collisions to simulate the decay of hot nuclei
 - ✓ *Standalone* when a good selection of central events can be performed
 - ✓ *Afterburner (after a dynamical code)* to produce secondary particles distributions from primary fragments -> to be compared with experimental data

R. J. Charity, Phys Rev C 82 (2010) 014610

Dynamical Models

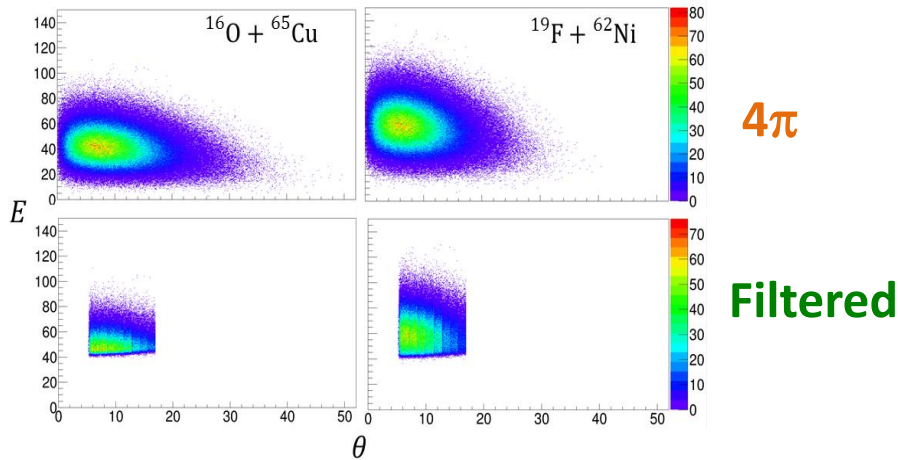
- **Stochastic Mean Field (SMF)** - **Twingo** code, based on SMF model, has been used to generate primary fragments distributions.
- **Antisymmetrized Molecular Dynamics (AMD)** - Clustering effects are better described, but not still optimized for Low Energies.

M. Colonna et al. NPA 642 (1998) 449

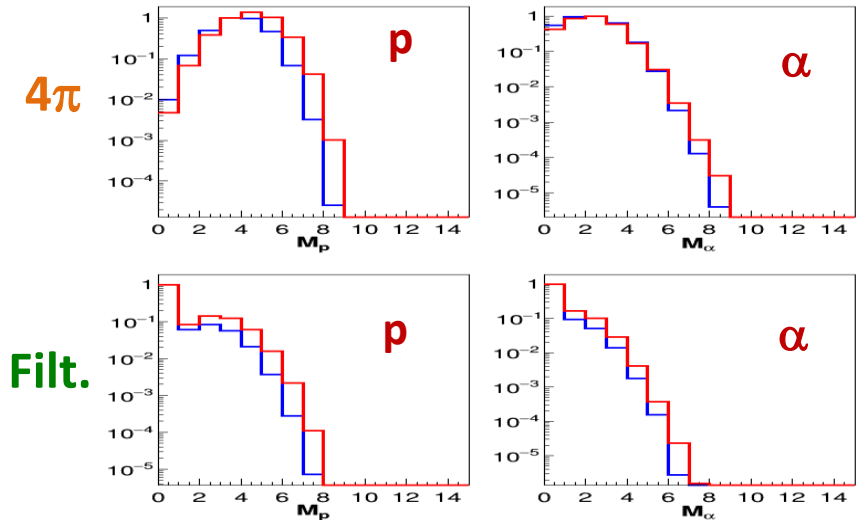
A. Ono, PRC 59 (1999) 853

GEMINI++ : Effect of the **Experimental filter** on the two systems

Evaporation Residues **E vs. θ** Distributions



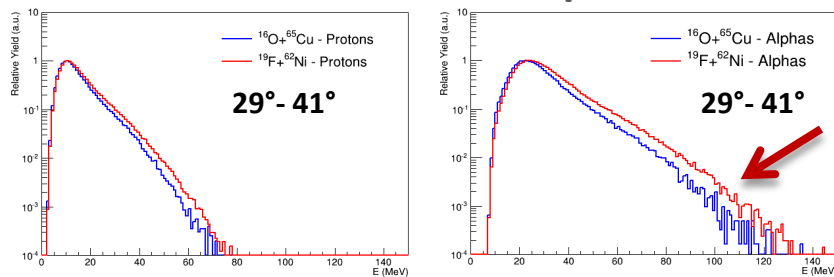
Particle Multiplicity



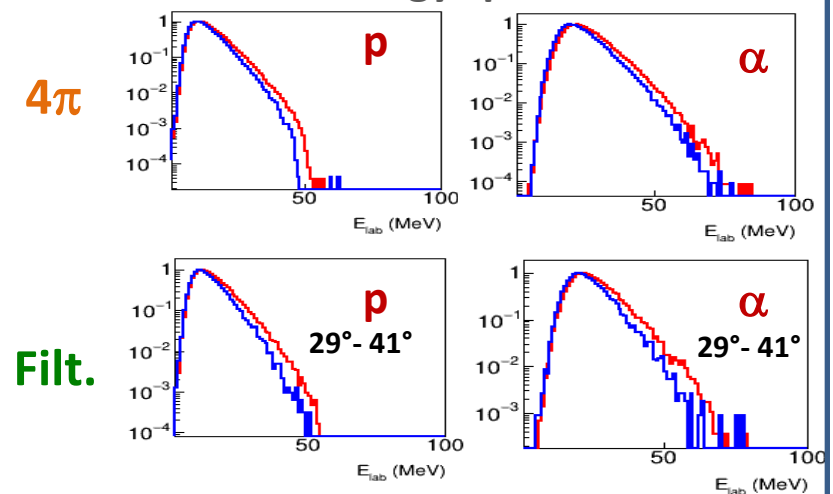
Experimental Energy spectra

Protons

α -particles



Energy spectra

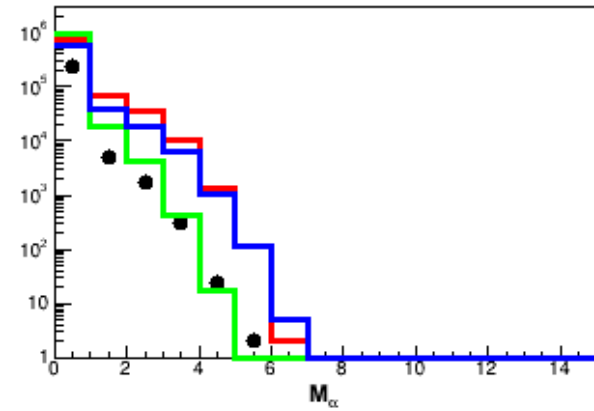
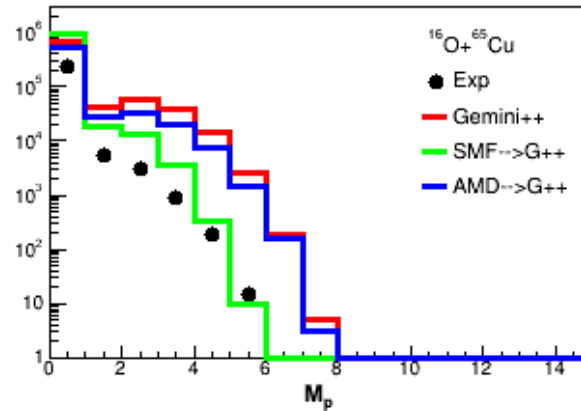


Comparison with different Models: **LCP Multiplicities** coinc. *Residues*

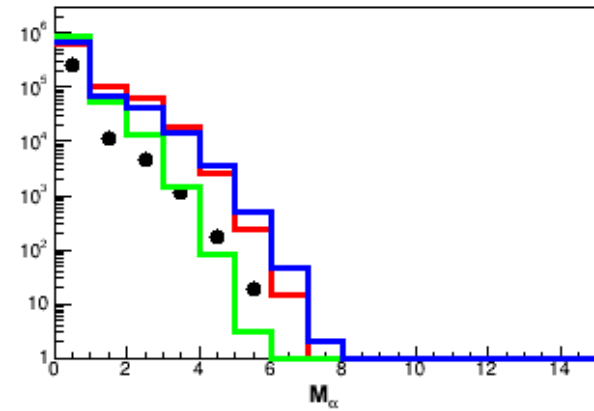
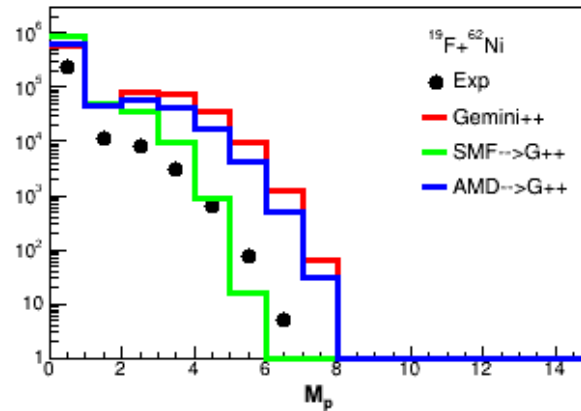
Protons

α -particles

$^{16}\text{O}+^{65}\text{Cu}$



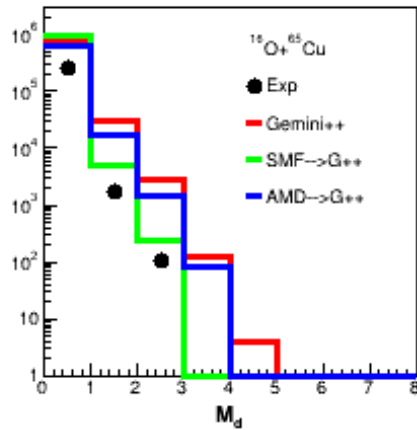
$^{19}\text{F}+^{62}\text{Ni}$



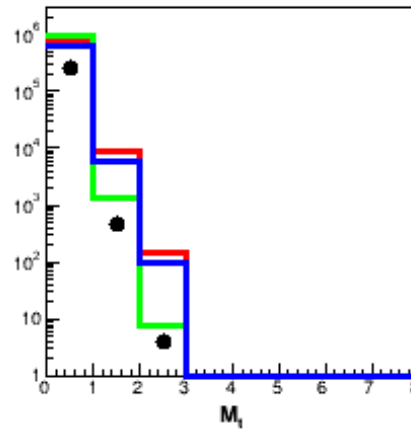
Comparison with different Models: **LCP Multiplicities** coinc. *Residues*

$^{16}\text{O}+^{65}\text{Cu}$

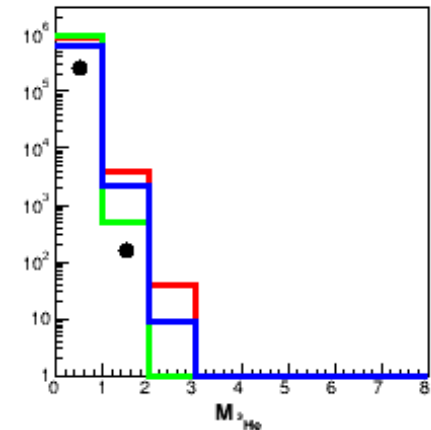
Deuteron



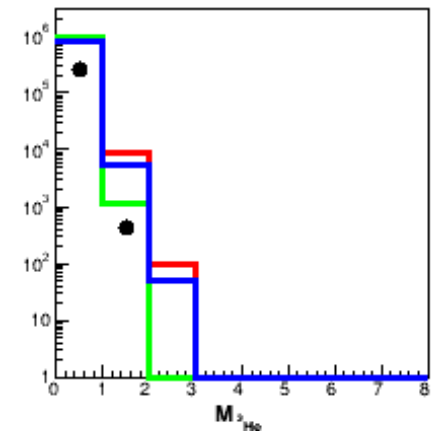
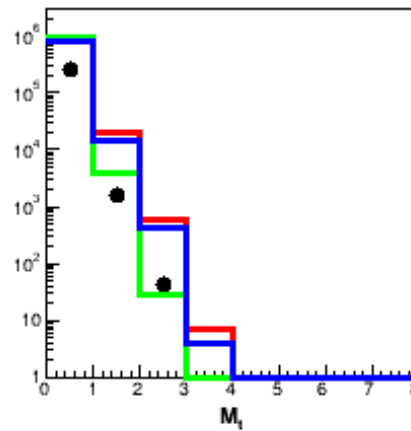
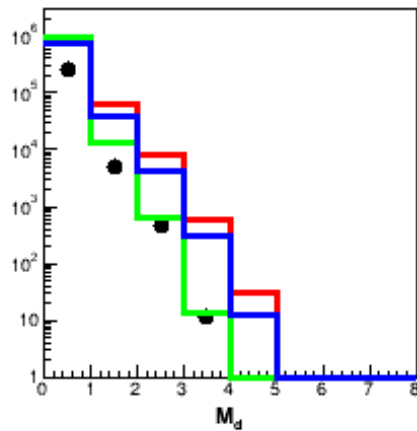
Tritons



^3He



$^{19}\text{F}+^{62}\text{Ni}$

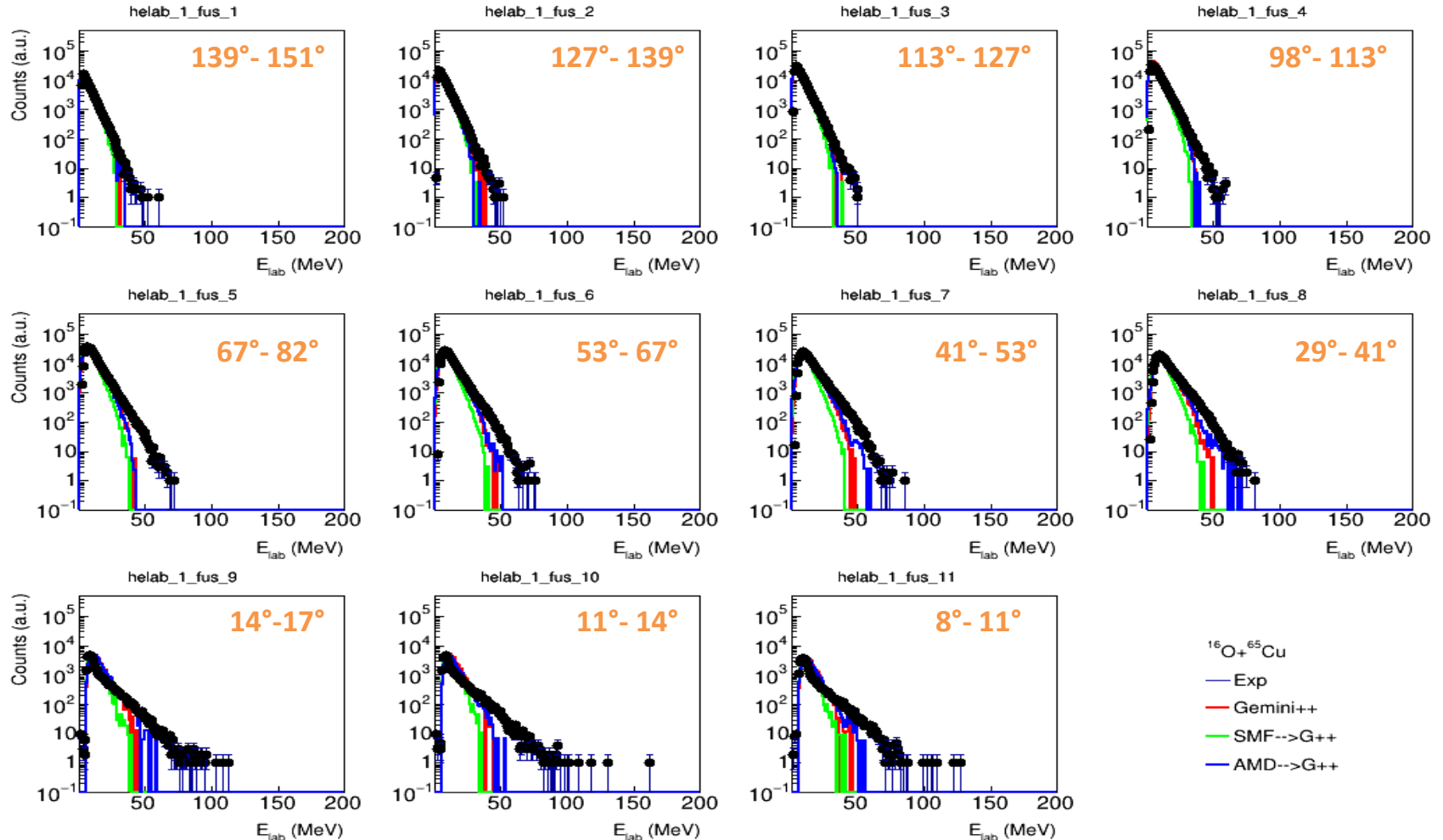


Comparison with different Models: Energy spectra in Lab

$^{16}\text{O}+^{65}\text{Cu}$

Protons

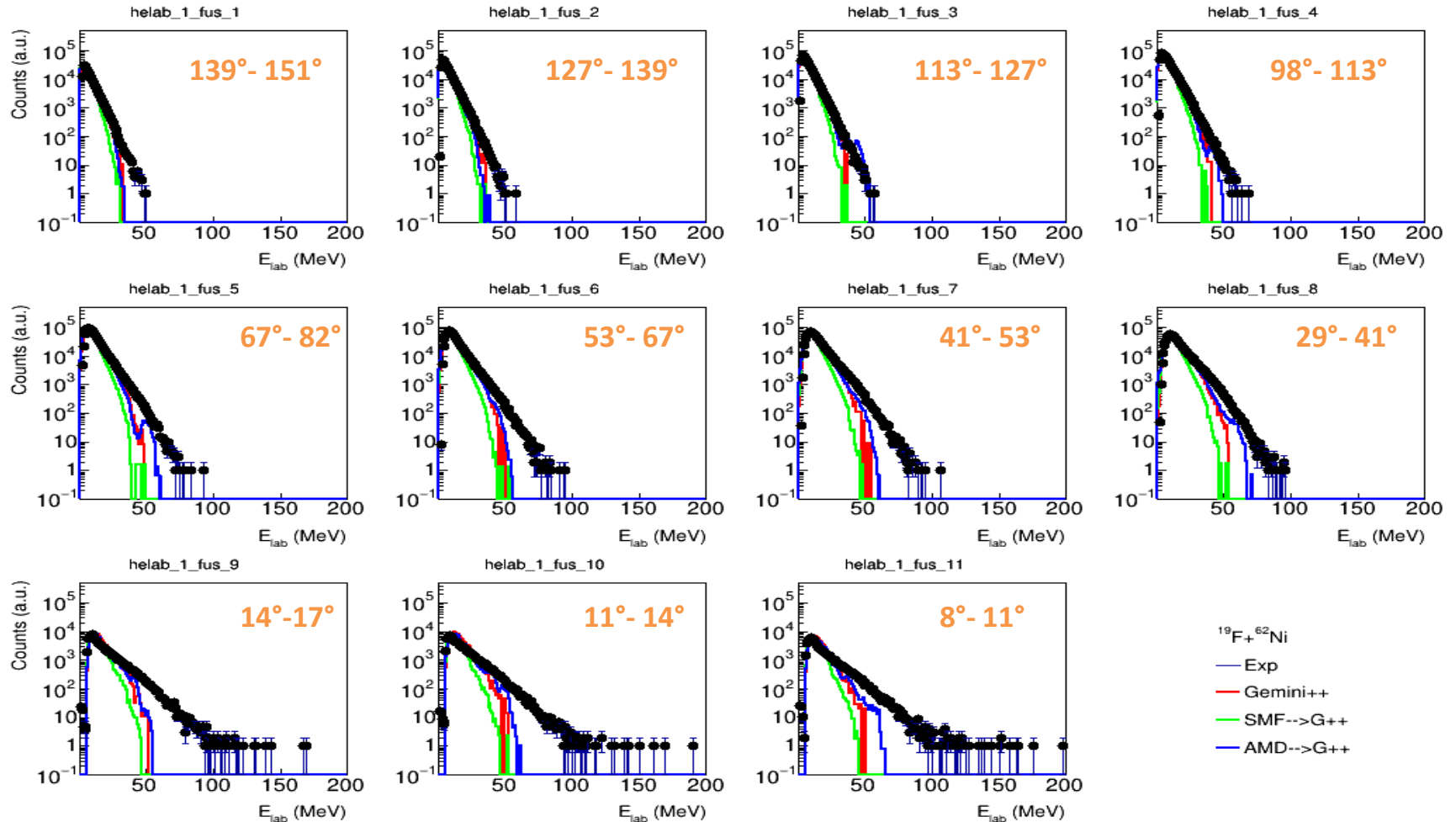
Coincidence with *Residues*



$^{19}\text{F} + ^{62}\text{Ni}$

Protons

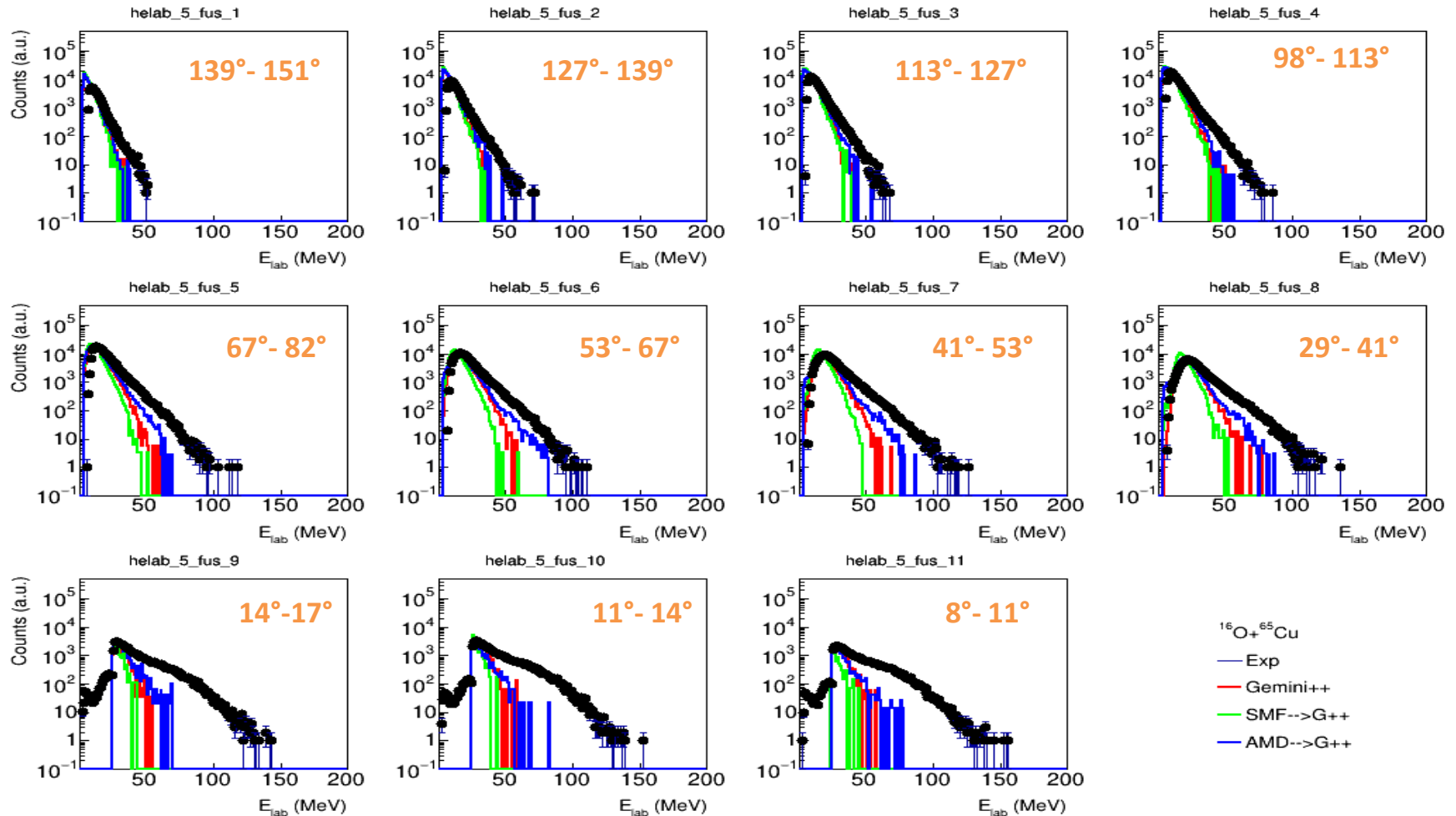
Coincidence with *Residues*

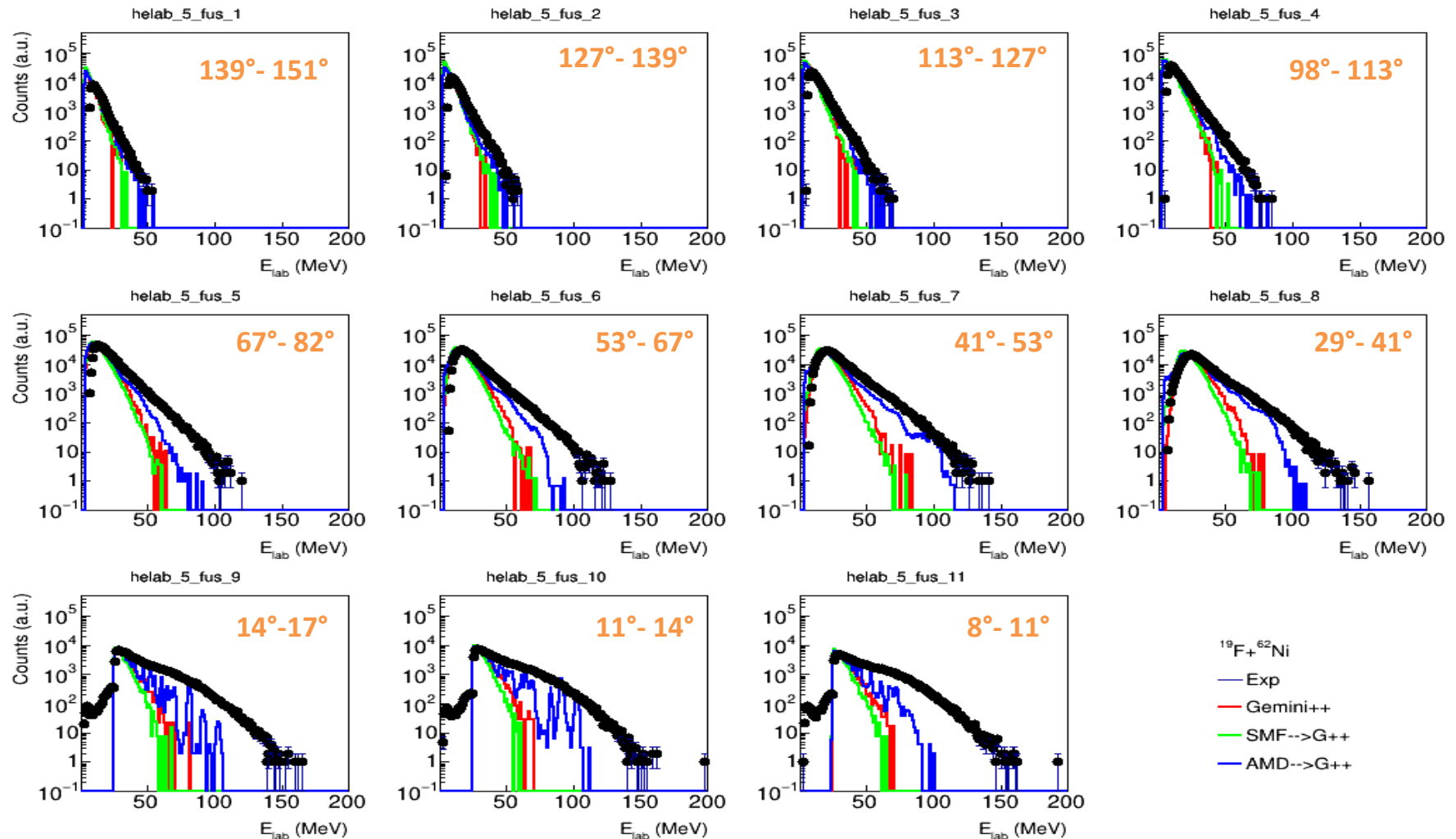


$^{16}\text{O}+^{65}\text{Cu}$

α -particles

Coincidence with *Residues*



$^{19}\text{F} + ^{62}\text{Ni}$ α -particlesCoincidence with *Residues*

Summary

- The **Pre-equilibrium particles emission** from the two $^{16}\text{O} + ^{65}\text{Cu}$ and $^{19}\text{F} + ^{62}\text{Ni}$ has been measured to get information on projectile clustering effects .
- Previous findings of overproduction of Pre-equilibrium α -particles, especially in the ^{19}F induced reaction, has been confirmed also from the comparison with statistical predictions of the **GEMINI ++** code, filtered through a replica of the experimental set-up
- The **Moscow Pre-equilibrium** model reasonably describes the α energy spectra, but overestimates the proton spectra. Model implementation are ongoing to include Clustering structure effects.
- The dynamical part of the reaction is under study using the **SMF Model** (Stochastic Mean Field) with GEMINI++ as *Afterburner* .
- Clustering effects are better described by the **AMD Model** (Antisymmetrized Molecular Dynamics) whc seems to agree better with the experimental data, even if it is not still optimized for Low Energies.

What next....

- **Complete the data analysis looking to more exclusive observables..**
- **Improve the comparison with theoretical models ...**

NUCL-EX collaboration

D. Fabris¹, F. Gramegna², T. Marchi², M. Cicerchia², J. Mabilia², M. Degerlier³, V.L. Kravchuk⁴, M. Cinausero², S. Appannababu², M. Bruno⁵, M. D'Agostino⁵, G. Baiocco⁵, L. Morelli⁵, G. Casini⁶, S. Barlini⁶, M. Bini⁶, A. Olmi⁶, G. Pasquali⁶, S. Piantelli⁶, G. Poggi⁶, S. Valdrè⁶, O.V. Fotina⁷, A. Brondi⁸, R. Moro⁸, E. Vardaci⁸

¹*INFN sezione di Padova, Padova, Italy*

²*Laboratori Nazionali di Legnaro, Legnaro (PD), Italy*

³*University of Nevsehir, Science and Art Faculty, Physics Department, Nevsehir, Turkey*

⁴*National Research Center “Kurchatov Institute”, Moscow, Russia*

⁵*Dipartimento di Fisica, Università di Bologna and INFN sezione di Bologna, Bologna, Italy*

⁶*Dipartimento di Fisica, Università di Firenze and INFN sezione di Firenze, Firenze, Italy*

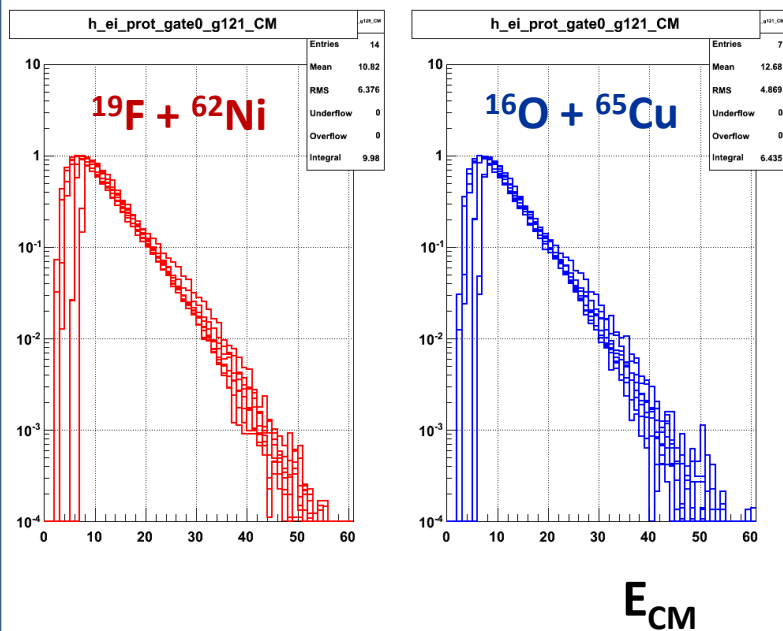
⁷*Skobeltsyn Institute of Nuclear Physics, Moscow State University, Moscow, Russia*

⁸*Dipartimento di Scienze Fisiche, Università di Napoli “Federico II”, Napoli, Italy*

Spares

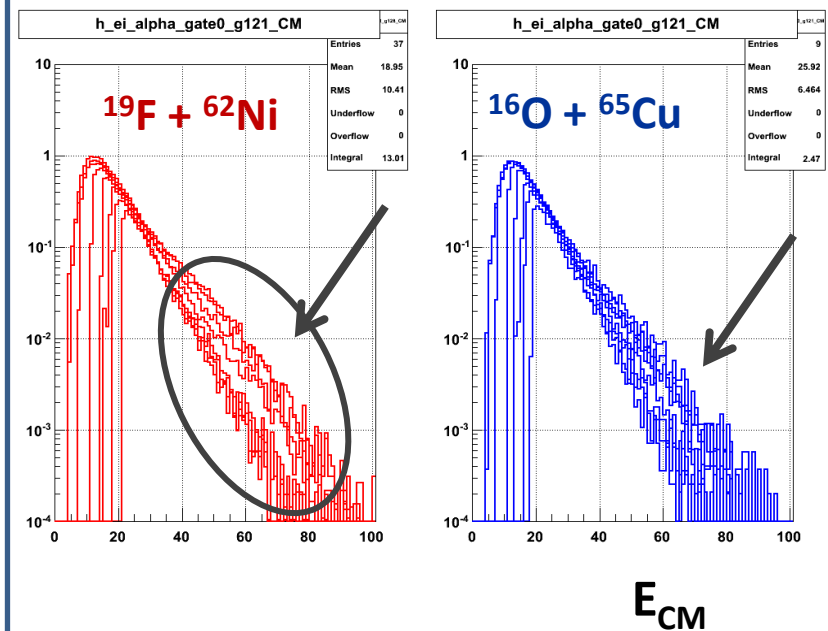
CM Spectra at different angles

Proton in CM



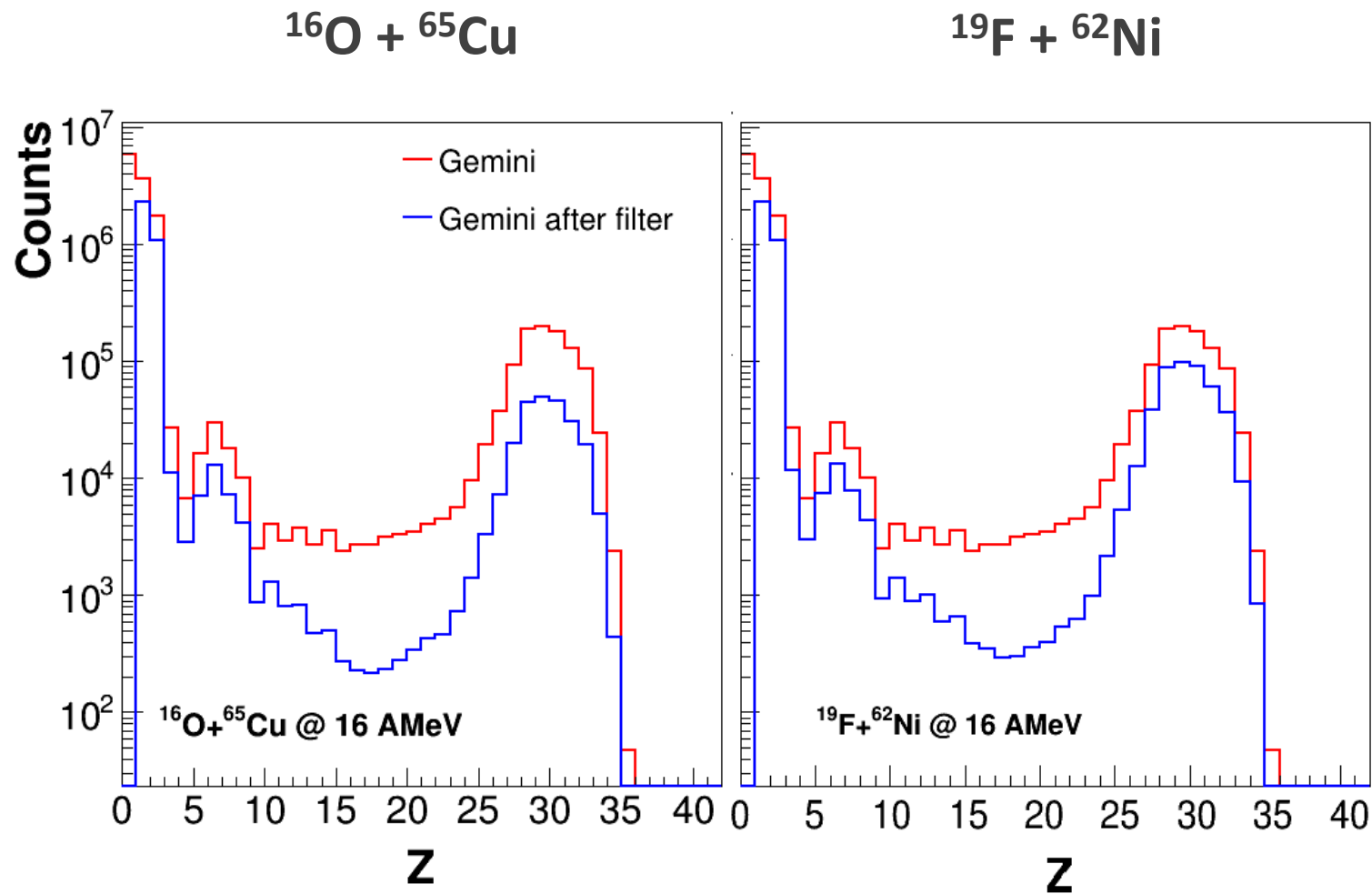
Very **small** pre-equilibrium contribution in proton spectra

Alpha in CM



Larger pre-equilibrium contribution in ^{19}F induced reaction α -spectra with respect to ^{16}O reaction

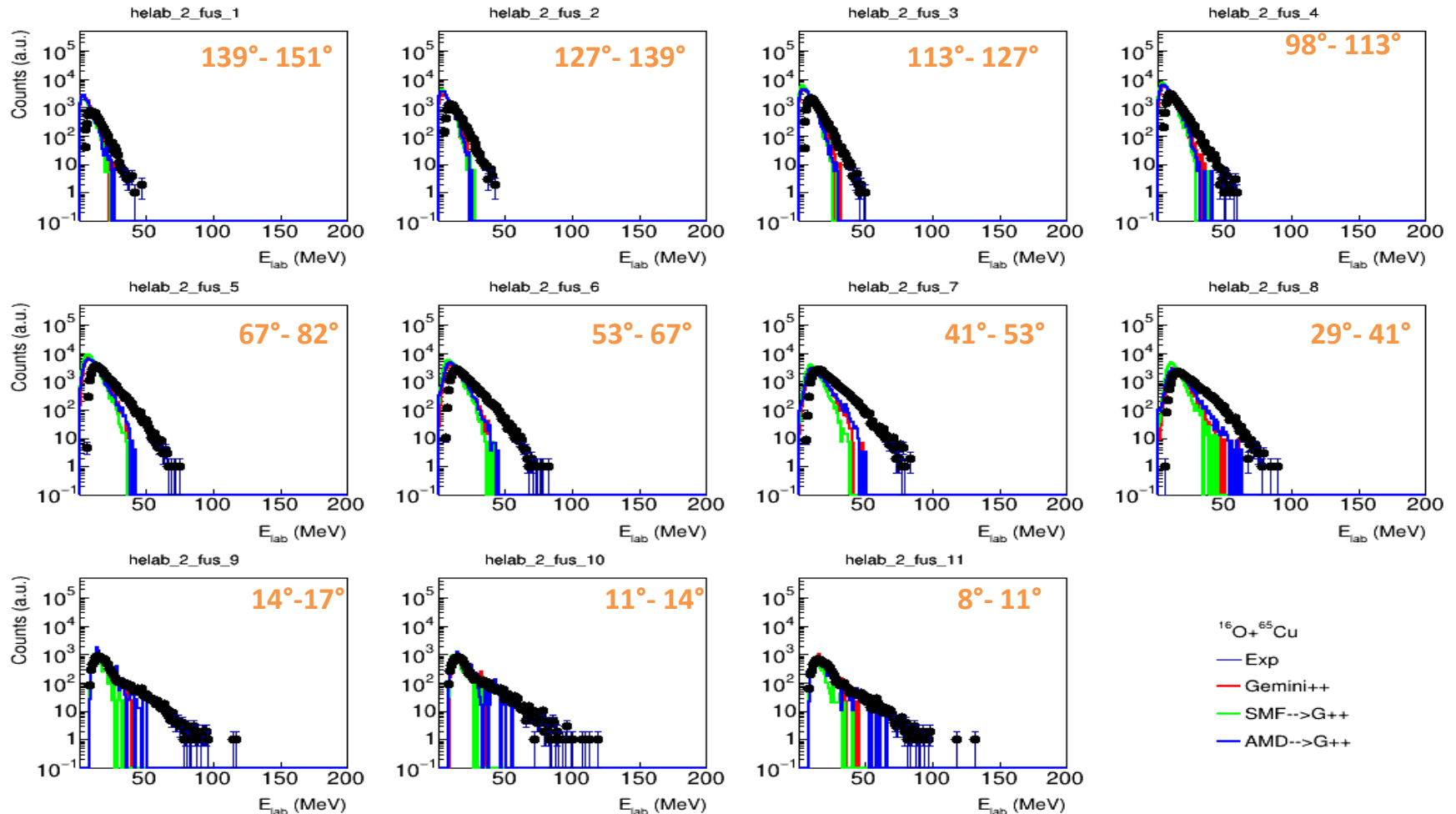
GEMINI ++ : Total **Z** Distributions



$^{16}\text{O}+^{65}\text{Cu}$

Deuterons

Coincidence with *Residues*

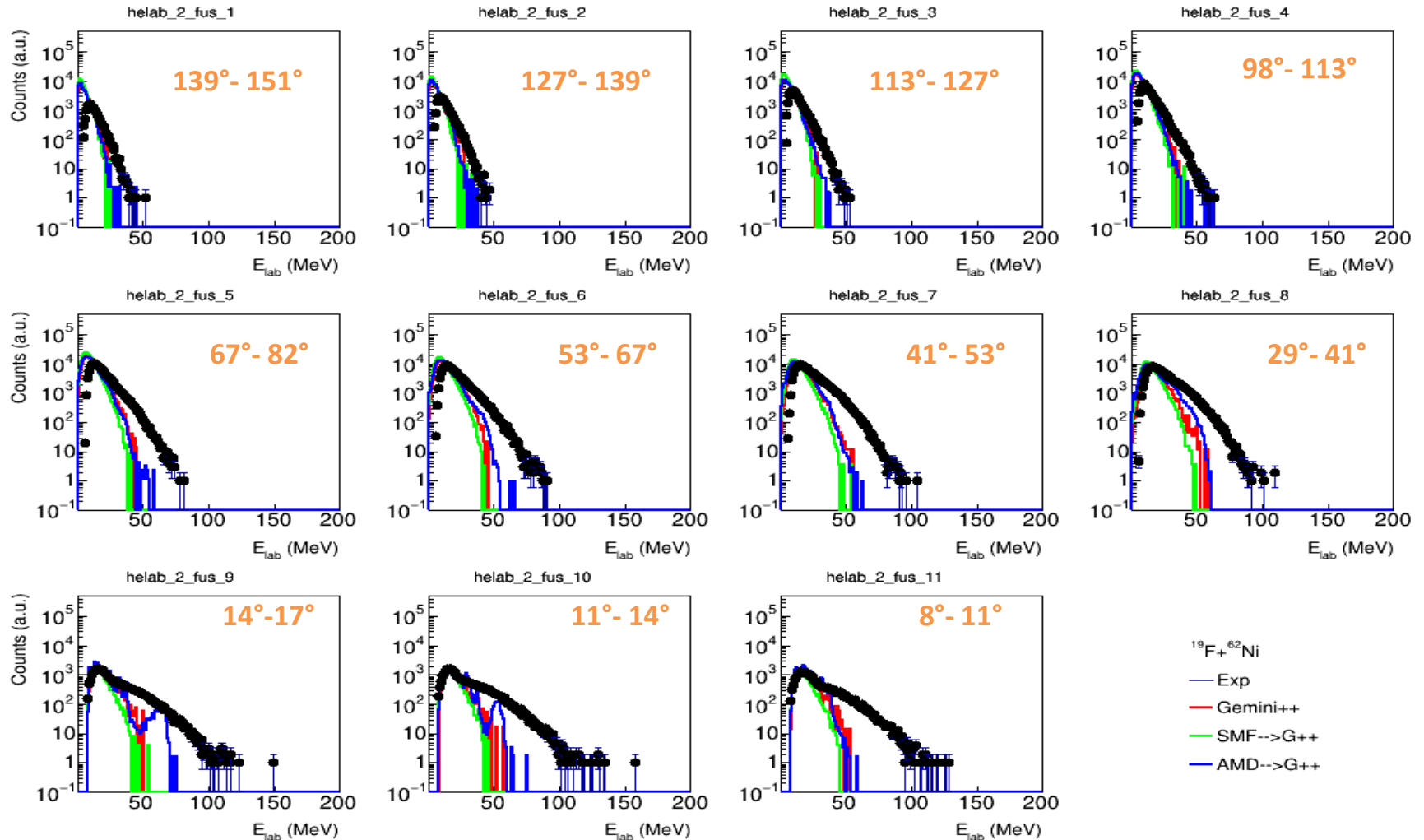


Comparison with different Models: Energy spectra in Lab

$^{19}\text{F} + ^{62}\text{Ni}$

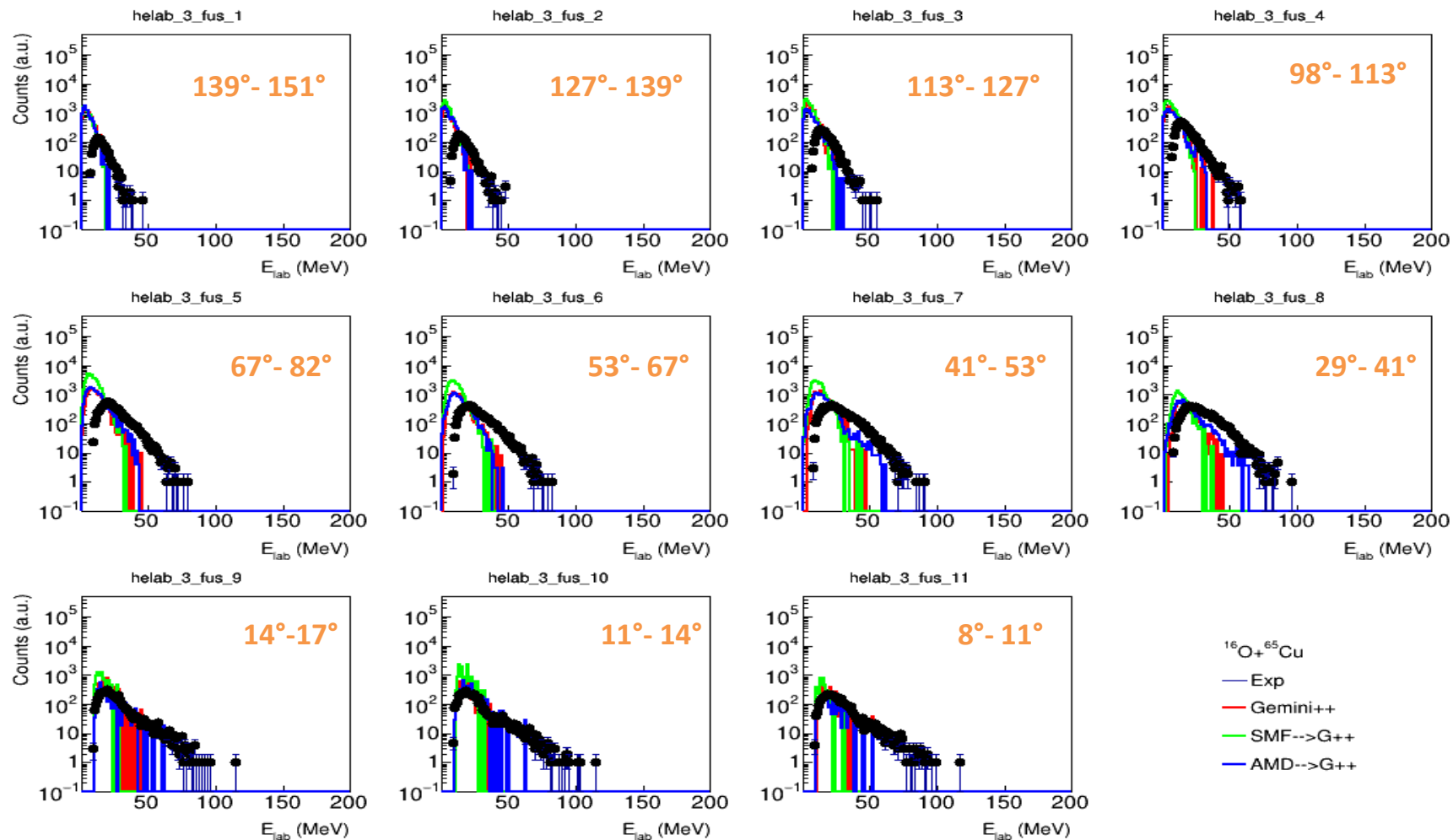
Deuterons

Coincidence with *Residues*



$^{16}\text{O}+^{65}\text{Cu}$

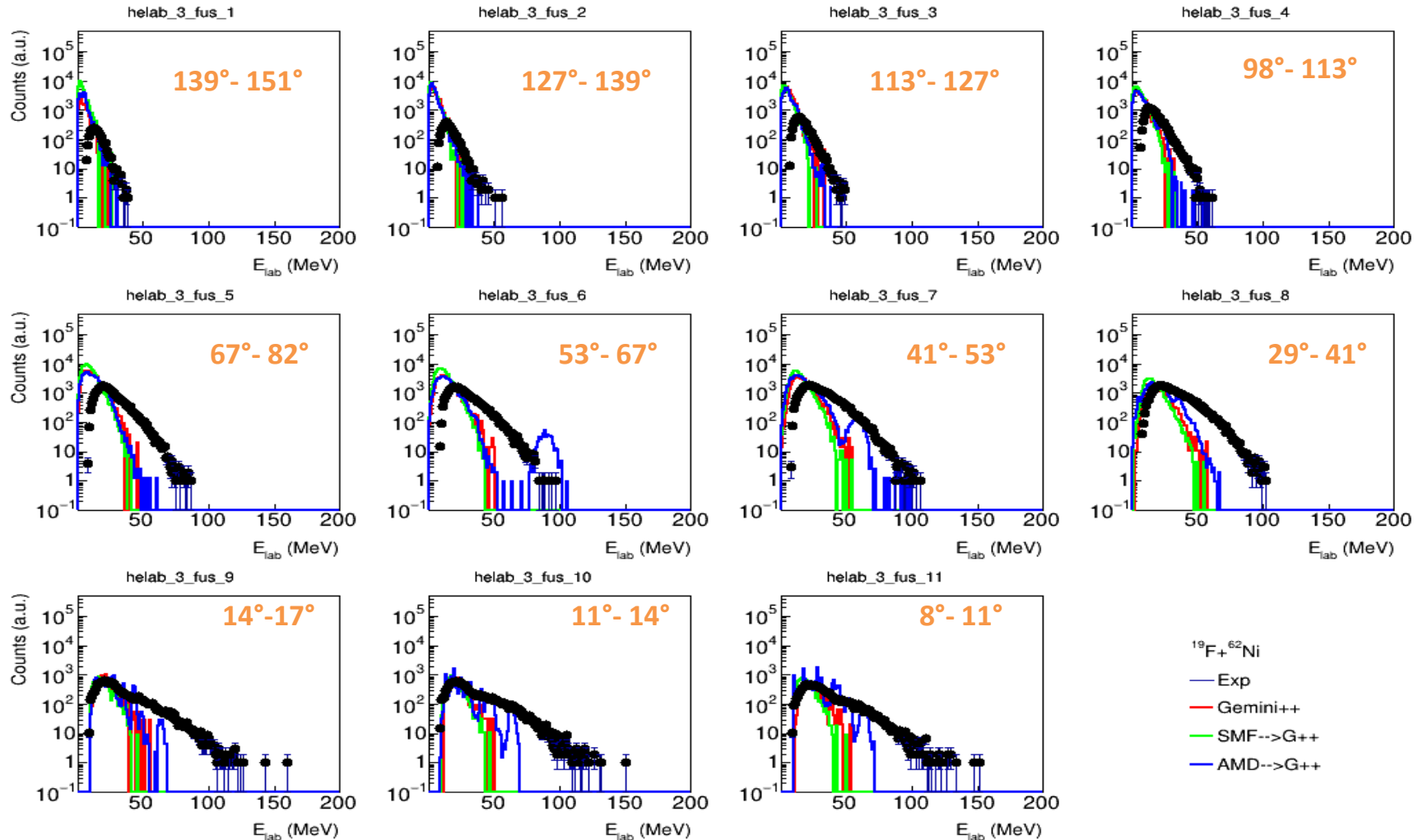
Tritons

Coincidence with *Residues*

$^{19}\text{F} + ^{62}\text{Ni}$

Tritons

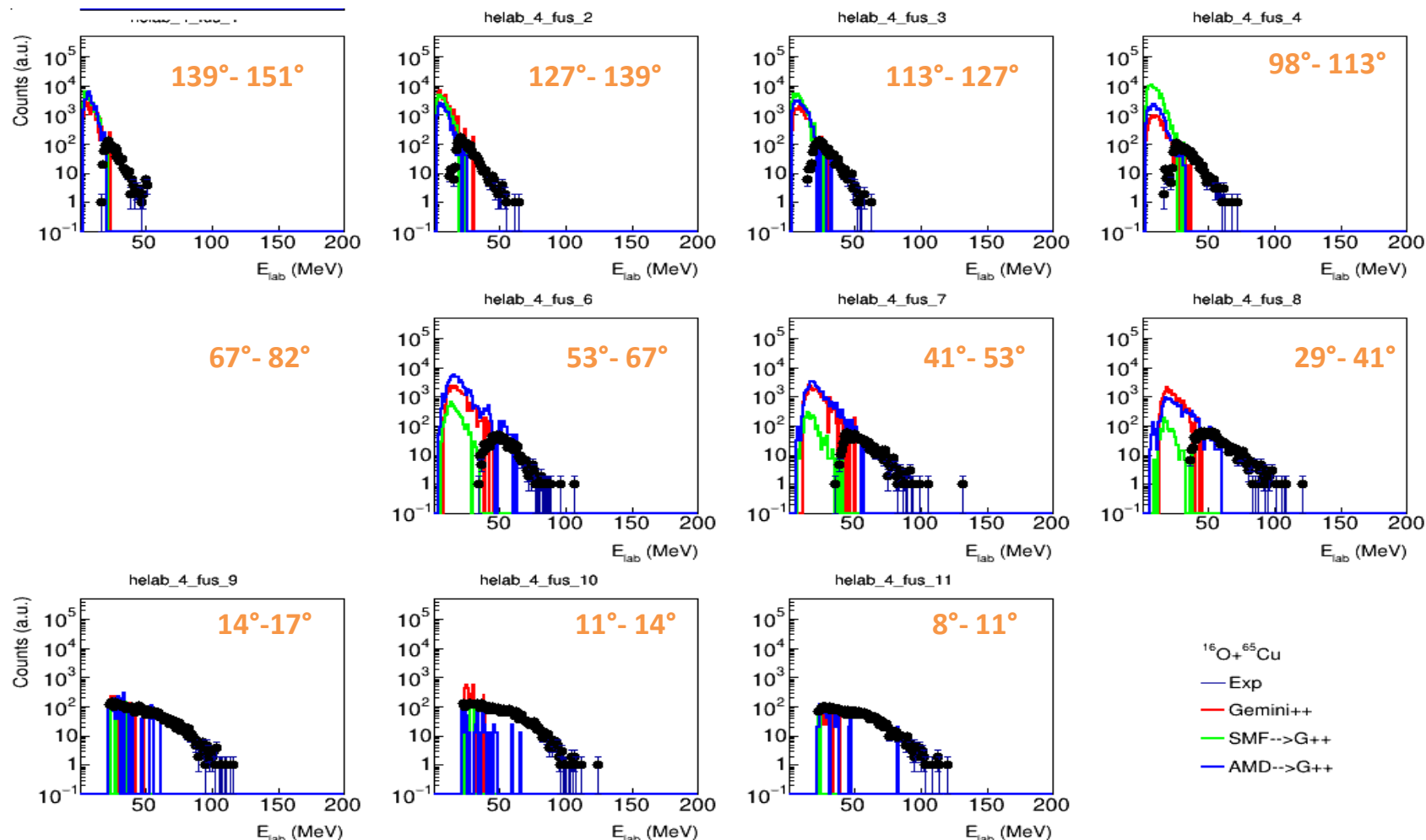
Coincidence with *Residues*



$^{16}\text{O}+^{65}\text{Cu}$

3He

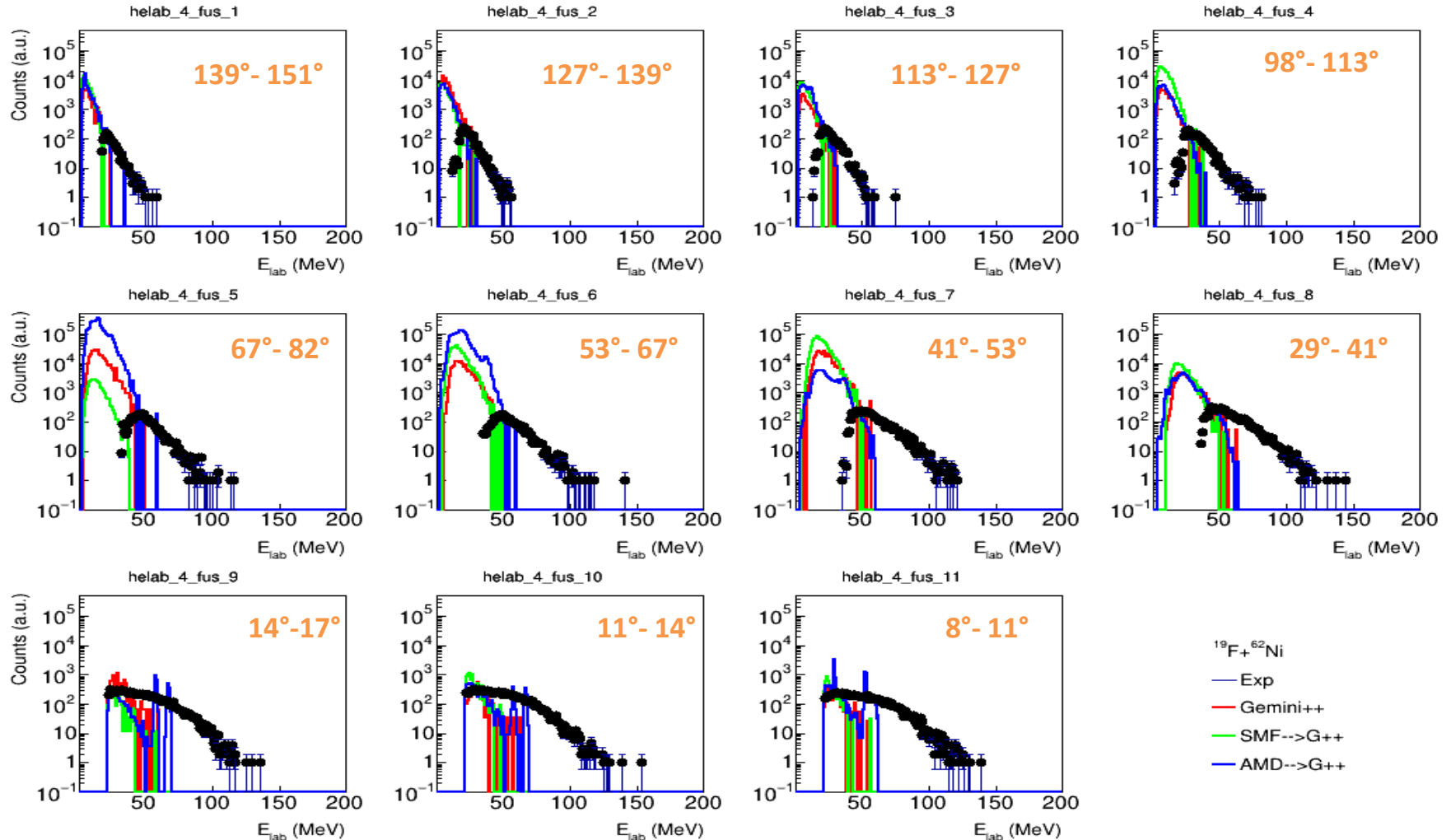
Coincidence with *Residues*



$^{19}\text{F}+^{62}\text{Ni}$

^3He

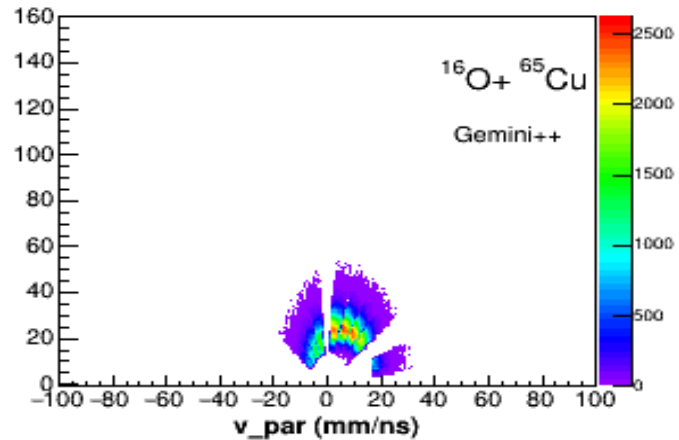
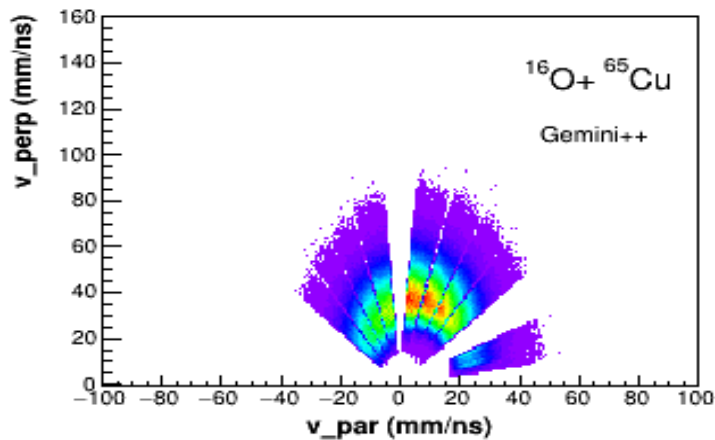
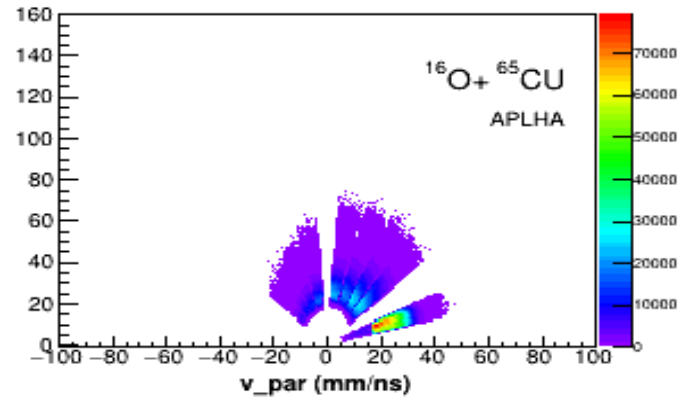
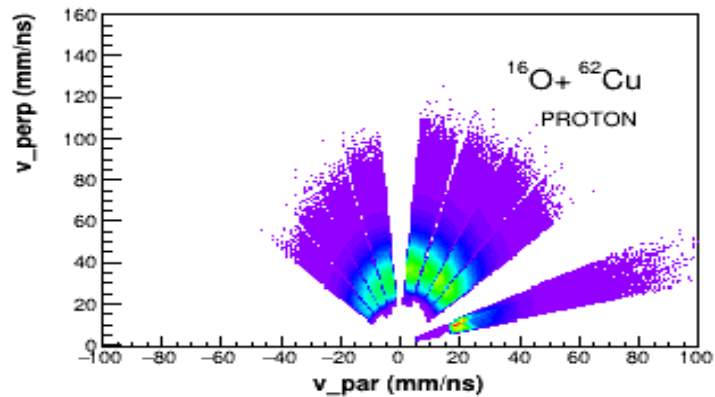
Coincidence with *Residues*



Comparison with filtered GEMINI ++ : $v_{\parallel}$ vs. $v_{\perp}$ in Lab

$^{16}\text{O} + ^{65}\text{Cu}$

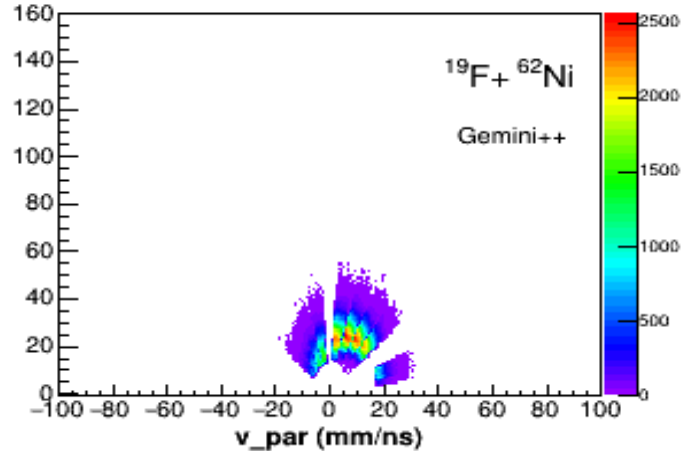
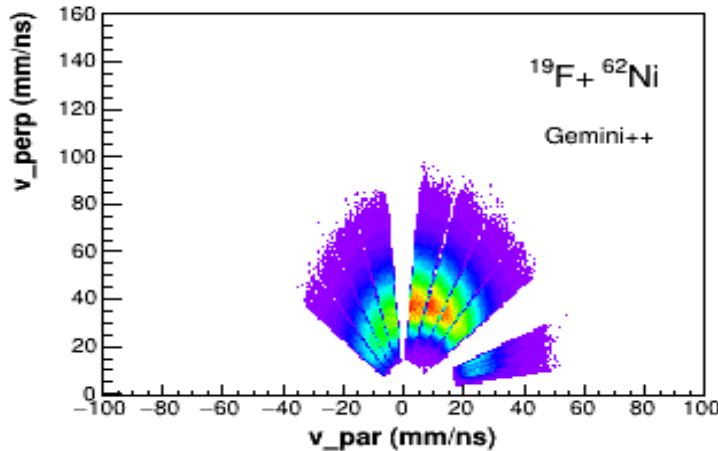
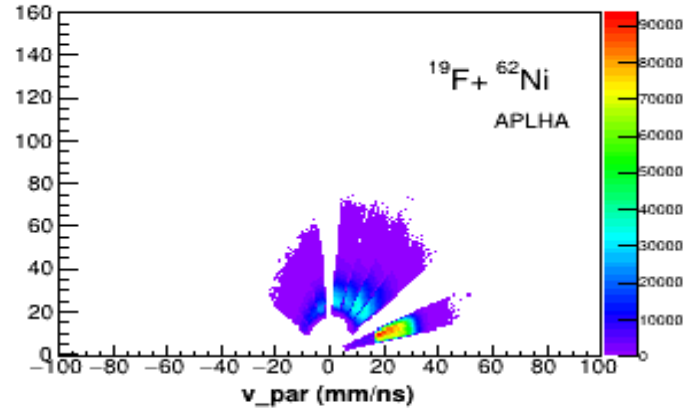
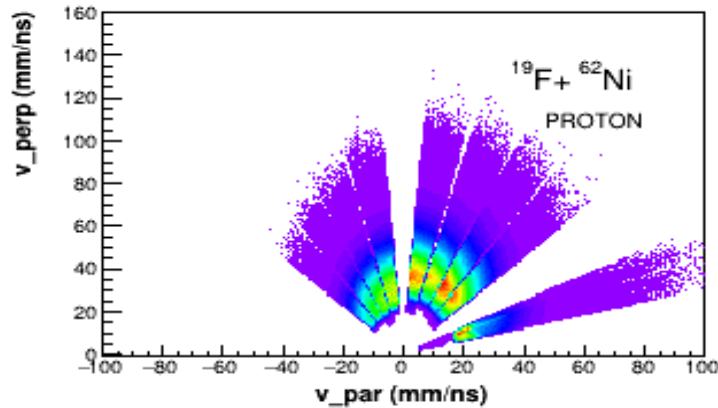
Coincidence with Resideus



Comparison with filtered GEMINI ++ : $v_{\parallel}$ vs. $v_{\perp}$ in Lab

$^{19}\text{F} + ^{62}\text{Ni}$

Coincidence with Residueus



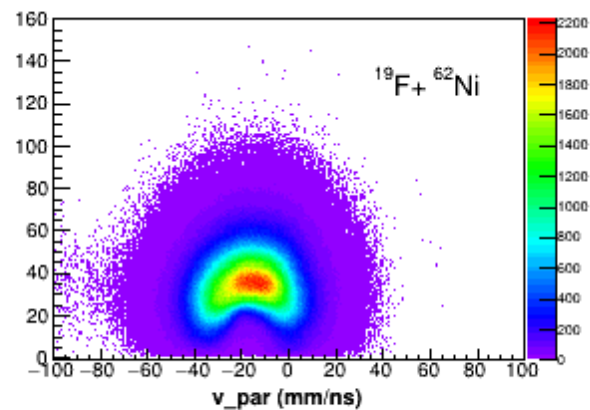
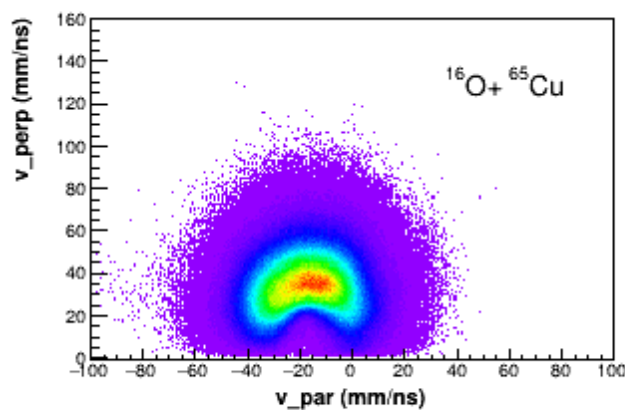
$v_{\parallel}$ vs. $v_{\perp}$ in residue frame

Exp

$^{16}\text{O} + ^{65}\text{Cu}$

$^{19}\text{F} + ^{62}\text{Ni}$

Protons



α -particles

